

# Finding Similar Exercises in Online Education Systems

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## **1 Background and Related Work**

## **2 Problem Definition**

## **3 Study Overview**

## **4 MANN Framework**

## **5 Experiments**

## **6 Conclusion and Future Work**

# Background



- Online education systems
  - Such as KhanAcademy, Knewton, Zhixue
  - Exercise: collected **millions of exercises**
  - Applications: **similar exercise** retrieval and recommendation, personalized cognitive diagnosis based on **exercise similarities**
- Fundamental task
  - **Finding Similar Exercises** (FSE).
  - finding the similar ones of each given exercise

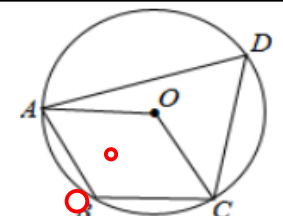


# Exercise

➤ Exercise contains multiple heterogeneous data

- Complex
- Rich semantics

如图，四边形  $ABCD$  内接于  $\odot O$ ，若四边形  $ABCO$  是平行四边形，则  $\angle ADC$  的大小为 ( )  
 A.  $45^\circ$       B.  $50^\circ$       C.  $60^\circ$       D.  $75^\circ$



组卷 320 次   作答 3037 人次   收起   考情   加入试卷

▶ 【答案】

▶ 【解析】  
 解：设  $\angle ADC$  的度数  $= \alpha$ ， $\angle ABC$  的度数  $= \beta$ ；  
 $\because$  四边形  $ABCO$  是平行四边形，  
 $\therefore \angle ABC = \angle AOC$ ；  
 $\therefore \angle ADC = \frac{1}{2}\beta$ ， $\angle ADC = \alpha$ ；而  $\alpha + \beta = 180^\circ$ ，  
 $\therefore \begin{cases} \alpha + \beta = 180^\circ \\ \alpha = \frac{1}{2}\beta \end{cases}$ ，  
 解得： $\beta = 120^\circ$ ， $\alpha = 60^\circ$ ， $\angle ADC = 60^\circ$ ，  
 故选：C。

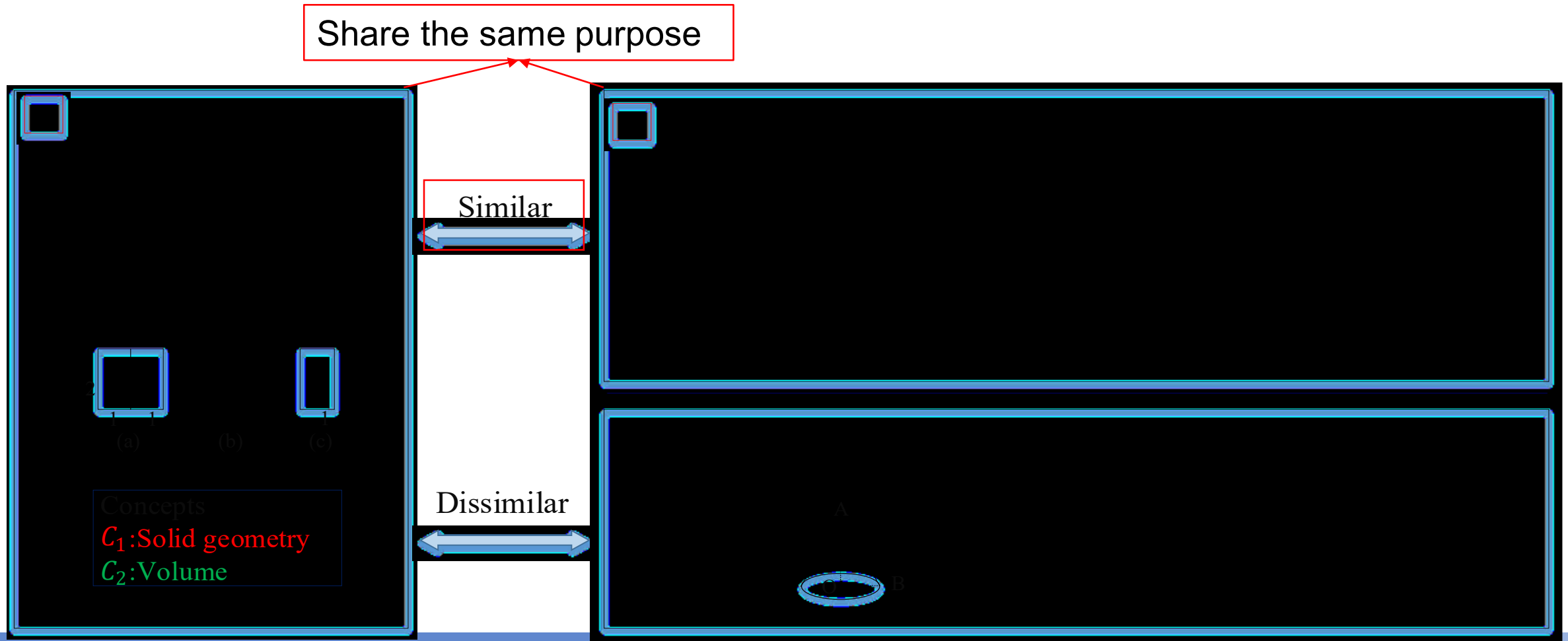
设  $\angle ADC$  的度数  $= \alpha$ ， $\angle ABC$  的度数  $= \beta$ ，由题意可得  
 该题主要考查了圆周角定理及其应用问题；应牢固掌握该定理并能灵活运用。

▶ 【知识点】   平行四边形的性质   圆周角定理及其推论   圆内接四边形的性质

▶ 【题型】   选择题

# What are similar exercises?

- Following Educational Psychology, **similar exercises** are those having **the same purpose** embedded in exercise contents.



# Background

- Existing solutions for **Finding Similar Exercises** (FSE) task
  - Manual Labeling
    - On a **small quantity** of exercises
    - requires **strong expertise** and takes **much time**
    - **not suitable** for **large-scale** online education systems containing millions of exercises
  - Methods based on text similarity
    - Use the same concepts or the similar words
    - **cannot** exploit rich semantics in the **heterogeneous data**
- **Urgent Issue**
  - Design an effective FSE solution for large-scale online education systems by exploit the heterogeneous data to understand exercise semantics and purposes.



# Challenge 1 for FSE

- Exercises contain **multiple heterogenous data**.
  - texts
  - Images
  - knowledge concepts
- integrates multiple heterogeneous data to understand and represent exercise semantics and purposes.

# Challenge 2 for FSE

- In **a single exercise**, different parts/words of the text are associated with different concepts (text-concept) or images (text-image).
- For better understanding each exercise, it is necessary to capture these **text-concept** and **text-image associations**.





# Challenge 3 for FSE

- A pair of similar exercises may consist of different texts, images and concepts.
- Finding similar exercises needs to measure the similar parts in each exercise pair by deeply interpreting their semantic relations.



# Related Work

## ➤ Studies on FSE

- Methods based on text similarity
  - Use the same concepts or the similar words
  - Vector Space Model (VSM)
- Methods based on learners' performance data

**Neglect semantics in heterogeneous materials of exercises.**

## ➤ Multimodal Learning

- Powerful approach to handle heterogeneous data
- Sound-video, video-text, image-text

**Cannot understand exercise purposes or measure similar parts between two exercises**

## ➤ Pair Modeling

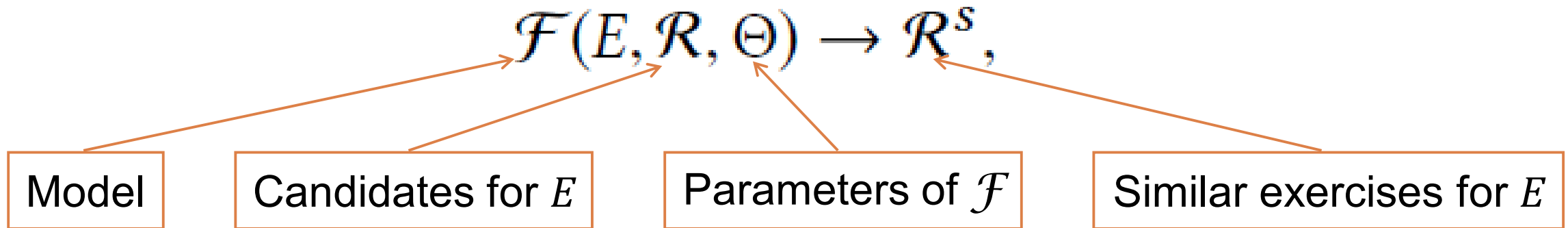
- Learn the relations between two instances in a pair
- Sentence pair, image pair, video-sentence pair

**Cannot handle instances having multiple heterogeneous data**

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# Problem Definition

- **Given:** exercises with corresponding heterogeneous materials including **texts, images and concepts**
- **Goal:** learn a model  $\mathcal{F}$  to **measure the similarity scores** of exercise pairs and **find similar exercises for any exercise**  $E$  by ranking the candidate ones  $\mathcal{R}$  with similarity scores



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# Study Overview

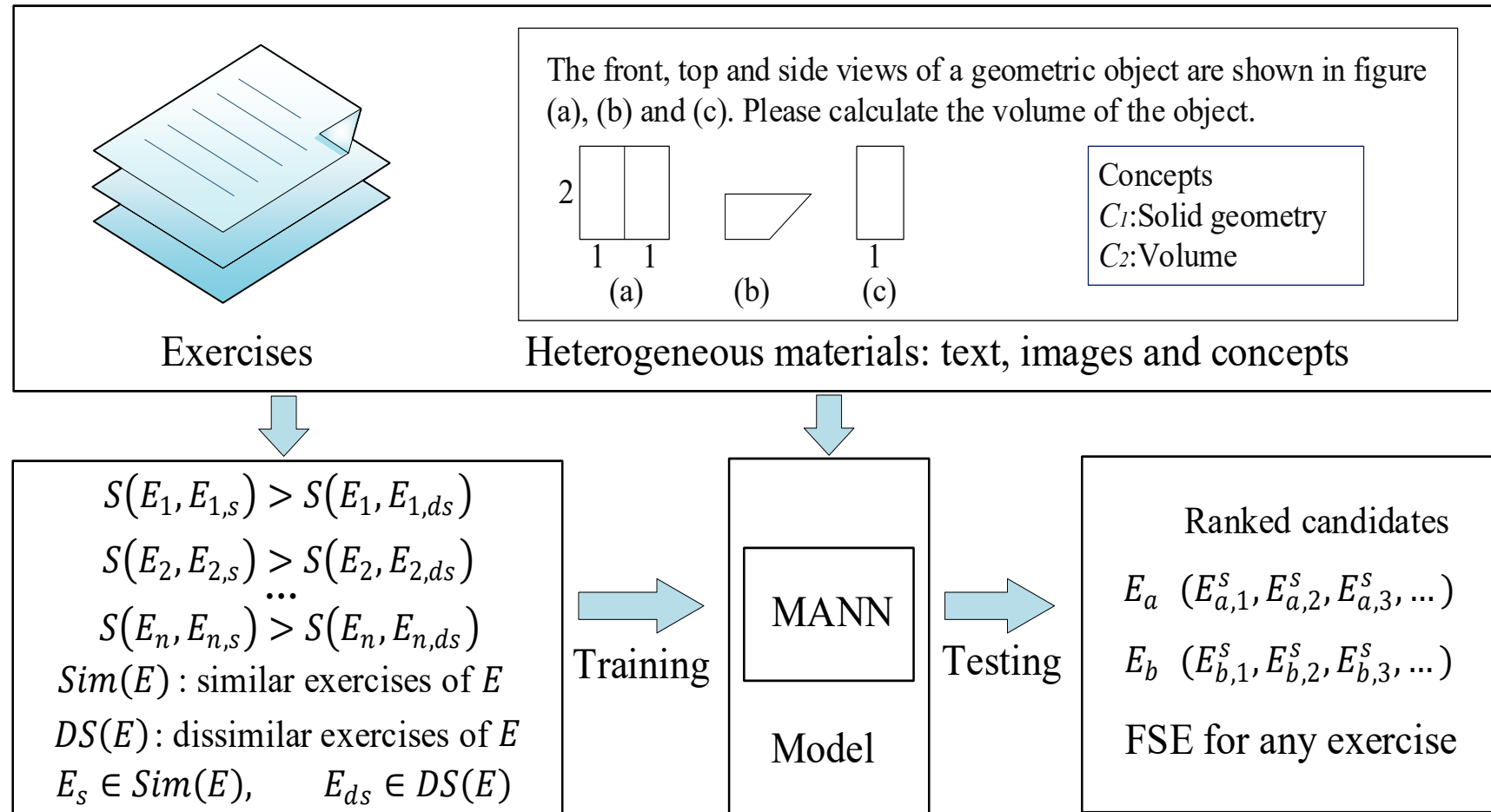
## Two-stage solution

### Training stage

- MANN
- Pairwise training

### Testing stage

- FSE for any exercise



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## ➤ Multimodal Attention-based Neural Network (MANN)

- Learn a **unified semantic representation** of each exercise by handling its heterogeneous materials in a multimodal way

**Challenge 1: multimodal exercises understanding and representation**

- Propose **two attention strategies** to capture the text-image and text-concept associations in each single exercise

**Challenge 2: learning text-image, text-concept associations**

- Design a **Similarity Attention** to measure the similar parts in each exercise pair with their semantic representations

**Challenge 3: learning similar parts**

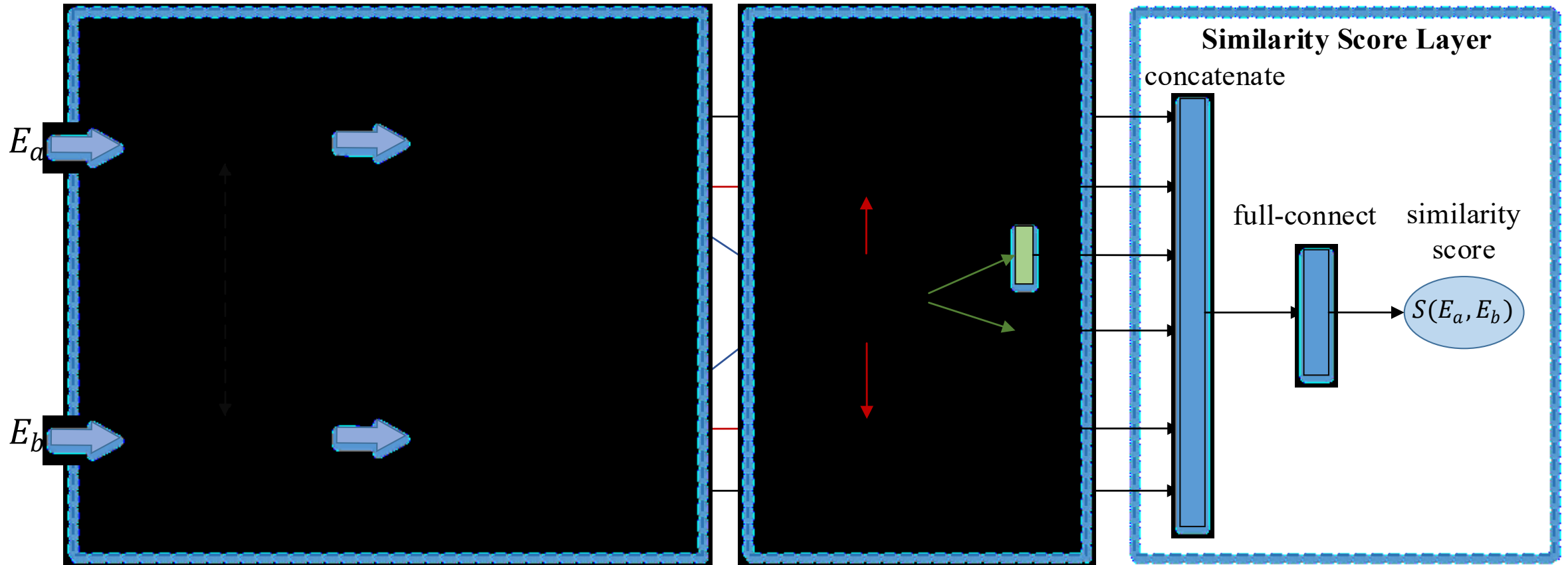


# MANN Framework



Input: a pair of exercise (  $E_a, E_b$  )

Output: similarity score



**Challenge 1: multimodal exercises understanding and representation**

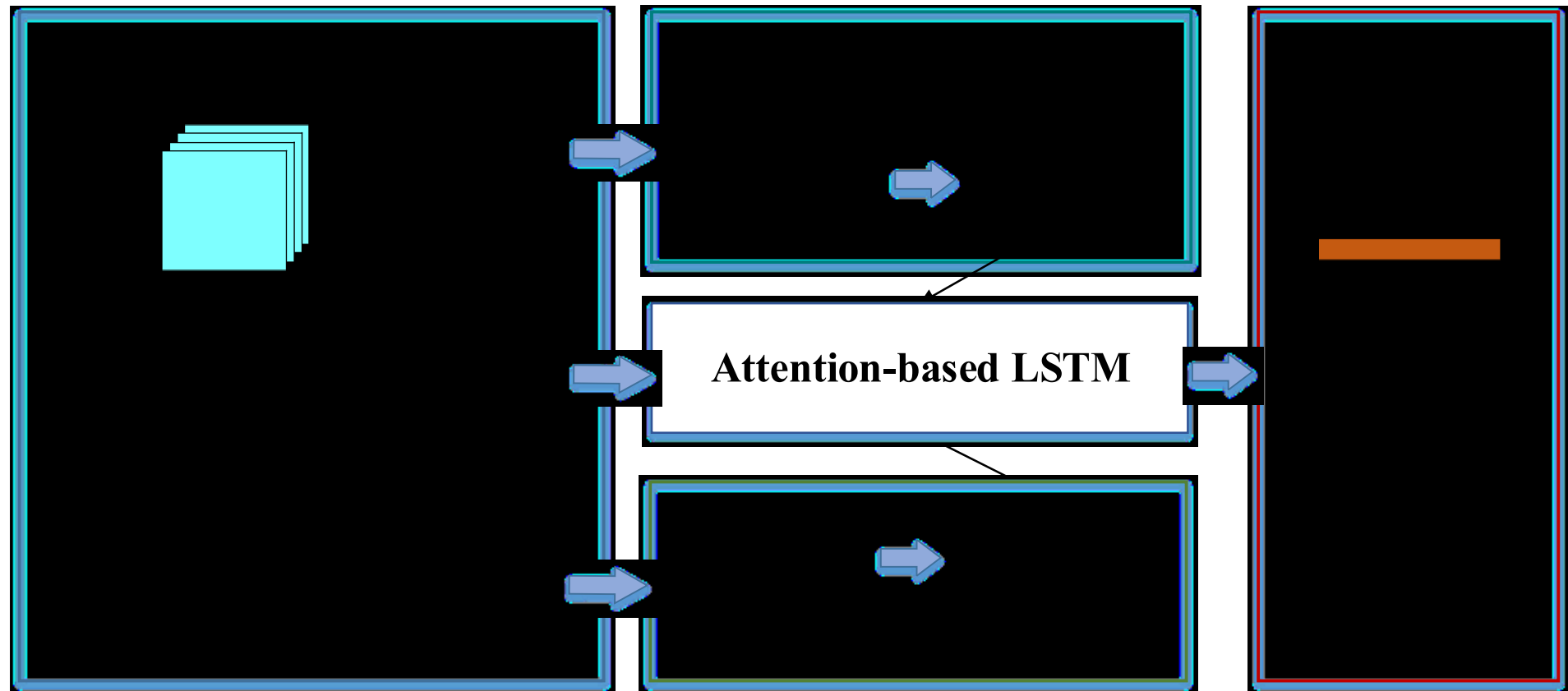
**Challenge 2: learning text-image, text-concept associations**

**Challenge 3: learning similar parts**

# MANN Framework - MERL

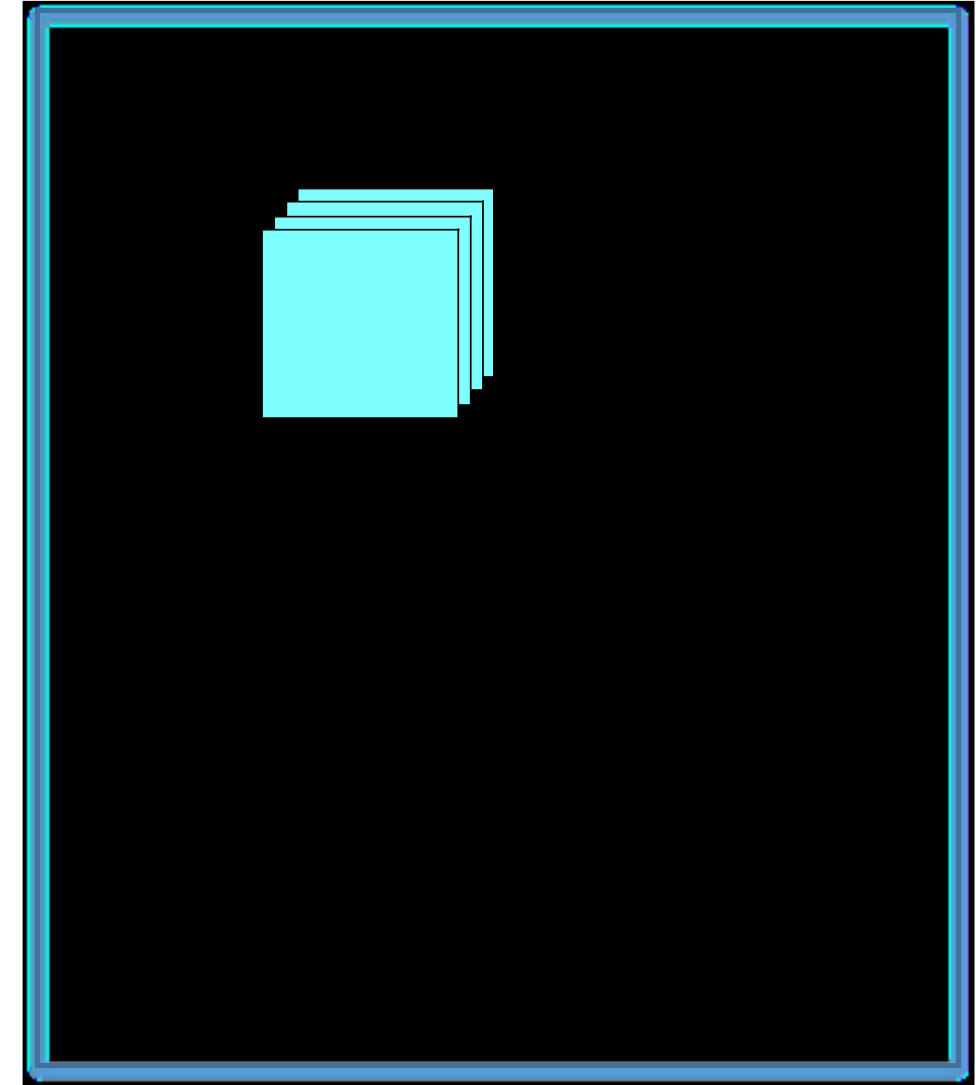


- Multimodal Exercise Representing Layer (MERL)
- **Goal:**
  - learn a unified semantic representation for each exercise by integrating its heterogeneous materials in a multimodal way



# MANN Framework - Exercise Input

- Exercise Input: for each exercise
  - Text (*ET*):
    - Sequence words:  $ET = (w_1, w_2, \dots, w_N)$
    - Each word:  $d_0$ -dimensional word2vec
  - Images (*EI*):
    - A tensor :  $EI = (p_1, p_2, \dots, p_M) \in \mathbb{R}^{M \times 64 \times 64}$
    - Each image: a 64 x 64 matrix
  - Concepts (*EC*):
    - A matrix :  $EC = (k_1, k_2, \dots, k_L) \in \{0, 1\}^{L \times L_{all}}$
    - Each concept: one-hot vector



# MANN Framework - Image CNN

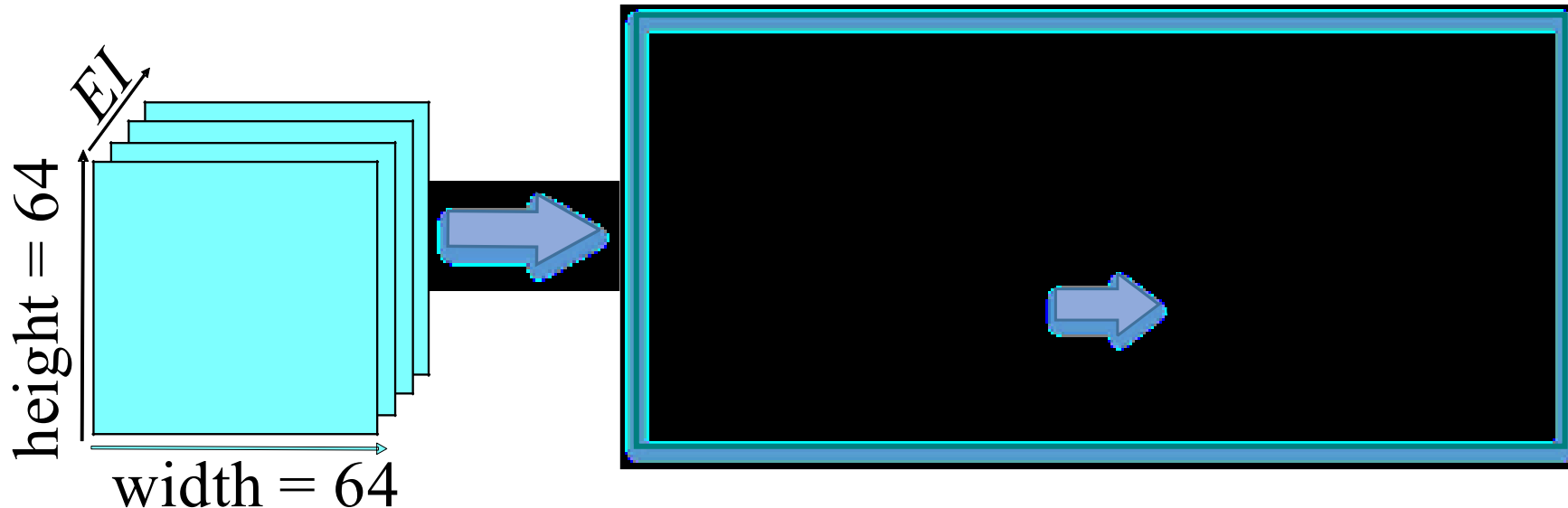
- Image CNN
- **Goal:**
  - gets the feature vector for each image.

$$v_i = \sigma(\text{ImCNN}(p_i)),$$

feature vector

Image CNN

A 64 x 64 Image



# MANN Framework – Concept Embedding

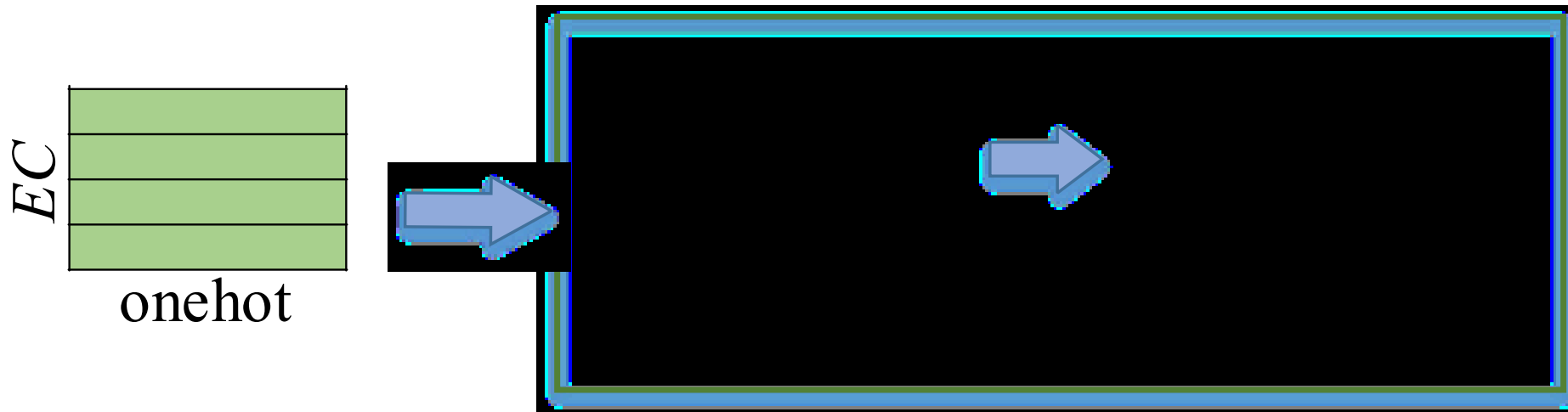
- Concept Embedding
- **Goal:**
  - convert one-hot vectors of concepts into low-dimensional ones with dense values.

$$u_i = k_i W_u,$$

Dense vector of concept  $i$

One-hot vector

Parameters of Concept Embedding



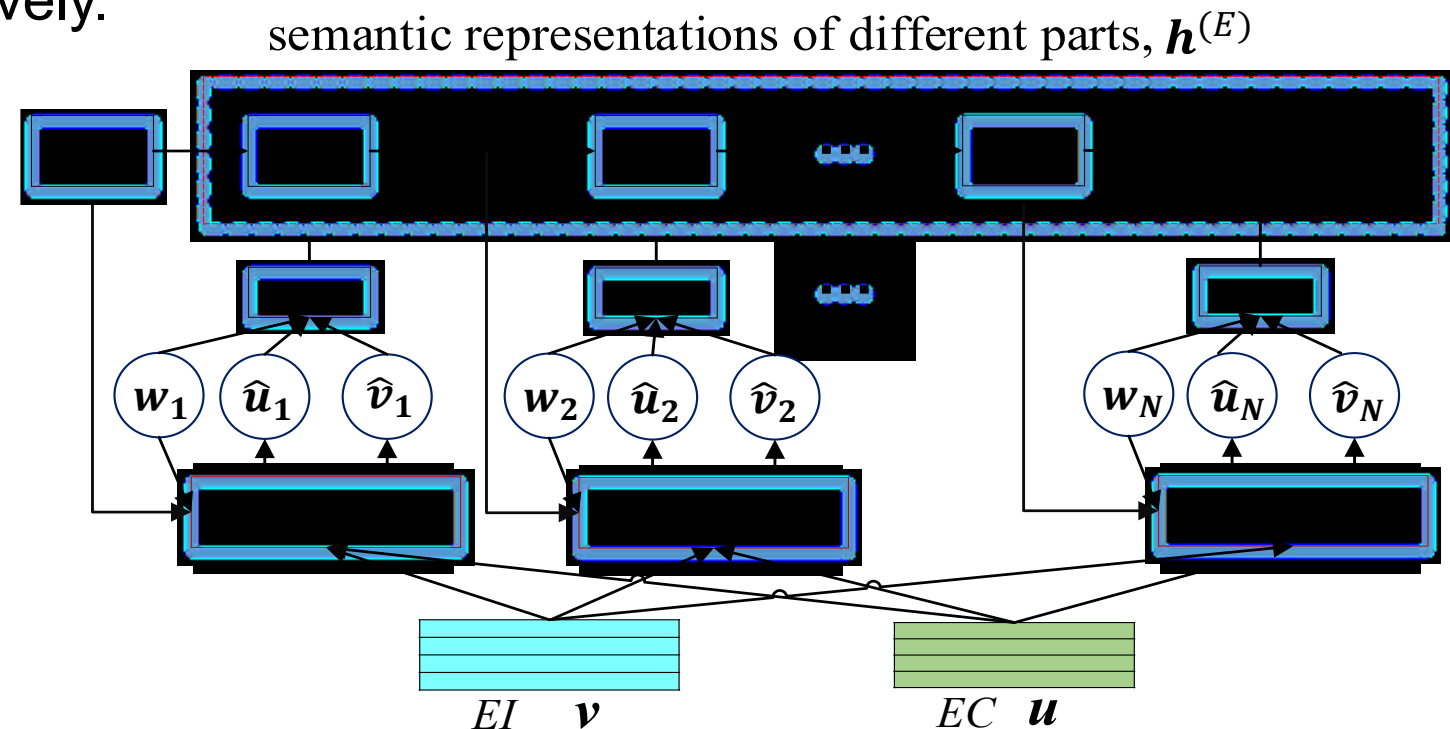
# MANN Framework - Attention-based LSTM



## ➤ Attention-based LSTM

### ➤ Goal:

- learn a unified semantic representation for each exercise by integrating its all heterogeneous materials
- capture text-concept and text-image associations with Text-Concept Attention (TCA) and Text-Image Attention (TIA), respectively.



# MANN Framework - Attention-based LSTM

- **LSTM input:** sequence  $x = (x_1, x_2, \dots, x_N)$  combined with all materials of each exercise.

$$x_t = w_t \oplus \hat{u}_t \oplus \hat{v}_t$$

t-th word representation  
in the text ET

Representation of the associated  
concepts learned by TCA

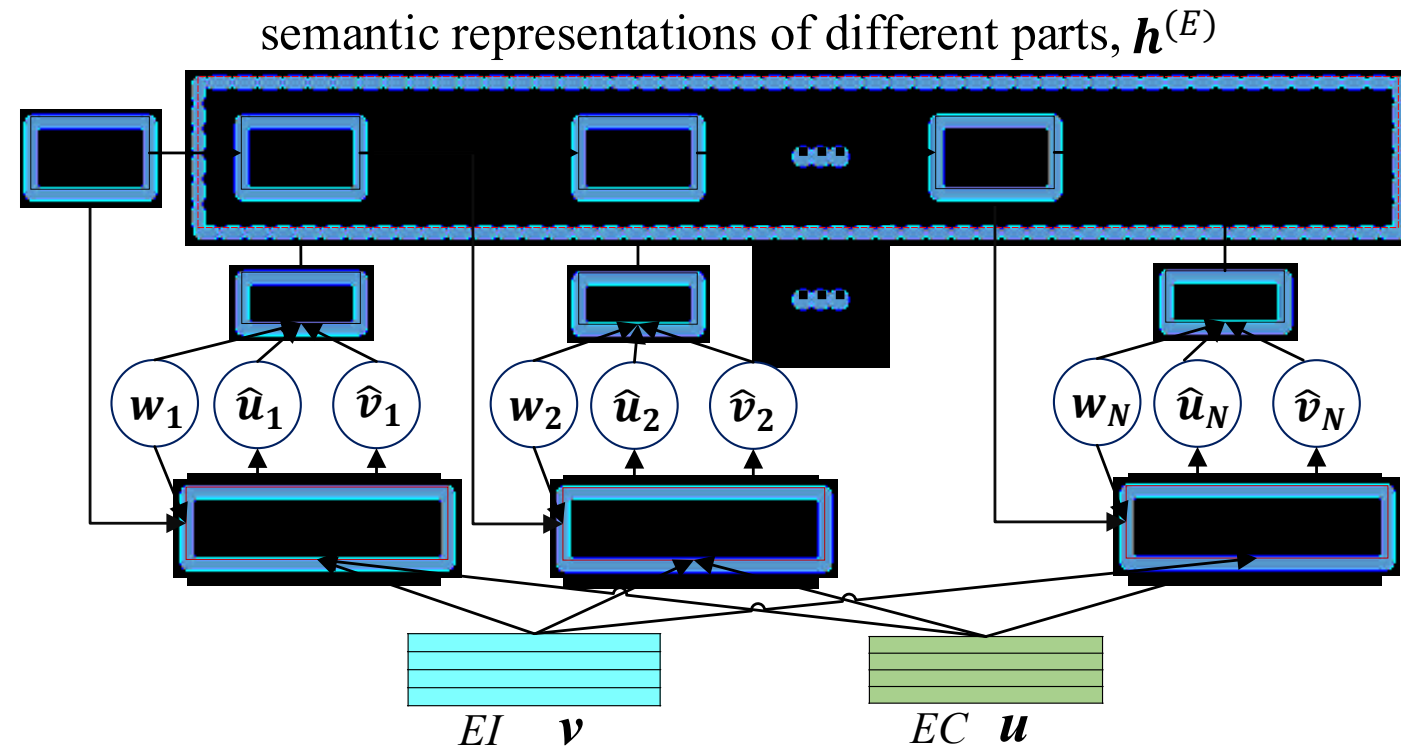
Representation of the associated  
images learned by TIA

- **Output:** unified semantic representation  
for an input exercise  $E$ .

$$(r^{(E)}, h^{(E)})$$

Whole semantic  
representation of  $E$

Representations of  
different parts of  $E$



# MANN Framework

- Text-Concept Attention (TCA): capture text-concept associations.

Representation of the associated concepts

Attention score after normalization

$$\hat{u}_t = \sum_{j=1}^L \alpha_j u_j, \quad \alpha_j = \frac{\varphi(u_j, w_t, h_{t-1})}{\sum_{i=1}^L \varphi(u_i, w_t, h_{t-1})},$$

$$\varphi(u_j, w_t, h_{t-1}) = V_{ac} \tanh(W_{ac}[u_j \oplus w_t \oplus h_{t-1}]),$$

Association score between the  $j$ -th concept  $u_j$  and  $w_t$  in  $E$

parameters of TCA

the  $t - 1^{th}$  hidden state

- Text-Image Attention (TCA): capture text-image associations.
  - modeled similarly as TCA.



# MANN Framework - Similarity Attention

## ➤ Similarity Attention

### ➤ Goal:

- measure similar parts between two exercises with their unified semantic representations, and learn attention representations for them.

## ➤ Attention Matrix **A**

- measure similar parts between  $E_a$  and  $E_b$

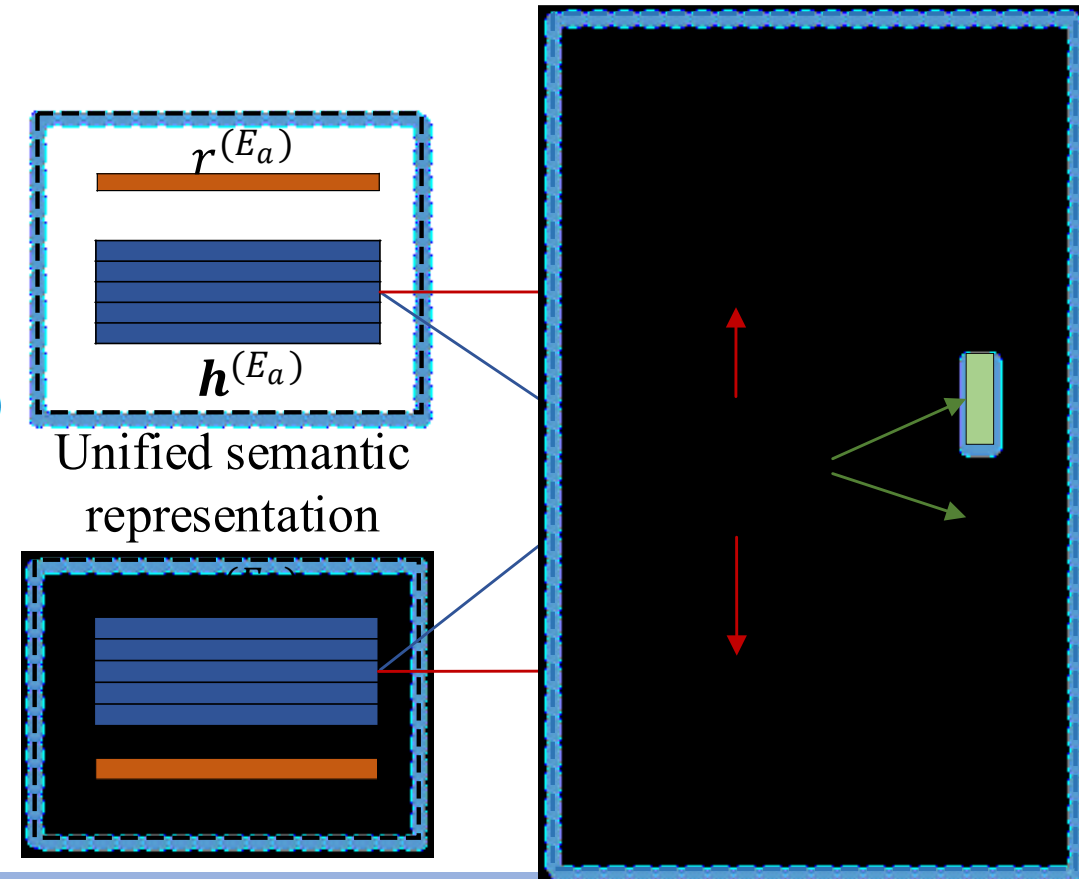
$$A_{i,j} = \cos(h_i^{(E_a)}, h_j^{(E_b)}), \quad 1 \leq i \leq N_{E_a}, 1 \leq j \leq N_{E_b}$$

## ➤ Similarity attention representations $s^{(E_a)}$ and $s^{(E_b)}$

$$s_i^{(E_a)} = \sum_{k=1}^{N_{E_b}} A_{i,k} \quad s_j^{(E_b)} = \sum_{k=1}^{N_{E_a}} A_{k,j}$$

## ➤ Semantic attention representations $h_{att}^{(E_a)}$ and $h_{att}^{(E_b)}$

$$h_{att}^{(E_a)} = \sum_{i=1}^{N_{E_a}} A_{i,N_{E_b}} h_i^{(E_a)}, \quad h_{att}^{(E_b)} = \sum_{j=1}^{N_{E_b}} A_{N_{E_a},j} h_j^{(E_b)}.$$



# MANN Framework - Similarity Score Layer



## ➤ Similarity Score Layer

### ➤ Goal:

- calculating the similarity score of each exercise pair to rank candidate exercises to find similar ones for any exercise.

Whole semantic representation

similarity attention representation

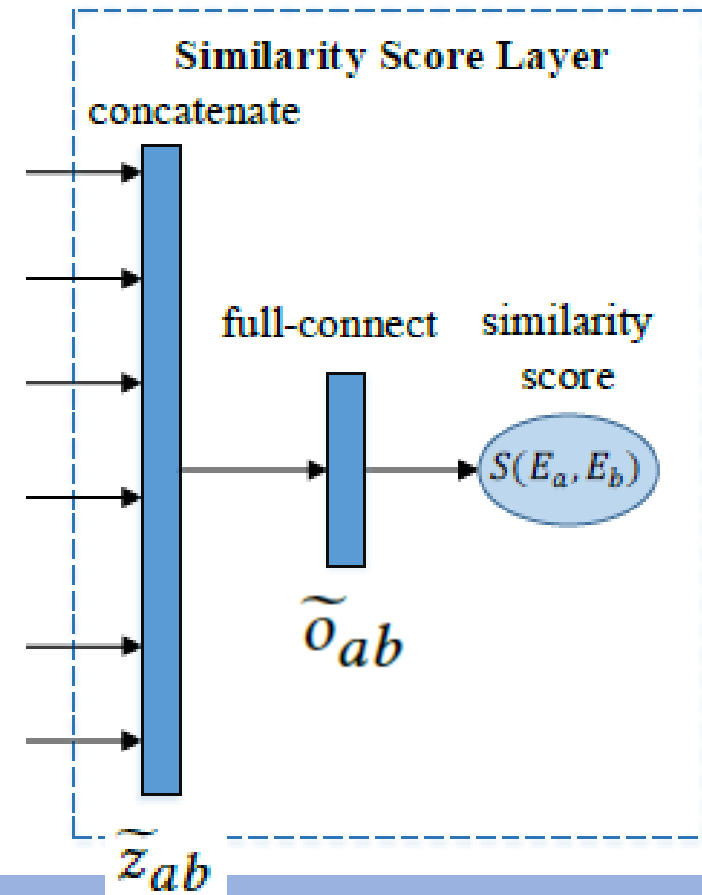
semantic attention representation

$$\tilde{z}_{ab} = r^{(E_a)} \oplus r^{(E_b)} \oplus s^{(E_a)} \oplus s^{(E_b)} \oplus h_{att}^{(E_a)} \oplus h_{att}^{(E_b)}$$

$$\tilde{o}_{ab} = \text{ReLU}(\mathbf{W}_1 \tilde{z}_{ab} + \mathbf{b}_1)$$

$$S(E_a, E_b) = \sigma(\mathbf{W}_2 \tilde{o}_{ab} + \mathbf{b}_2)$$

similarity score



## ➤ Pairwise loss function

$$\mathcal{L}(\Theta) = \sum_{E, E_s, E_{ds}} \max(0, \mu - (S(E, E_s) - S(E, E_{ds}))) + \lambda_{\Theta} \|\Theta\|^2$$

Diagram illustrating the components of the pairwise loss function  $\mathcal{L}(\Theta)$ :

- a margin**: Points to  $\mu$ .
- similarity score**: Points to  $S(E, E_s)$ .
- regularization hyperparameter**: Points to  $\lambda_{\Theta}$ .
- a labeled similar exercise of E**: Points to  $E_s$ .
- a dissimilar exercise of E**: Points to  $E_{ds}$ .
- parameters of MANN**: Points to  $\Theta$ .

- Similar exercises (e.g.  $E_s$ ) are labeled by education experts (e.g. teachers).
- Dissimilar exercises (e.g.  $E_{ds}$ ) are sampled in the training process:
  - **Sampling Randomly (Random)**: At each iteration, we randomly select a number of dissimilar exercises from all the dissimilar ones of  $E$ .
  - **Sampling by Concepts (Concept)**: At each iteration, we randomly select a number of dissimilar exercises from those having at least one common concept with  $E$ .

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# Experiments

## ➤ Experiments dataset

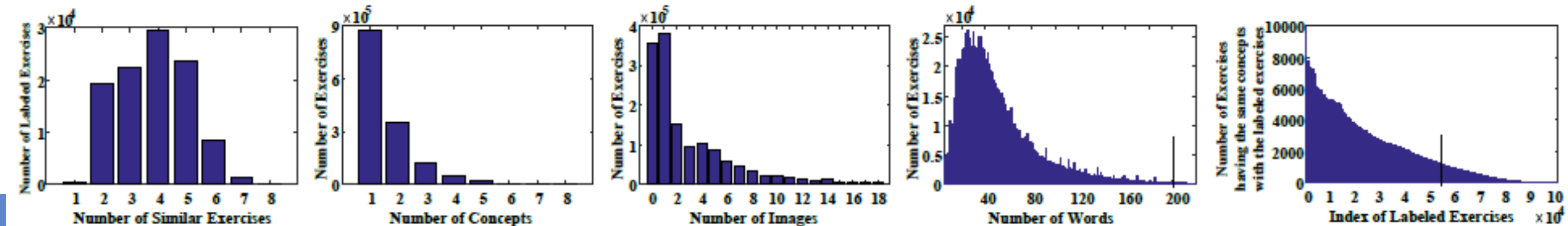
- supplied by iFLYTEK, collected from Zhixue.
- contains **1,420,727** math exercises.

## ➤ Observations in dataset

- On average **3.84** similar exercises are labeled for the given one.
- Each exercise consists of about **1.61 concepts** and **3.04 images**.
- About **75%** exercises have at least one image.
- **99%** exercises contain less than 200 words in the text.
- More than **55%** labeled exercises have the same concepts with at least 1,000 exercises.

Table 2: The statistics of the dataset.

Statistics	Values
number of exercises	1,420,727
number of exercises having images	1,064,964
number of labeled exercises	104,515
number of similar pairs	401,476
number of similar pairs having the same concepts	174,672
Average similar pairs per labeled exercise	3.84
Average concepts per exercise	1.61
Average images per exercise	3.04



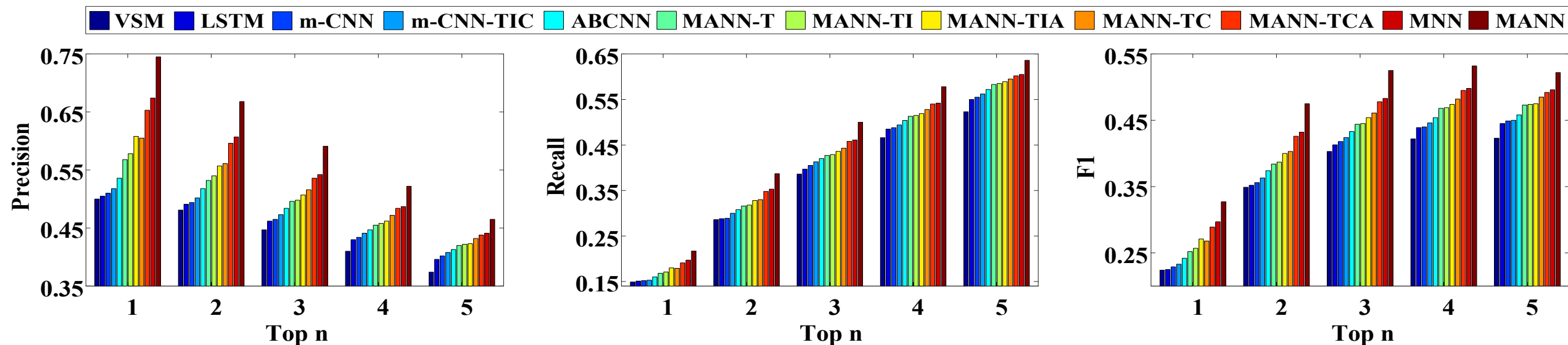
## ➤ Baseline Approaches

- Variants of MANN: **MANN-T** (only Text), **MANN-TI** (Text and Images), **MANN-TIA** (with TIA), **MANN-TC** (Text and Concepts), **MANN-TCA** (with TCA), **MNN** (Using Text, Images and Concepts, but without TIA and TCA).
- **VSM**: Vector space model (VSM) is applied for the FSE task based on texts of exercises.
- **LSTM**: learn the semantic similarity between sentences based on the texts.
- **ABCNN**: a network architecture based on texts for modeling sentence pairs.
- **m-CNN**: integrating texts and images into a vectorial representation.
- **m-CNN-TIC**: a variant of m-CNN integrating texts, images and concepts.

## ➤ Evaluation Metrics

- **Precision**, **Recall**, and **F1** at top  $n = 1, 2, 3, 4, 5$ .
- As on average 3.84 similar exercises are labeled for the given one.

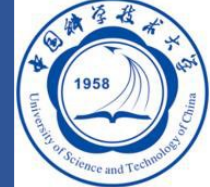
## Performance Comparison



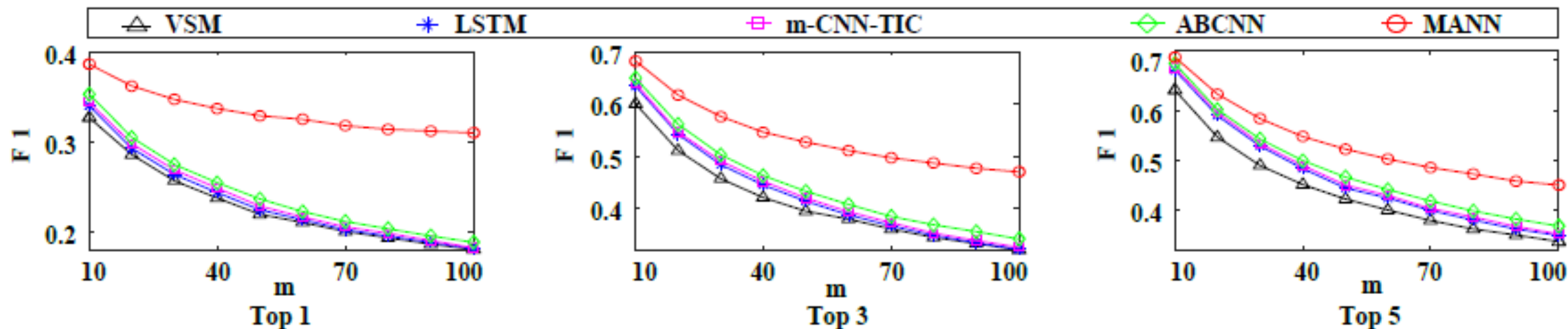
- **MANN achieves the best performance**, and the **variants** of MANN also perform **better** than other baselines.
- MANN-T performs better than ABCNN, indicating the **effectiveness of Similarity Attention** to measure similar parts of an exercise pair.
- MANN-TIA beats MANN-TI, and MANN-TCA performs better than MANN-TC, demonstrating the **effectiveness of TIA and TCA**.
- MANN performs best and MNN ranks the second, suggesting that it is **more effective** for the FSE task by integrating texts, images and concepts, and further demonstrating the effectiveness of TIA and TCA.



# Experiments



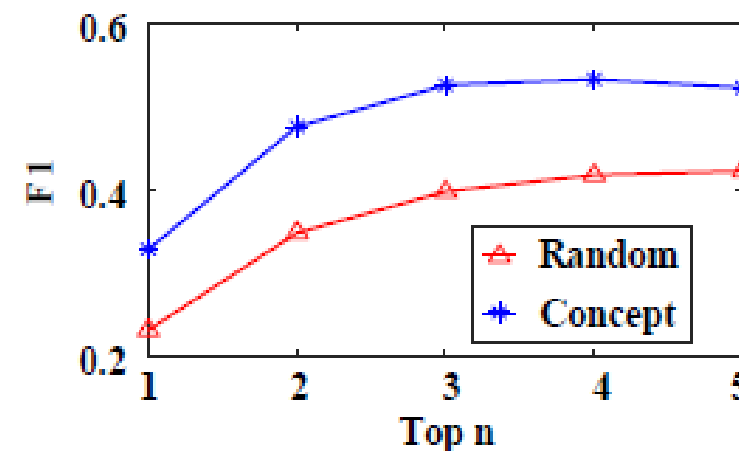
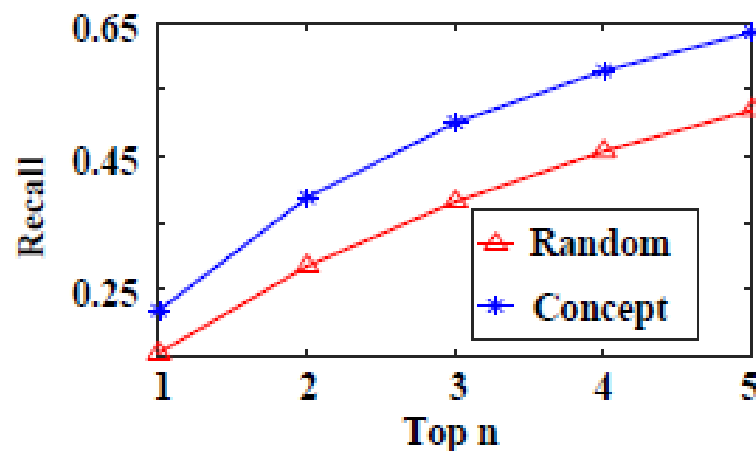
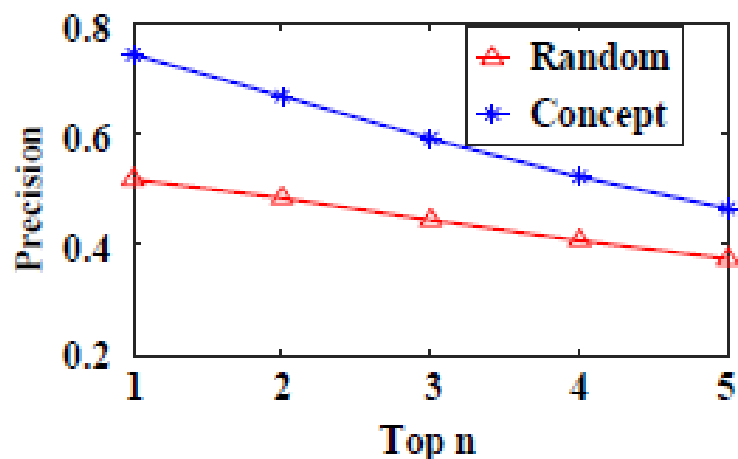
## ➤ Performance with Different Number of Sampled Dissimilar Exercises ( $m$ )



- MANN still **outperforms** baselines with different  $m$ .
- The F1 value of MANN **degrades the most slowly** while  $m$  increases.
- The more unlabeled exercises (i.e. negative samples) in the testing set, the **more improvement** of MANN compared with the baselines could be observed.



## ➤ Influence of Sampling Ways



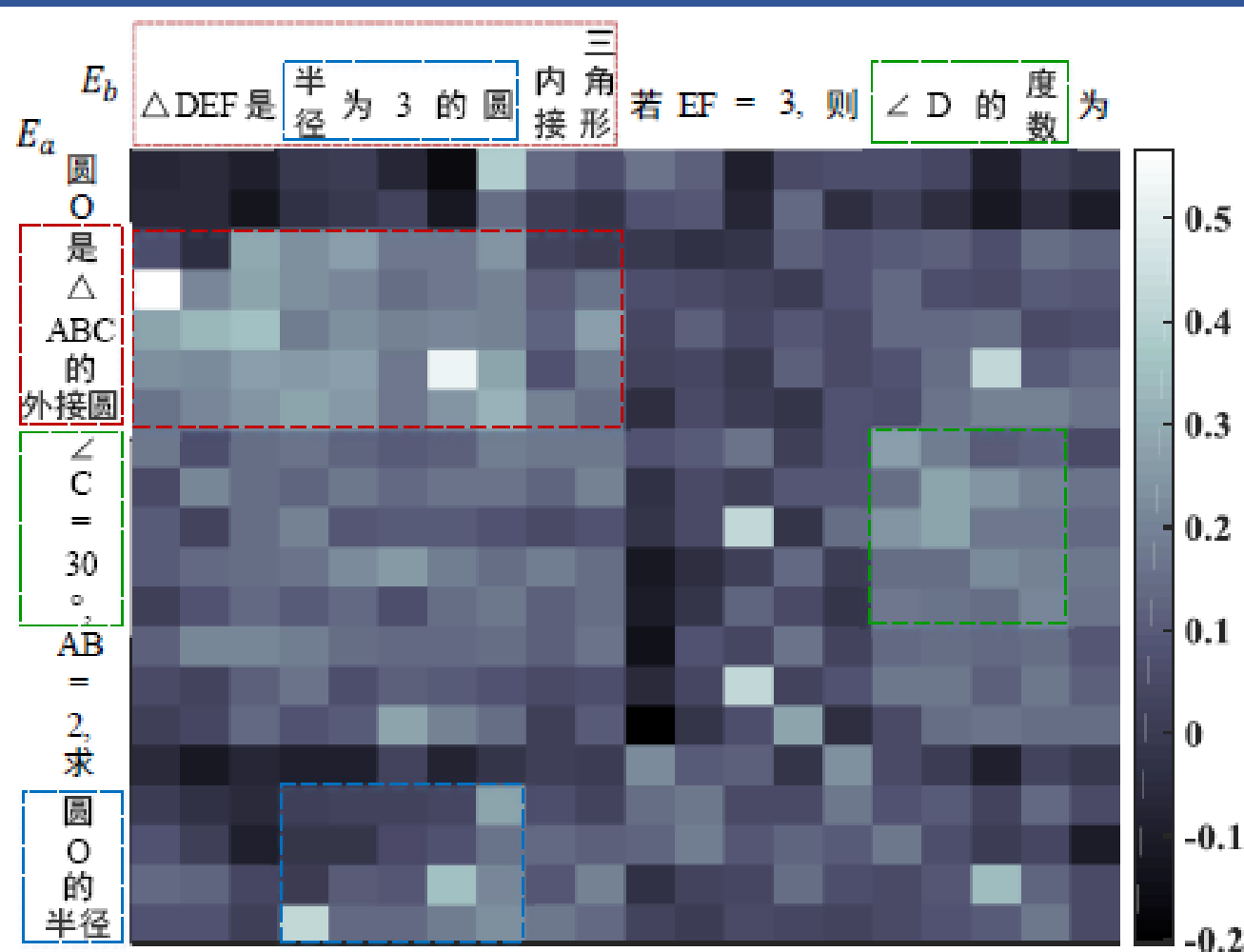
- MANN trained in the sampling way of **Concept** performs **much better** than that in **Random**.
- MANN can focus on the **subtle differences** between its similar pairs and dissimilar ones in **Concept**, because for each given exercise, its similar exercises are close to the dissimilar ones in **Concept**, while they are very different from most sampled dissimilar ones in **Random**

# Experiments

## Case Study

### MANN explanatory power

- The parts in the green box (or blue, red box) in  $E_a$  and  $E_b$  are the similar parts that express the same meaning.
- This implies that MANN provides a good way to capture the similarity information between exercises by **Similarity Attention**.



$E_a$  The circle O is a circumcircle of the triangle ABC.  $\angle C = 30^\circ$  and  $AB = 2$ . Figure out the radius of The circle O.

$E_b$  The triangle DEF is an inscribed triangle of a circle with a radius of 3. If  $EF = 3$ , the number of degrees of  $\angle D$  is \_\_

Figure 10: Visualization of the similar parts between two example exercises  $E_a$  and  $E_b$ .

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# Conclusion



- Provided a focused study on **finding similar exercises** (FSE) in online education systems.
- Proposed a novel **Multimodal Attention-based Neural Network** (MANN) framework for the FSE task by modeling the heterogeneous materials of exercises semantically.
- Designed an **Attention-based LSTM network** to learn a unified semantic representation of each exercise, where **two attention strategies** were proposed to capture text-image and text-concept associations.
- Designed a **Similarity Attention** to measure similar parts in exercise pairs.
- Experiments on a large-scale real-world dataset clearly demonstrated both the **effectiveness** and **explanatory power** of MANN.

- We would like to measure the relation of exercises in more aspects, e.g. by considering the difficulty of exercises.
- We will also try to develop the semi-supervised or unsupervised learning methods for the FSE task.
- As our MANN is a general framework, we will test its performance on other disciplines (e.g. Physics), and meanwhile, on the similar applications in other domains, such as the measurement of product similarities in e-commerce.



# Thanks!