Homework 7, Spring 2023:

Problem 7.1: (Muscalu, Schlag, *Classical and Multilinear Harmonic Analysis*, Vol 1, Section 8.2, Corollary 8.4 (i), P.202-203)

In their proof of Corollary 8.4 (i), they write

$$S(f_k - f)(x) \le \liminf_{m \to \infty} S(f_k - f_m)(x).$$

Please provide a proof of this inequality.

Problem 7.2: (Khinchin's inequality) In its proof, one can first prove the following version with real coefficients a_n ,

$$E\left(\left|\sum_{n=1}^{N} a_n w_n\right|^p\right)^{1/p} \asymp \left(\sum_{n=1}^{N} |a_n|^2\right)^{1/2}$$

for $1 . Assuming the above inequality, one can then extend it to a version with complex coefficients <math>a_n$. Please explain how to extend it to complex coefficients.