Homework 10:

Problem 10.1: If

$$\|f\mathrm{d}\sigma\|_{L^{p'}(\mathbb{R}^n)} \lesssim \|f\|_{L^{q'}(S^{n-1})}$$

holds for all  $f \in L^{q'}(S^{n-1})$ , then

$$q \le \frac{n-1}{n+1}p'.$$

Problem 10.2: Suppose that S is a bounded subset of a hyperplane in  $\mathbb{R}^n$ . Prove that if  $\|\hat{f}\|_S\|_{L^1(S)} \leq C \|f\|_{L^p(\mathbb{R}^n)}$  for all  $f \in \mathcal{S}(\mathbb{R}^n)$  then necessarily p = 1, in other words, there cannot be a nontrivial restriction theorem for flat (affine) surfaces.