Adaptive Period Embedding for Representing Oriented Objects in Aerial Images

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Abstract—We propose a novel method for representing oriented objects in aerial images named adaptive period embedding (APE). Although traditional object detection methods represent objects using horizontal bounding boxes, the objects in aerial images are oriented. Calculating the angle of the object is a yet challenging task. Almost all previous object detectors for aerial images directly regress the angle of objects; they use complex rules to calculate the angle, and their performance is limited by the rule design. In contrast, our method is based on the angular periodicity of oriented objects. The angle is represented by two 2-D periodic vectors the periods of which are different, so the vector is continuous as the shape changes. The label generation rule is simpler and more reasonable compared with previous methods. The proposed method is general and can be applied to other oriented objects. Besides, we propose a novel intersection over union (IoU) calculation method for long objects named length-independent IoU (LIIoU). We intercept part of the long side of the target box to get the maximum IoU between the proposed box and intercepted target box. Thereby, some long boxes will have corresponding positive samples. Our method reaches the first place of DOAI2019 competition task1 (oriented object) held in a workshop on detecting objects in aerial images in conjunction with IEEE CVPR 2019.

Index Terms—Aerial images, convolutional neural networks (CNN), deep learning, intersection over union (IoU), oriented object detection.

I. INTRODUCTION

TRADITIONAL object detection methods mainly detect objects with horizontal bounding boxes. However, objects in aerial images are oriented and cannot be effectively represented by horizontal bounding boxes. As shown in Fig. 1, detecting oriented objects with horizontal bounding boxes will contain more background and cannot accurately locate the objects. Besides, overlap calculation based on horizontal bounding box is not accurate for oriented objects, as the overlap between horizontal bounding boxes of two oriented objects may be too large; thus, nonmaximum suppression (NMS) based on horizontal bounding boxes is not suitable for oriented objects. Therefore, representing oriented objects with an oriented bounding box is necessary for object detection in aerial images. However, a regressing oriented bounding box is more challenging than regressing a horizontal bounding box. Four variables can represent a horizontal bounding box, such as \(x, y\) coordinates of top left corner and bottom right corner. However, oriented bounding box representation needs an extra variable \(\theta\) to represent its angle. It is hard to directly regress \(\theta\) because the angle is periodic.

Fig. 1. (Left) Horizontal bounding boxes. (Right) Oriented bounding boxes.
of the center of the bounding box, and \( w \) and \( h \) are the lengths of the sizes of long and short sides, respectively. We do not directly regress \( \theta \). Angle is different from other variables, it has periodicity, and the period of square is 90°, whereas the period of rectangle is 180°. Directly regressing the orientation parameter (\( \theta \)) will lead to ambiguity. For example, a rectangle whose angle is 359°, another one’s angle is 0°. Their vision is quite similar, but the labels are completely different, which is unreasonable. Considering this, \( \theta \) is represented by two 2-D periodic vectors. The proposed method is different from [9], as in our method, the periods of two vectors are 90° and 180°, respectively. Finally, we calculate the angle with these vectors. Our method is versatile and can be applied to other detectors. Besides, we design a novel cascade R-CNN method for long objects such as harbors. Generally, a two-stage model proposes bounding boxes with RPN in the first stage, and the output bounding boxes of the second stage (R-CNN) are limited by RPN results. Due to the limited size of the receptive field, some long objects cannot be covered by RPN. With this in mind, we adopt a two-stage cascade R-CNN model with length-independent intersection over union (IoU) (LIIoU) to detect long objects. In the first stage, some bounding boxes which only cover part of the objects are also set to positive samples. In this way, the first R-CNN can propose longer bounding boxes. The main contributions of our article are summarized as follows.

1) We present a novel method for representing oriented bounding boxes in aerial images. We do not directly regress \( \theta \) of oriented bounding boxes, but instead embed \( \theta \) with vectors whose periods are different. In this way, we do not need complex rules to label the angle which avoids ambiguity.

2) We present a novel IoU calculation method named LIIoU, which is designed for long objects. The presented method makes the detector more robust to long objects.

3) The presented method achieves state of the art on DOTA and wins the first place of Challenge-2019 on Object Detection in Aerial Images task1 (oriented task) in conjunction with IEEE CVPR 2019.

II. RELATED WORK

A. Horizontal Objects Detection

Labels of traditional object detection tasks are horizontal bounding boxes. Ren et al. [10] presented a real-time object detection method based on RPN that shares feature maps of RPN and R-CNN and uses anchors with different sizes and aspect ratios in the RPN stage. Though Faster R-CNN shares feature maps, it still requires much computation in the fully connected (FC) layer of R-CNN. Region-based fully convolutional networks (R-FCNs) [11] present position-sensitive score maps and position-sensitive RoI pooling for saving computation in the R-CNN stage. Scale variation is always a very challenging issue in object detection; to help solve this problem, Lin et al. [12] presented feature pyramid networks (FPNs). The FPN generates feature maps of different scales on different layers and detects large objects on higher layers but detects small objects on lower layers; the parameters of an RPN is shared over layers. Based on the FPN, mask R-CNN [7] presents RoIAlign which calculates values in RoI features via bilinear interpolation instead of maximum pooling to avoid quantization errors and adds several convolution layers on the mask-head to generate instant segmentation maps. Liu et al. [13] improved the mask R-CNN by adding bottom-up path augmentation and feature fusion.

Two-stage methods require more computation than one-stage methods, so one-stage methods are more suitable for real-time object detection tasks. Single shot multibox detector (SSD) [14] generates multiple layers and then detects objects with different sizes on different layers. Deconvolutional single shot detector (DSSD) [15] upsamples feature maps and detects small objects on lower layers which improves SSD performance for small objects. Lin et al. [16] presents focal loss to handle the imbalance between positive and negative samples. Although anchors are widely used in object detection, many models adopt the anchor-free method. Huang et al. [17] did not use anchors in RPN, but used a shrunk segmentation map as the label. Redmon et al. [18] also used segmentation maps as ground truth. The GA-RPN [19] combines anchor-free and anchor-based ideas: the label for the first step is generated by a shrunk segmentation map, and the label for the second step is calculated based on the output anchor of the first step.

Traditional object detection in aerial images only focuses on the horizontal bounding box. Yang et al. [20] focused on detecting small urban elements in mobile mapping system (MMS) images. Leng et al. [21] tried to detect ship in single-channel synthetic aperture radar (SAR) imagery with complex signal kurtosis. Li et al. [22] presented local-contextual feature fusion network which is designed for remote sensing images. Its RPN includes multiangle, multiscale, and multiaspect-ratio anchors which can deal with oriented objects, but the final output bounding boxes are still horizontal. Wang et al. [23] presented a rotation-invariant matrix (RIM) which can get both the angular spatial information and radial spatial information. Long et al. [24] presented an automatic and accurate localization method for detecting objects in high-resolution remote sensing images based on Faster R-CNN. Salberg [25] presented a method to detect seals in aerial remote sensing images based on a convolutional network. Chen et al. [26] presented a hybrid DNN (HDNN), the last convolutional and max-pooling layers of DNN of which are divided into multiple blocks, so HDNN can generate multiscale features that improve the detector performance for small objects. Unlike the images used for general object detection, aerial images have higher resolutions. However, large models cannot be implemented due to memory limitations. Therefore, Pang et al. [27] proposed a self-reinforced network named remote sensing region-based CNN (R2-CNN) including Tiny-Net and intermediate global attention blocks. It adopts a lightweight residual structure, so the network can feedforward high-resolution sensing images at high speeds. Deng et al. [28] proposed a novel method for ship detection in SAR images. It redesigns the network structure, does not pretrain on ImageNet, and specifically designs the system for small objects such as ships.
B. Oriented Objects Detection

Oriented object detection is first presented in the field of text detection. Liao et al. [29] presented a novel SSD-based text detection method, which adapts the size and aspect ratio of the anchor and uses $1 \times 1$ convolutional filters for long text lines. Textboxes++ [2] are based on textboxes but directly regress the eight vertices of the oriented bounding box. Liu and Jin [30] designed rules for calculating the order of the vertices of the oriented bounding box and proposed parallel IoU computation to save time. Ma et al. [3] presented rotation RPNs (RRPNs) that proposed oriented bounding boxes in the RPN stage and used rotation region-of-interest (RROI) pooling layer in the R-CNN stage. The aspect ratio of text lines varies greatly, and limited anchors cannot cover the size or aspect ratio of all objects; thus, many methods are anchor-free. Both [1] and [4] generate labels with shrunk segmentation maps and regress the vertices or angles of the bounding box on positive pixels. Lyu et al. [31] generated a corner map and a position-sensitive segmentation map, calculated oriented bounding boxes based on the corner map, and computed the score for each bounding box using the position-sensitive segmentation map. Zhong et al. [32] presented anchor-free RPN (AF-RPN) based on Faster R-CNN with the same design as the FPN [12] and the label is calculated from the shrunk segmentation map instead of the anchors. Zhang et al. [33] proposed an arbitrary-oriented ship detection method for ship detection from remote sensing images. Yang et al. [34], [35] proposed arbitrarily oriented ship detection methods based on CNN.

Horizontal bounding boxes cannot closely surround the objects in aerial images, so the academic community begins to pay attention to oriented bounding box detection in aerial images. Xia et al. [36] labeled a large-scale data set which contains 15 categories and 188 282 instances, each labeled with an arbitrary quadrilateral (eight vertices). A novel detector which directly regresses eight vertices based on Faster R-CNN is also presented. ICPR ODAI [37] and CVPR DOTA [38] competitions are organized based on this data set. Ding et al. [5] presented a two-stage R-CNN method with RoI transformer, which, in the first step, proposed horizontal bounding boxes. The first R-CNN outputs oriented bounding boxes, and the inputs of the second R-CNN are oriented bounding boxes. Li et al. [39] proposed a novel method named rotatable region-based residual network (R3-Net) which can detect multi-oriented vehicles in aerial images and videos. The rotatable RPN (R-RPN) is adopted to generate rotatable regions of interest (R-RoIs) which crops rotated rectangle areas from feature maps.

III. Method

A. Deep Learning-Based Object Detection

In recent years, deep learning-based object detection methods are widely used. In this article, our method is based on Faster R-CNN [10] including RPN and R-CNN. Its process is as follows:

1) Using a CNN such as VGG [40] or ResNet [41] to extract features of the picture. Then each pixel of features predicts whether there is a target near the current point and coordinates of the target. Finally, the network gets $N$ candidate boxes. This process is called RPN. In the RPN stage, traditional method directly predicts $\theta$, but our adaptive period embedding (APE) replaces $\theta$ with $(u_1, u_2)$. In this way, the label is more reasonable and there is no ambiguity in APE. The APE can be used in regressing methods such as RPN, YOLO, and SSD.

2) The $N$ candidate boxes in the RPN stage are not accurate. Therefore, the network will classify and regress these boxes again with more powerful features. R-CNN is used in this stage to extract the features of the entire object. In the R-CNN stage, we use LIIoU for long objects, LIIoU is useful in these data sets which have many long objects. LIIoU can be used in cascade R-CNN, it can set more bounding boxes to positive ones in the R-CNN stage for long objects by replacing the IoU calculation method with LIIoU. In this way, the bounding boxes of long objects will be more accurate.

B. Overview

The overall pipeline of our proposed method is shown in Fig. 2. Recently, anchor-free methods [17]–[19], [32] are widely used in object detection. In this article, we also use AF-RPN. In particular, the label of RPN is not calculated based on the overlap between the anchor and ground truth; instead, the label is generated from the shrunk segmentation map of the oriented bounding box. Unlike traditional object detection tasks, the output bounding box of RPN is oriented, so a novel angle embedding method is adopted to better represent oriented bounding boxes. Segmentation maps with eight channels ($x$, $y$, $w$, $h$, angle embedding) are generated in the RPN stage. Then our model proposes oriented bounding boxes with rotated RoIAAlign in the R-CNN stage, where a cascade R-CNN is used. In the first R-CNN, a novel IoU calculation method named LIIoU is adopted. To make IoU independent of the length of the target box, we intercept part of the long side of the target box to obtain the maximum IoU between the proposed box and intercepted target box. In this way, some long boxes will also have corresponding positive samples. In the second R-CNN, the traditional IoU calculation method is used. The backbone of our network is based on the FPN [12], and we augment the network in the same way as path aggregation network (PANet) [13] by adopting bottom-up path augmentation and feature fusion. Next, we will introduce each component in detail.

C. Network Design

Inspired by recent object detection works [7], [12], [13], we use FPNs as our backbone. FPN generates multiple feature maps of different sizes and detects objects of different sizes on different layers. The FPN is robust to scale variation, especially for small objects, which is suitable for this task. Besides scale variation, aspect ratio variation is another challenging problem. Most traditional object detection methods use anchors of different sizes and aspect ratios to calculate
Fig. 2. Illustration of our proposed architecture. (From left to right) AF-RPN, cascade R-CNN. Yellow bounding box is ground truth, red bounding box is proposed box.

labels in the RPN stage. Thus, we have to manually set the hyperparameters of the anchors which is quite troublesome; moreover, when the aspect ratio of objects varies greatly, limited anchors cannot cover all the objects. The performance of these detectors highly relies on anchor design. Recently, many methods [1], [4], [17]–[19], [32] adopt the anchor-free strategy. In this article, we also adopt the anchor-free method and generate the label of RPN from the shrunk segmentation map. Different layers extract different features, and the detector can achieve better performance by combining these features [13]. In the R-CNN stage, we fuse features of different layers after the first FC layer with max pooling.

D. Anchor-Free Label Generation

The RPN is adopted to propose candidate bounding boxes. Most of the previous methods are based on anchors in this stage. Considering the huge difference in aspect ratio of objects, we use AF-RPN. The shrunk segmentation label is shown in Fig. 3. The shrinking method is the same as EAST [4]. In particular, \( r_1 \) is set to 0.1 and \( r_2 \) is set to 0.25. We shrink the oriented bounding box with \( r_2 \) ratio and set the pixels in the shrunk bounding box to positive samples (blue area). Next, we shrink the oriented bounding box with \( r_1 \) ratio, set the pixels in this shrunk bounding box but not in blue area to “do not care” (purple area), and set the loss weight of these pixels to 0. The FPN outputs multiscale feature maps, and we detect objects of different scales on different layers. We assign a target object the shorter side of which is \( h \) to the level \( pk \), and \( k \) is calculated as follows:

\[
k = \left\lfloor k_0 + \log_2 \left( \frac{h}{128} \right) \right\rfloor \tag{1}
\]

where \( k \) is the layer that objects should be assigned to; \( k_0 \) is the target layer when the height \( h \) of the object is greater than 128 and less than 256, which we set to 4. The height and width are among \([0, +\infty]\), log scale transformations can turn this interval into \([-\infty, +\infty]\). The outputting of network without activation is among \([-\infty, +\infty]\). Objects of different scales share the regression and classification parameters of RPN, so the regression targets should be normalized. An oriented bounding box is labeled as

\[
(x_c, y_c, w, h, \theta)
\]

where \((x_c, y_c)\) are the coordinates of the center point, \(w\) and \(h\) are the lengths of the long side and short side, respectively, and \(\theta\) is the angle of the long side. The pixel on the \(k\)th layer is labeled as \(x_k, y_k\). First, we normalize the target bounding box with the stride of the \(k\)th layer

\[
x'_c = \frac{x_c}{s_k}, \quad y'_c = \frac{y_c}{s_k}, \quad w' = \frac{w}{s_k}, \quad h' = \frac{h}{s_k}, \quad \theta' = \theta \tag{3}
\]

Fig. 3. Shrink segmentation label of anchor-free method. Purple area is the ignored area which is shrunk with \( r_1 \) ratio, blue area is the positive area which is shrunk with \( r_2 \) ratio.
where \( s_k \) is the stride of the \( k \)th layer calculated as
\[
s_k = 2 \times 2^k. \tag{4}\]

The regression targets are calculated as follows:
\[
t_x = \frac{x'_c - x_k}{N}, \quad t_y = \frac{y'_c - y_k}{N},
\]
\[
t_w = \log \frac{w'}{N}, \quad t_h = \log \frac{h'}{N} \tag{5}\]

where \( N \) is a constant and is set to 6 as default.

### E. Adaptive Period Embedding

A horizontal bounding box can be easily represented by four variables \((x, y, w, h)\). But we need an extra variable \( \theta \) to represent an oriented bounding box. The primary challenge of oriented bounding box detection is to regress the angle of objects. The property of \( \theta \) is different from other variables, such as \((x, y, w, h)\), as \( \theta \) is a periodic variable. As shown in Fig. 4, if the length and width of the rectangle are equal, the rectangle is a square, and the period of \( \theta \) is 90°. Otherwise, the period of \( \theta \) is 180°. In neural networks, the periodicity cannot be represented by one variable. Though [9], [42], [43] all use 2-D periodic vector \((\cos \theta, \sin \theta)\) for representing the angle, they do not adapt the period of vector. The proposed APE uses two 2-D vectors to represent the angle. The first vector has a period of 90° and can be formulated as
\[
\mathbf{u}_1 = (\cos 4\theta, \sin 4\theta) \tag{6}\]

where \( \theta \) is the angle of long side of the rectangle. The period of the second vector is 180°. It is calculated as follows:
\[
\mathbf{v} = (\cos 2\theta, \sin 2\theta) \tag{7}\]
\[
\mathbf{u}_2 = \mathbf{v} \times \min (\frac{w - h}{\lambda h}, 1) \tag{8}\]

where \( \lambda \) is set to 0.5, \( w \) is the long side of the rectangle, and \( h \) is the short side. Each component of \( \mathbf{u}_1, \mathbf{u}_2 \) is in \([-1, 1]\), so we use sigmoid as activation, and then multiply them by 2 and subtract 1. Smooth \( L1 \) loss [44] is used in all regression tasks of this article which can be formulated as
\[
\text{smooth}_L (z, z^*) = \begin{cases} 
0.5 (z - z^*)^2, & \text{if } |z - z^*| < 1 \\
|z - z^*| - 0.5, & \text{otherwise}.
\end{cases} \tag{9}\]

The final outputs of the neural network are \((x, y, w, h, \mathbf{u}_1, \mathbf{u}_2)\). Next, we calculate the angle of long side of the rectangle based on \((\mathbf{u}_1, \mathbf{u}_2)\). First, \( \theta_{90^\circ} \) the period of which is 90° and can be calculated as
\[
\theta_{90^\circ} = \frac{\text{atan2}(\mathbf{u}_1)}{4} \tag{10}\]

where \text{atan2} function calculates one unique arctangent value from a 2-D vector. The \( \theta \) of rectangle’s long side may be \( \theta_{90^\circ} \) or \( \theta_{90^\circ} + 90^\circ \). The \( \theta_{180^\circ} \) the period of which is 180° can be calculated as
\[
\theta_{180^\circ} = \frac{\text{atan2}(\mathbf{u}_2)}{2}. \tag{11}\]

Then we calculate the distance between \( \theta_{90^\circ} \) and \( \theta_{180^\circ} \)
\[
\text{dis} = |(2\theta_{90^\circ} - 2\theta_{180^\circ} + 180^\circ) \mod 360^\circ - 180^\circ|. \tag{12}\]

Therefore, the final \( \theta \) is calculated as
\[
\theta = \begin{cases} 
\theta_{90^\circ}, & \text{dis} < 90^\circ \\
\theta_{90^\circ} + 90^\circ, & \text{otherwise}.
\end{cases} \tag{13}\]

If they are all squares (the gap between long and short sides is zero), only using \( \mathbf{u}_1 \) can represent its angle. If they are all rectangles (the gap between long and short sides is large), only using \( \mathbf{u}_2 \) can represent its angle. But in DOTA, the gap between long and short sides may be large or zero. So, both of them are needed. \( \theta_{90^\circ} \) encodes angles into vectors with a 90° period and \( \theta_{180^\circ} \) encodes angles into vectors with a 180° period. The angle calculated by \( \theta_{90^\circ} \) may be the angle of the long or short side. When the sizes of long and short sides are equal, there is no additional information required. But if long and short sides are not equal, other information to represent the angle of the long side is needed. \( \mathbf{u}_2 = \mathbf{v} \times \min ((w - h)/\lambda h, 1) \) which means the angle of long side. We do not directly regress \( \mathbf{v} \) because there is ambiguity for \( \mathbf{v} \). For example, when height and width are equal, the angle of the long side is ambiguous, the \( \mathbf{v} \) will produce mutation. But \( \mathbf{u}_2 \) continuously changes as long or short sides change. When the sizes of long and short sides are equal, \( \mathbf{u}_2 \) is zero, the changing is also continuous. We use sigmoid as activation, accordingly, we set the maximum of \( \theta_{90^\circ} \) to 1. The distance between \( \theta_{90^\circ} \) and \( \theta_{180^\circ} \) is \( \text{dis} = |(2\theta_{90^\circ} - 2\theta_{180^\circ} + 180^\circ) \mod 360^\circ - 180^\circ| \). \( \theta_{90^\circ} \) maybe the angle of the long or short side, the final angle of the long side may be \( \theta_{90^\circ} \) or \( \theta_{90^\circ} + 90^\circ \). We find the closer angle among \( \theta_{90^\circ}, \theta_{90^\circ} + 90^\circ \), and \( \theta_{180^\circ} \). The distance between \( \theta_{90^\circ} \) and \( \theta_{180^\circ} \) is the distance of two periodic vectors which is the closer rotated angle from \( \theta_{90^\circ} \) to \( \theta_{180^\circ} \) clockwise or counterclockwise.

### F. Length-Independent IoU

IoU is the evaluation protocol of object detection; the more accurate the regression, the better the performance. But the receptive field of a neural network is limited and thus cannot cover some long objects. The detector proposes candidate

![Fig. 4. Period of oriented bounding box. (Top) Rectangle the period of which is 180°. (Bottom) Square the period of which is 90°. (The four sides of each bounding box are in different colors for better visualization.)](image)
bounding boxes in the RPN stage and then classifies and regresses these boxes again. The result of R-CNN highly relies on the output bounding boxes of the RPN. In the R-CNN stage, only the proposed bounding boxes whose IoU is higher than 0.5 is set to positive samples. Some target objects that are not well regressed in the RPN cannot be detected in the R-CNN. One idea is multiple regression [45] in the R-CNN stage, only the proposed bounding boxes whose IoU is higher than 0.5 is set to positive samples. Some target objects that are not well regressed in the RPN cannot be detected in the R-CNN. One idea is multiple regression [45] in the R-CNN stage, only the proposed bounding boxes whose IoU is higher than 0.5 is set to positive samples. Some target objects that are not well regressed in the RPN cannot be detected in the R-CNN.

As shown in Fig. 2, two R-CNNs are used after RPN. In the first R-CNN, we set more bounding boxes to the positive center of a rotated RoIAlign is then calculated as the score of the box with poor quality and the evaluation is lower, bounding boxes in the RPN stage and then classifies and regresses these boxes again. The result of R-CNN highly relies on the output bounding boxes of the RPN. In the R-CNN stage, only the proposed bounding boxes whose IoU is higher than 0.5 is set to positive samples. Some target objects that are not well regressed in the RPN cannot be detected in the R-CNN.

In this way, we propose a novel IoU calculation method named LIIoU.

**Algorithm 1 LIIoU Calculation**

**Input:** pbbox($x^p$, $y^p$, $w^p$, $h^p$, $\theta^p$), gbbox($x^g$, $y^g$, $w^g$, $h^g$, $\theta^g$)

**Output:** LIIoU

```
1: if $w^p \geq w^g$ then
2: $x^g = x^p$; $y^g = y^p$; $w^g = w^p$; $h^g = h^p$; $\theta^g = \theta^g$
3: else
4: $A_1 = x^g - \cos(\theta^g) \times \frac{w^g}{2}$
5: $A_2 = y^g - \sin(\theta^g) \times \frac{w^g}{2}$
6: $B_1 = x^g + \cos(\theta^g) \times \frac{w^g}{2}$
7: $B_2 = y^g + \sin(\theta^g) \times \frac{w^g}{2}$
8: $C_1 = x^p$; $C_2 = y^p$
9: $z = \frac{(C_1 - A_1)(B_2 - A_2)}{||B_2 - A_1||}$
10: $w_1 = z - \frac{w^g}{2}$; $w_2 = z + \frac{w^g}{2}$
11: if $w_1 < 0$ then
12: $w_1 = 0$; $w_2 = w^p$
13: else if $w_2 \geq w^g$ then
14: $w_2 = w^g$; $w_1 = w^p - w^g$
15: end if
16: $x^g = A_1 + \cos(\theta) \times \frac{w_2 + w_1}{2}$; $y^g = A_2 + \sin(\theta) \times \frac{w_2 + w_1}{2}$
17: $w^g = w_2 - w_1$; $h^g = h^p$; $\theta^g = \theta^p$
18: end if
19: calculate overlaps between $(x^p, y^p, w^p, h^p, \theta^p)$ and $(x^g, y^g, w^g, h^g, \theta^g)$
```

are both rotated, cascade R-CNN is adopted for improving the model’s performance on long objects.

Rotated RoIAlign is adopted, so the ground truth is calculated in a rotated coordinate system. Following [8], if the center of a rotated RoIAlign is $(x^r, y^r)$ and the angle is $\theta^p$, the affine transformation can be represented by an affine matrix

$$ M = \begin{bmatrix} 1 & 0 & x^p \\ 0 & 1 & y^p \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \theta^p & \sin \theta^p & 0 \\ -\sin \theta^p & \cos \theta^p & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos \theta^p & \sin \theta^p & (1-\cos \theta^p)x^p - y^p * \sin \theta^p \\ -\sin \theta^p & \cos \theta^p & (1-\cos \theta^p)y^p + x^p * \sin \theta^p \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \Rightarrow \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = M \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}. $$(14)

Fig. 5. Details of LIIoU calculation, green bounding box is proposed bounding box, orange bounding box is target box.

G. Cascade R-CNN

As shown in Fig. 2, two R-CNNs are used after RPN. In the first R-CNN, we only refine the center, height, and width of the oriented bounding box without regressing the vertices of the target box. This is because the output of the first R-CNN is the input of the second R-CNN, and rotated RoIAlign can only handle oriented rectangle but not quadrangle. In the second R-CNN, we regress the vertices of the target box. Our method is different from rotated cascade R-CNN [8], we directly regress oriented bounding boxes in the RPN. The two R-CNNs...
We set the coordinate system to rotated coordinate system with (14) and (15). The final ground truth in the rotated coordinate system is \((x, y, (x', y'))\) and \((x, y)\) is the coordinates in the original coordinate system. In the first R-CNN, the regression targets are \(r_{c_{m1}}, r_{c_{1}}, r_{h_{m1}}, r_{h_{1}}\) which can be formulated as

\[
\begin{align*}
r_{c_{m1}} &= \frac{x_c - x_p}{w_p}; & r_{c_{1}} &= \frac{y_c - y_p}{h_p} \\
r_{h_{m1}} &= \log \left( \frac{w}{w_p} \right); & r_{h_{1}} &= \log \left( \frac{h}{h_p} \right).
\end{align*}
\]

(16)

In the second R-CNN, the regression targets are \(r_{c_{m2}}, r_{c_{1}}, i = 1, 2, 3, 4\) which can be formulated as

\[
\begin{align*}
r_{c_{m2}} &= \frac{x_c - x_p}{w_p}; & r_{c_{1}} &= \frac{y_i - y_p}{h_p}, & i = 1, 2, 3, 4
\end{align*}
\]

(18)

where \((x_c, y_c, w, h)\) are the center, width, and height of the ground truth, \((x_i, y_i)\) is the vertex of the ground truth bounding box, and \((x_p, y_p, w_p, h_p)\) are the center, width, and height of the proposed bounding box.

IV. EXPERIMENT

A. Data Sets

DOTA [36] is a large data set that contains 2806 aerial images from different sensors and platforms. The size of the image varies greatly, ranging from about 800 \(\times\) 800 to 4000 \(\times\) 4000 pixels, so it is necessary to crop the images and detect the objects in the cropped images. As the instances in aerial images, such as cars, ships, and bridges, are oriented, each instance is labeled by an arbitrary (eight d.o.f.) quadrilateral. For the oriented object detection task, the output bounding boxes are quadrilateral to evaluate the performance of our detector on the quadrilateral, we use the evaluation system provided along with this data set. There are two versions of the DOTA data set, DOTA-v1.0 and DOTA-v1.5; DOTA-v1.5 fixes some errors and is provided for DOAI2019 competition [38]. We use DOTA-v1.5 for this competition, but in the following experiments, we use DOTA-v1.0 for a fair comparison.

B. Implementation Details

The backbone of our detector is ResNet-50 [41] pretrained on ImageNet [47]. The number of FPN channels is set to 256. In the R-CNN stage, two FC layers are used, the channel of which is set to 1024. Feature fusion is applied after the first FC layer along with maxpooling. Batchnorm is not used in this article. Our network is trained with SGD, where the batch size of images is 1 and the initial learning rate is set to 0.00125, model is trained with about 161790 iterations, learning rate is then divided by 10 at 2/3 and 8/9 of the entire training. Weight decay is set to 0.0001. Due to the limited memory, we crop images to 1024 \(\times\) 1024 with the stride of 256 for training and testing. We merge all predicted bounding boxes with DOTA’s code\(^1\) in testing. The model is trained and tested on a single scale. Data augmentation is used for better performance; in particular, we randomly rotate images with angle among \(0, \pi/2, \pi, \) and \(3\pi/2\), and class balance resampling is adopted to solve class imbalance problem. In default, we train our model with the training set and evaluate it on the validation set and testing set.

C. Ablation Study

In order to evaluate the effect of each component, we conduct ablation experiments on the validation set of DOTA. The model is not modified except for the component being tested.

1) Effect of APE: We need to propose oriented bounding boxes in the RPN stage, but it is challenging to effectively represent an oriented bounding box. Most of the previous methods [3]–[5] that directly regress the angle do not notice the periodicity of the angle. When the angle is too diverse, the performance of the system will drop significantly. To evaluate whether the proposed APE can well handle the diversity of the angles, we conduct ablation experiments: one model directly regresses the angle of the long side of the target box, whereas the other regresses APE vectors. We evaluate the quality of the proposed oriented bounding box in the RPN stage. The network only classifies objects into two classes (positive sample and negative sample) in the RPN stage. We use average precision (AP) as our evaluation protocol. AP is average precision which calculates the AP at different recall rates, it is widely used in object detection evaluation. And mAP is the mean of AP on all classes. As shown in Table I, RPN achieves much better performance with APE. We show the comparison in Fig. 6, where we can see that RPN outputs a more accurate angle with APE compared with directly regressing the angle.

2) LIIoU Versus IoU: To evaluate the efficiency of LIIoU, we conduct a control experiment. Faster R-CNN means there is only one R-CNN. When Cascade R-CNN is adopted, two R-CNNs are used. In the first model, we calculate the overlap between oriented bounding boxes with traditional IoU in both two R-CNNs. In the second model, the overlap between oriented bounding boxes is calculated with LIIoU in the first R-CNN and with traditional IoU in the last R-CNN, and the threshold is set to 0.5. Results are shown in Table II, where we can see that Cascade R-CNN gains much better performance with LIIoU. We show their comparison in Fig. 7, where we can find that LIIoU can improve the quality of the proposed bounding boxes and the recall rate. Regardless of the aspect

\(^1\)https://github.com/CAPTAIN-WHU/DOTA_devkit
ratio and size, nearly every object has positive samples with L1IoU, so the detector can handle objects with large aspect ratios and lengths well.

### D. Comparing With Other State-of-the-Art Methods

We compare our method with other state-of-the-art methods. The results are shown in Table III, results of RRPN, R2CNN, R-DFPN, and Yang et al. [34] are from [5]. Our model is trained and tested with the single-scale setting. When our model is only trained with the training set ex validation set, our method significantly outperforms other methods, and if the validation set is also used for training, our model achieves better performance. The detection results are shown in Fig. 8. The angle, size, aspect ratio of objects in aerial images vary greatly, but our proposed method can well handle these challenging conditions. Our model is also efficient that can handle four images whose resolution is 1024/sec.

### E. Limitations

We show some failure cases of our method in Fig. 9. When the boundary line of the court is not obvious, our method cannot predict accurate bounding boxes. When the scale of the object is too small, the detector misses these objects. When the shape of the objects is quite special and the shape does not exist in the training set, our method will produce the wrong results.
TABLE IV

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<tr>
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<th>USTC-NEUSLP</th>
<th>pca_lab</th>
<th>czh</th>
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Fig. 7. Comparison of LIIoU and IoU. (From left to right) Calculate overlaps with IoU in the first R-CNN, calculate overlaps with LIIoU in the first R-CNN (overlaps are both calculated with IoU in the last R-CNN).

results. In the future, we will explore a solution for these hard cases.

F. DOAI2019 Competition

DOAI2019 competition [38] is held in the workshop on detecting objects in aerial images in conjunction with IEEE CVPR 2019. The competition is more difficult and requires detecting all objects including samples labeled as difficult. Based on our proposed methods including APE and LIIoU, we adopt class balance resampling, image rotation, multi-scale training and testing and model assembling for better performance. Three models are used whose backbone is ResNeXt-101(32 × 4) [49]. Finally, we combine the training set with the validation set for training. The results of the competition are shown in Table IV. Our method wins the first place on the oriented task, with a gain of about 1.7% over the most competing competitor.

V. CONCLUSION AND FUTURE WORK

Detecting oriented objects in aerial images is a challenging task. In this article, we make full use of the periodicity of the angle. A novel method named APE is proposed which can well-regress oriented bounding boxes in aerial images. The vector with the adaptive period can learn the periodicity of the angle, which cannot be implemented with the 1-D vector. The proposed method can be applied to both one-stage methods such as RPN and two-stage methods, and we believe other detectors can also directly adopt the APE module. Besides, we propose a novel LIIoU. LIIoU sets more proposed bounding boxes to positive samples especially for long objects which can improve the quality of R-CNN regression. Our ablation study proves that each proposed module is effective. Based on our method, we won the first place on the oriented task of DOAI2019. In the future, we will explore a more efficient and accurate detector for detecting oriented objects in aerial images.
REFERENCES


ZHU et al.: APE FOR REPRESENTING ORIENTED OBJECTS IN AERIAL IMAGES


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