

number of PTS groups, and 2) it possesses faster decoding convergence and lower decoder complexity. With the improved performance, better PAPR performance can be supported.

As future work, the following two aspects could be considered to further improve the decoding performance: 1) Try other optimization objectives, such as reducing the number of short-length cycles; and 2) design better algorithms so that the degrees of phase nodes are further reduced, particularly for large  $U$ .

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## Generalized Interrelay Interference Cancellation for Two-Path Successive Relaying Systems

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**Abstract**—This paper proposes a generalized interrelay interference cancellation (gIRIC) scheme for a two-path relay model in multisource systems. Both the sources and the relay adopt complex field network coding (CFNC) to remove the interrelay interference (IRI) caused by the two-path relay. Furthermore, we introduce two detecting modes (gIRIC-noSD and gIRIC-SD) for destination in our scheme. Two switching rules are given to select a suitable detecting mode between treating the signal of a direct link as noise (gIRIC-noSD) and utilizing the direct link to assist signal detection (gIRIC-SD). The bounds of average symbol error probability (SEP) and throughput of our scheme are derived.

**Index Terms**—Complex field network coding (CFNC), interrelay interference (IRI), multisource, two-path relay.

#### I. INTRODUCTION

Relay-based cooperative communications serves as a promising technique, which has been studied over the past decade, to extend coverage and combat channel fading in wireless networks [1], [2]. Nevertheless, due to the half-duplex nature of relay nodes, one transmission process often occupies two time slots (TSs) for the relay to receive the signal and then forward it, respectively, which results in spectral inefficiency. To overcome it, a spectrally efficient cooperative schemes named two-path successive relay was proposed in [3] and [4]. As shown in Fig. 1, at each TS, the source ( $S$ ) symbol is sent to one of the relays, and the other relay forwards the symbol received from  $S$  at the previous TS. Therefore, only  $(L + 1)$  TSs are required to transmit  $L$  symbols from  $S$  to  $D$ , leading to an ideal throughput as high as  $L/(L + 1)$  symbols per source per TS (sym/S/TS). However, the two-path relay scheme results in interrelay interference (IRI) due to simultaneous transmissions of the source and the relays, which are marked in Fig. 1. Diverse schemes were proposed in [5]–[8] to deal with the IRI.

However, existing approaches have several common shortcomings. First, they only considered a single-source model. Several approaches introduced in [5]–[8] are based on binary XOR, and the others require a large number of computations. Thus, in consideration of practicability, those approaches cannot be directly extended to multisource systems. Second, most of them did not deeply discuss the effects of a direct link ( $S-D$ ). Due to the broadcast nature of the user terminal, it is necessary to investigate whether the interference caused by the  $S-D$  link should be ignored or be exploited to assist signal detection [9]. Therefore, we are motivated to explore a new scheme for the two-path relay system. In [10], Wang and Giannakis developed complex field

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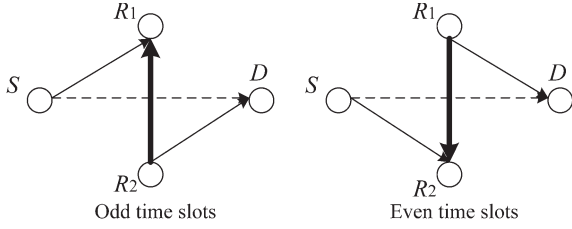


Fig. 1. Two-path relay system model. The black line arrows denote the desired signals and the bold arrows represent the IRI, whereas the dotted lines denote direct links.

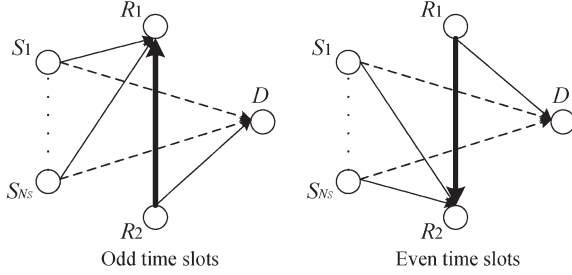


Fig. 2.  $(N_S, 2, 1)$  system model. The black line arrows denote the desired signals and the bold arrows represent the IRI, whereas the dotted lines between  $S_i$  and  $D$  denote direct links.

network coding (CFNC), which allows simultaneous transmissions of multiple sources within the same TS on the same resource blocks. In our previous work [11], we adopted physical-layer network coding [12] to deal with the IRI. Nevertheless, we did not take direct links into consideration.

Thus, in this paper, we propose a new generalized IRI cancellation (gIRIC) scheme with CFNC in the two-path successive relay system. In general, our main contributions are as follows.

- In either one-source or multisource model, we adopt CFNC at sources and relays before transmissions. We design the precoding vectors for sources and relays so that the desired symbols can be separated from the IRI through maximum likelihood (ML) detection at the receiver.
- We introduce two switching strategies for destination to select a suitable detecting mode between treating an  $S$ - $D$  link as noise (gIRIC-noSD) and utilizing a direct link to assist signal detection (gIRIC-SD).

*Notations:*  $(\cdot)^T$  is the transpose,  $(\cdot)^*$  is the conjugation,  $\mathcal{CN}(0, \sigma^2)$  is the circular symmetric complex Gaussian distribution with zero mean and variance  $\sigma^2$ ,  $\hat{x}$  is the estimation of  $x$ , and  $Q(x) = 1/\sqrt{2\pi} \int_x^\infty \exp(-t^2/2) dt$  is the Gaussian tail function.

## II. SYSTEM MODEL

As shown in Fig. 2, this paper considers a two-path relay cooperative system that consists of  $N_S$  sources  $S_1, \dots, S_{N_S}$ , two relays ( $R_1, R_2$ ), and one destination  $D$ . CFNC makes it possible for sources to broadcast symbols within the same TS after symbol-level operations at the physical layer. By deploying CFNC, a cooperative network with  $N_S$  sources achieves an ideal throughput as high as  $1/2$  sym/S/TS [10]. Thus, we introduce CFNC into our system to distinguish source symbols and the IRI. Each source  $S_i$  broadcasts its own modulated symbols  $x_i[k]$ , multiplied by the precoding factor, at TS  $k$  ( $k = 1, \dots, L$ ), where  $L$  is the frame length. Two relay nodes, operating in the half-duplex mode and equipped with a single antenna, take turns to demodulate-and-forward the received symbol to the destination. Assuming slow flat fading, the channel coefficients between  $S_i$  and

$R_m$ ,  $S_i$  and  $D$ ,  $R_1$  and  $R_2$ ,  $R_m$  and  $D$ , which are represented by  $h_{S_i R_m}$ ,  $h_{S_i D}$ ,  $h_{12}$ , and  $h_{R_m D}$  ( $i = 1, 2, \dots, N_S$  and  $m = 1, 2$ ), respectively, are modeled as zero-mean complex Gaussian random variables with finite variances  $\mu_{S_i R_m}$ ,  $\mu_{S_i D}$ ,  $\mu_{12}$ , and  $\mu_{R_m D}$ . A channel coefficient between  $R_1$  and  $R_2$  satisfies channel reciprocity (i.e.,  $h_{12} = h_{21}$ ). All channel coefficients are supposed to remain constant within one frame time and vary independently from frame to frame. Regardless of environmental interference from other nodes in the network, we focus on the IRI at relay and the collisions at  $D$ . The corresponding channel noise  $w_{R_m}$  and  $w_D$  at  $R_m$  and  $D$  are assumed to be additive complex white Gaussian noise with zero mean and variance  $N_0/2$ . For simplicity, we allocate equal transmit power among sources and relays. Let  $\mathbf{x}[k] = [x_1[k], x_2[k], \dots, x_{N_S}[k]]^T$  denote the symbols sent by sources at TS  $k$  and  $\mathbf{x}_r[k] = [\hat{x}_1[k], \hat{x}_2[k], \dots, \hat{x}_{N_S}[k]]^T$  be the estimation of  $\mathbf{x}[k]$  by relay at TS  $k$ .

## III. PROPOSED SCHEME

The core idea of CFNC [10] is to establish a one-to-one mapping between  $\mathbf{x} = [x_1, x_2, \dots, x_N]^T$  and  $\Theta^T \mathbf{x}$ , where  $\Theta^T = [\theta_1, \theta_2, \dots, \theta_N]$ . The design of  $\Theta^T$  is supposed to satisfy  $\Theta^T \mathbf{x} \neq \Theta^T \mathbf{x}'$  if  $\mathbf{x} \neq \mathbf{x}'$ , where  $x'_i$  in  $\mathbf{x}'$  is drawn from the same finite alphabet set as  $x_i$  in  $\mathbf{x}$ . CFNC allows simultaneous transmissions of  $N$  sources (the received symbol is  $y_D = \Theta^T \mathbf{H}_{SD} \mathbf{x} + n_{SD}$ , where  $\mathbf{H}_{SD} = \text{diag}(h_{S_1 D}, \dots, h_{S_{N_S} D})$ ). Then, ML detection (i.e.,  $\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \|y_D - \Theta^T \mathbf{H}_{SD} \mathbf{x}\|^2$ ) is performed at the destination to recover each source's symbol (for details, see [10]). In our system, since the signal forwarded by the relay is the superposition of  $N_S$  estimated symbols from  $N_S$  sources, we model the relay as "virtual"  $N_S$  transmitters. Thus,  $N_S$  sources, together with one of the relays, can be equivalent to a "virtual" ( $2N_S$ -source, 2-destination) transmission model. Therefore, we adopt  $\Theta^T = [\theta_1, \theta_2, \dots, \theta_{2N_S}]$ , the design of which is based on a linear complex field encoder introduced in [10, Sec. III]. Let  $\Theta_{(1)}^T = [\theta_1, \theta_2, \dots, \theta_{N_S}]$  and  $\Theta_{(2)}^T = [\theta_{N_S+1}, \theta_{N_S+2}, \dots, \theta_{2N_S}]$ . Without losing generality, we assume that, at each odd TS, original symbols from sources are multiplied by  $\Theta_{(1)}^T$  and sent to  $R_1$ . Simultaneously,  $R_2$  forwards the previously received symbols, multiplied by  $\Theta_{(2)}^T$ . While at each even TS, original symbols from sources are multiplied by  $\Theta_{(2)}^T$  and sent to  $R_2$ . Simultaneously,  $R_1$  forwards the previously received symbol, multiplied by  $\Theta_{(1)}^T$ .

Our proposed gIRIC scheme consists of two detecting modes: treating the  $S$ - $D$  link as noise and utilizing the direct link to assist signal detection. We will separately detail both of them.

### A. gIRIC for $(N_S, 2, 1)$ Model, Ignoring $S$ - $D$ Link

*Odd TS  $2n - 1$  ( $n = 2, 3, \dots, \lfloor L/2 \rfloor$ ):*  $S_i$  transmits its symbol as  $\theta_i x_i[2n - 1]$ . Simultaneously,  $R_2$  forwards  $\Theta_{(2)}^T \hat{\mathbf{x}}_r[2n - 2]$ , where  $\hat{\mathbf{x}}_r[2n - 2] = [\hat{x}_1[2n - 2], \hat{x}_2[2n - 2], \dots, \hat{x}_{N_S}[2n - 2]]$  are the estimates of the received symbols at the previous TS. Under the assumption that symbol timing and carrier-phase synchronization have been established, the received signals by  $R$  and  $D$  are, respectively, given by

$$y_{R_1}[2n - 1] = \Theta_{(1)}^T \mathbf{H}_{S R_1} \mathbf{x}[2n - 1] + h_{12} \Theta_{(2)}^T \hat{\mathbf{x}}_r[2n - 2] + w_{R_1}[2n - 1] \quad (1)$$

$$y_D[2n - 1] = h_{R_2 D} \Theta_{(2)}^T \hat{\mathbf{x}}_r[2n - 2] + \Theta_{(1)}^T \mathbf{H}_{SD} \mathbf{x}[2n - 1] + w_D[2n - 1] \quad (2)$$

where  $\mathbf{H}_{S R_1} = \text{diag}(h_{S_1 R_1}, h_{S_2 R_1}, \dots, h_{S_{N_S} R_1})$ ,  $\mathbf{H}_{SD} = \text{diag}(h_{S_1 D}, h_{S_2 D}, \dots, h_{S_{N_S} D})$ , and  $w_{R_1}[2n - 1], w_D[2n - 1] \sim \mathcal{CN}(0, N_0/2)$ . We use subscript "r" to denote the symbol from relay nodes. All the symbols ( $x_i[2n - 1], \hat{x}_i[2n - 2]$ ) sent by sources or relays are drawn from a finite alphabet  $\mathcal{A}_x$  with cardinality  $|\mathcal{A}_x|$ , which is determined by the modulation mode.

TABLE I  
DETAILED OPERATIONS OF THE PROPOSED gIRIC FOR THE (2, 2, 1) SYSTEM ( $L$  IS AN EVEN NUMBER). TX: TRANSMIT; RX: RECEIVE

TS	$S_1$ (Tx:)	$S_2$ (Tx:)	$R_1$	$R_2$	$D$ (Rx:)
1	$\theta_1 x_1[1]$	$\theta_2 x_2[1]$	Rx: $\theta_1 x_1[1] + \theta_2 x_2[1]$		$(\theta_1 x_1[1] + \theta_2 x_2[1])$
2	$\theta_3 x_1[2]$	$\theta_4 x_2[2]$	Tx: $\theta_1 x_1[1] + \theta_2 x_2[1]$	Rx: $\theta_1 x_1[1] + \theta_2 x_2[1]$ $+ \theta_3 x_1[2] + \theta_4 x_2[2]$	$\theta_1 x_1[1] + \theta_2 x_2[1] + (\theta_3 x_1[2] + \theta_4 x_2[2])$
3	$\theta_1 x_1[3]$	$\theta_2 x_2[3]$	Rx: $\theta_1 x_1[3] + \theta_2 x_2[3]$ $+ \theta_3 x_1[2] + \theta_4 x_2[2]$	Tx: $\theta_3 x_1[2] + \theta_4 x_2[2]$	$\theta_3 x_1[2] + \theta_4 x_2[2] + (\theta_1 x_1[3] + \theta_2 x_2[3])$
4	$\theta_3 x_1[4]$	$\theta_4 x_2[4]$	Tx: $\theta_1 x_1[3] + \theta_2 x_2[3]$	Rx: $\theta_1 x_1[3] + \theta_2 x_2[3]$ $+ \theta_3 x_1[4] + \theta_4 x_2[4]$	$\theta_1 x_1[3] + \theta_2 x_2[3] + (\theta_3 x_1[4] + \theta_4 x_2[4])$
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$
$L+1$	-	-	-	Tx: $\theta_3 x_1[L] + \theta_4 x_2[L]$	$\theta_3 x_1[L] + \theta_4 x_2[L]$

For  $R_1$ , the second part of  $y_{R_1}[2n-1]$  in (1) (i.e.,  $h_{12}\Theta_{(2)}^T \hat{\mathbf{x}}_r[2n-2]$ ) is the IRI, which precludes the detection of  $\mathbf{x}[2n-1]$ . Owing to CFNC,  $R_1$  is able to extract the desired  $\mathbf{x}[k]$  through the ML detector as follows:

$$(\hat{\mathbf{x}}[2n-1], \hat{\mathbf{x}}_r[2n-2])_{R_1} = \arg \min_{\text{all } x_i, x_{r_i} \in \mathcal{A}_x} \times \left\| y_{R_1}[2n-1] - \Theta_{(1)}^T \mathbf{H}_{SR_1} \mathbf{x} - h_{12} \Theta_{(2)}^T \mathbf{x}_r \right\|^2 \quad (3)$$

where  $x_i$  is the  $i$ th element of  $\mathbf{x}$ , whereas  $x_{r_i}$  corresponds to  $\mathbf{x}_r$ . It is obvious that the IRI is separated from the desired symbols. The symbol for  $R_1$  to forward in the next TS is  $x_r[2n-1] = \Theta_{(1)}^T \hat{\mathbf{x}}[2n-1]$ .

Since  $D$  regards the signal of  $S$ - $D$  link as noise, ML detection is performed at  $D$  as

$$(\hat{\mathbf{x}}_r[2n-2])_D = \arg \min_{\text{all } x_{r_i} \in \mathcal{A}_x} \left\| y_D[2n-1] - h_{R_2 D} \Theta_{(2)}^T \mathbf{x}_r \right\|^2. \quad (4)$$

Since  $\hat{\mathbf{x}}_r[2n-2]$  is the estimation of the received symbol at  $R_2$  at the previous TS (i.e.,  $\mathbf{x}[2n-2]$ ), the original  $(2n-2)$ th symbols of  $N_S$  sources are recovered after two-hop transmissions.

Even TS  $2n$  ( $n = 1, 2, \dots, \lfloor L/2 \rfloor$ ).  $S_i$  transmits its symbol as  $\theta_{i+N_S} x_i[2n]$ . Simultaneously,  $R_1$  forwards  $\Theta_{(1)}^T \hat{\mathbf{x}}_r[2n-1]$ .  $R_2$  and  $D$  receive the signals. Then, the input/output relationships are

$$y_{R_2}[2n] = \Theta_{(2)}^T \mathbf{H}_{SR_2} \mathbf{x}[2n] + h_{12} \Theta_{(1)}^T \hat{\mathbf{x}}_r[2n-1] + w_{R_2}[2n] \quad (5)$$

$$y_D[2n] = h_{R_1 D} \Theta_{(1)}^T \hat{\mathbf{x}}_r[2n-1] + \Theta_{(2)}^T \mathbf{H}_{SD} \mathbf{x}[2n] + w_D[2n]. \quad (6)$$

Similar to what  $R_1$  operates at TS  $2n-1$ ,  $R_2$  can extract  $\mathbf{x}[2n]$  through the ML detector. Still regarding the signal of  $S$ - $D$  link as noise, the original  $(2n-1)$ th symbols of the sources are recovered at  $D$ .

To show clearly the entire procedure, we take a (2, 2, 1) system as an example and summarize the detailed operations of our gIRIC scheme within each TS in Table I, regardless of channel coefficients and noise.  $N_S = 2$  results in  $\Theta^T = [\theta_1, \theta_2, \theta_3, \theta_4]$  and  $\Theta_{(1)}^T = [\theta_1, \theta_2]$ ,  $\Theta_{(2)}^T = [\theta_3, \theta_4]$ . At each odd TS,  $\Theta_{(1)}^T$  is the precoding vector for sources, and  $\Theta_{(2)}^T$  corresponds to the symbol sent by  $R_2$ . While at each even TS, the system operates in the opposite way. Therefore, only  $L+1$  TSs are occupied to finish  $L \times 2$  symbols' transmissions. In addition, by employing CFNC, IRI can be removed at relay nodes.

The items encapsulated in parenthesis in Table I are treated as noise at  $D$ . We further propose an alternative scheme that exploits such parts to assist signal detection.

#### B. gIRIC for ( $N_S, 2, 1$ ) Model, Utilizing $S$ - $D$ Link

Due to simultaneous transmissions of all sources and one of the relays, the two-path relaying system not only generates the IRI but also introduces collisions at  $D$ . Most existing works on the two-path relay model assume that  $S$ - $D$  link does not exist. However, in a practical mobile scenario, the signal strength of the  $S$ - $D$  link is not always weak enough to be ignored. Therefore, we provide an alternative scheme to deal with the items encapsulated in parenthesis in Table I. The entire transmission procedure is still the same as that described earlier. We only need to rewrite (4) as follows:

$$(\hat{\mathbf{x}}_r[2n-2], \hat{\mathbf{x}}[2n-1])_D = \arg \min_{\text{all } x_{r_i}, x_i \in \mathcal{A}_x} \times \left\| y_D[2n-1] - h_{R_2 D} \Theta_{(2)}^T \mathbf{x}_r - \Theta_{(1)}^T \mathbf{H}_{SD} \mathbf{x} \right\|^2. \quad (7)$$

For convenience, we let gIRIC-noSD represent the system that regards the signals of direct links as noise and gIRIC-SD represent the system that utilizes  $S$ - $D$  links to assist signal detection.

#### IV. SWITCHING STRATEGIES BETWEEN gIRIC-noSD AND gIRIC-SD

For most scenarios, gIRIC-SD achieves better symbol error probability (SEP) behavior than that of gIRIC-noSD, particularly when the signal strength of the  $S$ - $D$  link is sufficiently strong. However, gIRIC-SD requires much more computational complexity due to the ML detector. In addition, if the sources are far from the destination, the effect of direct links can be ignored without obvious degradation of system performance. Hence, taking into account the mobility of the sources, switching strategies are given here to exhibit a tradeoff between computational complexity and system performance.

It is obvious that, if  $\sum_i |h_{S_i D}|$  is in the same order with  $|h_{R_m D}|$  ( $m = 1, 2$ ), the received signal-to-interference-plus-noise ratio at  $D$  of gIRIC-noSD equals approximately  $10 \lg((|h_{R_m D}|^2 P) / (\sum_i |h_{S_i D}|^2 P + P_{noise})) \approx 10 \lg 1 = 0$  dB, which results in poor SEP, low channel capacity, and high outage probability. As a result, if  $\sum_i |h_{S_i D}| \approx |h_{R_m D}|$ , we recommend gIRIC-SD for the destination without additional computations on switching strategies. Therefore, the switching strategies introduced here are based on

$\sum_i |h_{S_i D}| \ll |h_{R_m D}|$ . We particularly highlight that all channel coefficients remain constant within one frame time.

#### A. Mutual-Information-Based Switch

In this switching rule, we parameterize the system in terms of mutual information between sources and destination. Since the transmission of  $S$ - $R_m$  link in gIRIC-noSD is the same as that in gIRIC-SD, we only consider the mutual information between  $R_m$  and  $D$  under the assumption that the source symbols are successfully detected by  $R_m$ . According to (2) and (4), the maximum average mutual information between  $\mathbf{x}$  and  $y_D$  in gIRIC-noSD can be expressed as

$$I_{\text{noSD}} = \frac{1}{2} \sum_{m=1}^2 \log \left( 1 + \frac{|h_{R_m D}|^2 P}{N_0/2 + P \sum_{i=1}^{N_S} |h_{S_i D}|^2} \right) \quad (8)$$

where  $P$  is the transmit power of each sender. The factor  $1/2$  denotes that half of the sources' symbols are forwarded by  $R_1$ , whereas the others correspond to  $R_2$ . Likewise, in gIRIC-SD, we have

$$I_{SD} = \frac{1}{2} \sum_{m=1}^2 \log \left( 1 + \frac{|h_{R_m D}|^2 P + P \sum_{i=1}^{N_S} |h_{S_i D}|^2}{N_0/2} \right). \quad (9)$$

Therefore, for mutual-information-based switching, the destination chooses the detecting mode based on

$$\begin{cases} \text{gIRIC-noSD,} & \text{if } I_{\text{noSD}} + \text{bias}_1 \geq I_{SD} \\ \text{gIRIC-SD,} & \text{if } I_{\text{noSD}} + \text{bias}_1 < I_{SD} \end{cases} \quad (10)$$

where  $\text{bias}_1 = \lambda_1 f_1$ .  $\text{bias}_1$  reveals the overall complexity saved by gIRIC-noSD.  $f_1$  is a function of computational complexity.  $\lambda_1$  ensures that  $\text{bias}_1$  and mutual information are of the same order.  $\text{bias}_1$  varies according to different system constraints. For example, if the transmission requires a high data rate, it may adopt small  $\text{bias}_1$ . Conversely, gIRIC-noSD is a suitable choice to achieve low complexity with large  $\text{bias}_1$ . The calculations of (9) and (10) only need to be performed once per  $L + 1$  TSs or when channel coefficients obviously change.

However, without consideration about the modulation mode and the fact that channel capacity is the theoretical bound, such mutual information-based switch is too idealistic. In practice, modulation mode plays a significant role in determining SEP behavior, which reflects the throughput under a fixed transmission rate. Consequently, we introduce a simplified SEP-based switching rule.

#### B. Simplified SEP-Based Switch

All symbols are delivered to  $D$  through  $S$ - $R$ - $D$ . The SEP at  $D$  can be expressed as

$$P_{e-\text{noSD}} = (1 - P_{e-SR})P_{e-RD} + P_{e-SR} \quad (11)$$

where  $P_{e-SR}$  represents the SEP of the  $S$ - $R$  link, whereas  $P_{e-RD}$  corresponds to the  $R$ - $D$  link. Both of the detecting modes share the same SEP of the  $S$ - $R$  link. As a result, simplified SEP-based switching rule parameterizes the system only in terms of  $P_{e-RD}$ . Making use of the union bound [13], the average SEP of the  $R$ - $D$  link for gIRIC-noSD is upper bounded by

$$P_{RD-\text{noSD}} \leq \frac{1}{2} (M^{N_S} - 1) \sum_{m=1}^2 Q \left( \frac{|h_{R_m D}| d_{\min}^{\Theta^T \mathbf{x}}}{\sqrt{2(N_0 + 2P \sum_{i=1}^{N_S} |h_{S_i D}|^2)}} \right) \quad (12)$$

where  $d_{\min}^{\Theta^T \mathbf{x}}$  is the minimum Euclidean distance in the constellation of  $\Theta_{(m)}^T \mathbf{x}$  and  $M = |\mathcal{A}_x|$ . To facilitate the calculation, we make another

approximation based on the Chernoff bound [14]

$$P_{RD-\text{noSD}} \leq \frac{1}{2} (M^{N_S} - 1) \sum_{m=1}^2 \exp \left( - \frac{|h_{R_m D}|^2 d_{\min}^{2\Theta^T \mathbf{x}}}{4(N_0 + 2P \sum_{i=1}^{N_S} |h_{S_i D}|^2)} \right). \quad (13)$$

Likewise, for gIRIC-SD, the corresponding SEP of the  $R$ - $D$  link is given by

$$P_{RD-SD} \leq \frac{1}{2} (M^{N_S} - 1) \sum_{m=1}^2 \exp \left( - \frac{|h_{R_m D}|^2 d_{\min}^{2\Theta^T \mathbf{x}}}{4N_0} \right). \quad (14)$$

Then, the simplified SEP-based switching rule is given as

$$\begin{cases} \text{gIRIC-noSD,} & \text{if } P_{RD-\text{noSD}} \leq P_{RD-SD} + \text{bias}_2 \\ \text{gIRIC-SD,} & \text{if } P_{RD-\text{noSD}} > P_{RD-SD} + \text{bias}_2 \end{cases} \quad (15)$$

where  $\text{bias}_2 = \lambda_2 f_2$ .  $\lambda_2$  and  $f_2$  play the same role as  $\lambda_1$  and  $f_1$ . Since the range of SEP is different from that of mutual information, former  $\text{bias}_1$  is no longer applicable. Thus,  $\text{bias}_2$  is the redesign of  $\text{bias}_1$ .

#### C. Discussion

The selection of detecting mode is performed at  $D$  as follows.

- 1) When the first two symbols in a frame arrive,  $D$  measures channel coefficients via estimation from training sequences in protocol headers.
  - If channel coefficients are the same as those of the former frame,  $D$  continuously operates in the same detecting mode and continues with Step 3.
  - If  $\sum_i |h_{S_i D}| \approx |h_{R_m D}|$ ,  $D$  directly chooses gIRIC-SD and continues with Step 3.
- 2) According to measured channel coefficients,  $D$  performs one of the two switching rules to determine a suitable detecting mode.
- 3) Based on the chosen detecting mode,  $D$  estimates the received symbols until the end of this frame or obvious changes of channel coefficients.

The mutual-information-based switch requires fewer computations, whereas the simplified SEP-based switch is consistent with practice via taking into account divers modulation constellations at a cost of more computational complexity. We provide these comparisons as the reference for choosing a switching rule between the given alternatives in Step 2.

The configurations of  $\text{bias}_t$  ( $t = 1, 2$ ) play a significant role in switching. Since  $\text{bias}_t$  reflects system overheads that vary in different networks and is not the focus of our paper, we will not detail its design.

#### V. SYMBOL ERROR PROBABILITY AND THROUGHPUT ANALYSIS

Earlier, in the simplified SEP-based switch, only the SEP of the  $R$ - $D$  link is deduced to achieve fewer computations. Thus, here, the bounds of average end-to-end (e2e) SEP from each source to the destination and the throughput will be analyzed. Regardless of computational complexity, we focus on the gIRIC-SD detecting mode.

Let  $s = \Theta_{(\bar{m})}^T \mathbf{H}_{SD} \mathbf{x} - h_{R_m D} \Theta_{(m)}^T \mathbf{x}_r$ , where ( $m = 1, \bar{m} = 2$ ) or ( $m = 2, \bar{m} = 1$ ). The destination should recover the symbols from relay (i.e.,  $\mathbf{x}_r$ ). According to [11, Sec. V-A], adopting e CFNC in the multisource system, the result calculated via (14) is the SEP of  $s$ , rather than  $x_{r_i} \in \mathbf{x}_r$  ( $i = 1, 2, \dots, N_S$ ). To obtain an average e2e SEP from each source to the destination, we rewrite (11) as

$$P_{e2e}^* = P_{e-RD}^* + P_{e-SR}^* - P_{e-SR}^* P_{e-RD}^* \quad (16)$$

where  $P_{e2e}^*$ ,  $P_{e-SR}^*$ , and  $P_{e-RD}^*$  represent the average e2e SEP of source-destination, source-relay, and relay-destination, respectively.

TABLE II  
 SIMULATION PARAMETERS

Parameters	Value
Modulation Mode	BPSK
Packet Size ( $L$ )	128 bits
Source number ( $N_S$ )	1/2/3
User Antenna Gain	0 dBi
$\Theta^T$	LCF[21]
Noise Power	-174 dBm/Hz
Channel fading	Rayleigh fading

According to [11, Eq. (25)], we have

$$P_{e-RD}^* \leq \frac{1}{2N_S|\mathcal{A}_s|} \sum_{m=1}^2 \sum_{k=1}^{N_S} k \sum_{a=1}^{|\mathcal{A}_s|} \left( \sum_{\substack{b=1 \\ \|\mathbf{x}_{r_a} - \mathbf{x}_{r_b}\|_0 = k}}^{|\mathcal{A}_s|} Q\left(\frac{d_{ab}^{(s)}}{\sqrt{2N_0}}\right) \right) \quad (17)$$

where  $d_{ab}^{(s)}$  denotes the Euclidean distance between  $s_a$  and  $s_b$ .  $s_a = \Theta_{(\bar{m})}^T \mathbf{H}_{SD} \mathbf{x}_a - h_{RmD} \Theta_{(\bar{m})}^T \mathbf{x}_{r_a}$  and  $s_b = \Theta_{(\bar{m})}^T \mathbf{H}_{SD} \mathbf{x}_b - h_{RmD} \Theta_{(\bar{m})}^T \mathbf{x}_{r_b}$  are two different points in the constellation of  $s$  (finite alphabet  $\mathcal{A}_s$  with cardinality  $|\mathcal{A}_s|$ ).  $\|\mathbf{x}_{r_a} - \mathbf{x}_{r_b}\|_0$  indicates the number of nonzero elements of  $\mathbf{x}_{r_a} - \mathbf{x}_{r_b}$ .

For the source-relay link, let  $z = \Theta_{(\bar{m})}^T \mathbf{H}_{SRm} \mathbf{x} + h_{12} \Theta_{(\bar{m})}^T \mathbf{x}_r$  (the signal received by relay, regardless of noise). The relay wants to recover  $\mathbf{x}$ . As in the relay-destination link,  $P_{e-SR}^*$  can be calculated through the following:

$$P_{e-SR}^* \leq \frac{1}{2N_S|\mathcal{A}_z|} \sum_{m=1}^2 \sum_{k=1}^{N_S} k \sum_{a=1}^{|\mathcal{A}_z|} \left( \sum_{\substack{b=1 \\ \|\mathbf{x}_a - \mathbf{x}_b\|_0 = k}}^{|\mathcal{A}_z|} Q\left(\frac{d_{ab}^{(z)}}{\sqrt{2N_0}}\right) \right). \quad (18)$$

$d_{ab}^{(z)}$  represents the Euclidean distance between  $z_a$  and  $z_b$ , where  $z_a = \Theta_{(\bar{m})}^T \mathbf{H}_{SRm} \mathbf{x}_a + h_{12} \Theta_{(\bar{m})}^T \mathbf{x}_{r_a}$ , and  $z_b = \Theta_{(\bar{m})}^T \mathbf{H}_{SRm} \mathbf{x}_b + h_{12} \Theta_{(\bar{m})}^T \mathbf{x}_{r_b}$ . Then, based on (17) and (18), the upper bound of the average e2e SEP from each source to the destination ( $P_{e2e}^*$ ) is obtained through (16).

Here, the throughput (represented by  $T$ ) is defined as the number of successfully recovered symbols by the destination per TS. Thus, the throughput of our proposed scheme is expressed as

$$T_{\text{gIRIC}} = \frac{1}{L+1} \sum_{n=2}^{L+1} N_S \times \left(1 - P_{e2e}^{(n)}\right) \text{ sym/TS} \quad (19)$$

where  $P_{e2e}^{(n)}$  is the average e2e SEP at the destination during TS  $n$ . Since there is no IRI at TS 1 and no interference at TS  $L+1$ ,  $P_{e2e}^{(n)}$  is given by

$$P_{e2e}^{(n)} = \begin{cases} P_{e-RD}^* + P'_{e-SR} - P'_{e-SR} P_{e-RD}^*, & n = 2 \\ P_{e2e}^*, & n \in [3, L] \\ P'_{e-RD} + P_{e-SR}^* - P_{e-SR}^* P'_{e-RD}, & n = L+1 \end{cases} \quad (20)$$

where  $P'_{e-SR}$  and  $P'_{e-RD}$  are the average e2e SEPs in the case of no IRI at relay and no collision at destination, respectively. With large  $L$ , we have  $T_{\text{gIRIC}} \approx N_S(1 - P_{e2e}^*)$ . With the increase in SNR, the upper bound of  $T_{\text{gIRIC}}$  is  $N_S$  sym/TS. The given derivations are based on gIRIC-SD. The analysis on gIRIC-noSD is analogous to that of gIRIC-SD.

## VI. SIMULATION

### A. Simulation Setup

Here, the SEP behaviors of our proposed scheme are investigated through Monte Carlo simulations. Some primary simulation parameters are presented in Table II. In addition, we set  $h_{S_i R_m}$ ,  $h_{12}$ , and  $h_{R_m D} \sim \mathcal{CN}(0, 1)$ . Let  $\gamma_{S_i R} = \gamma_{RD} = \gamma_{12} = \gamma = (P/N_0/2)$ , denoting the notation ‘‘SNR’’ in Figs. 3–5. We assume  $E\{[h_{S_i D}]^2\} \in$

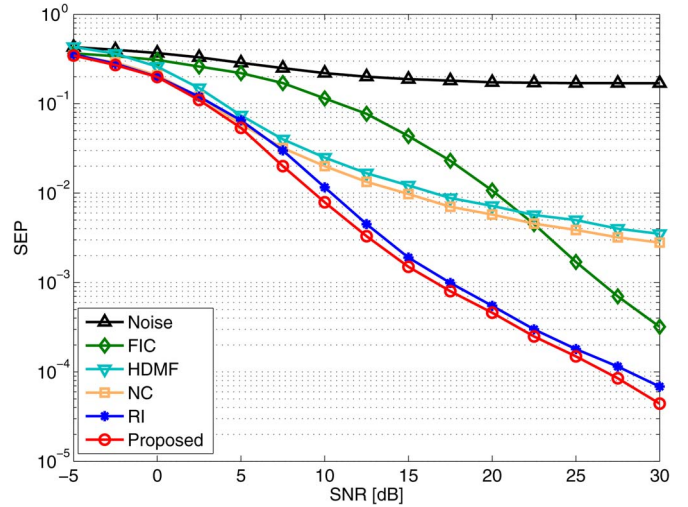


Fig. 3. SEP comparisons in the (1, 2, 1) system.  $\gamma_{SD} = \gamma - 5$  dB.

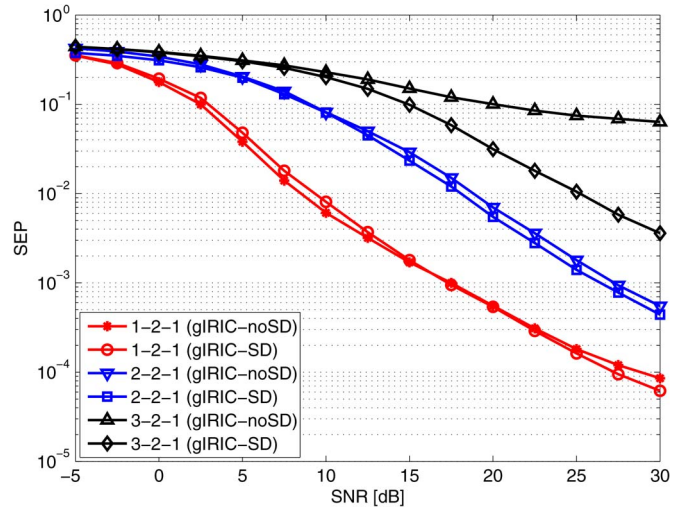


Fig. 4. SEP comparisons between the proposed gIRIC-noSD and gIRIC-SD in the  $(N_S, 2, 1)$  system.  $\gamma_{S_i D} = \gamma - 10$  dB.

$\{0.1, \sqrt{0.1}\}$  to simulate different positions of sources, corresponding to  $\gamma_{S_i D} = \gamma - 10$  dB and  $\gamma_{S_i D} = \gamma - 5$  dB, respectively.

For comparison, we choose several existing strategies as the benchmarks. First, the scheme that treats the interrelay signals as noise, labeled as ‘‘Noise,’’ is considered to demonstrate the necessity of removing IRI. Then, the schemes proposed in [5]–[8] are labeled as ‘‘NC,’’ ‘‘FIC,’’ ‘‘RI,’’ and ‘‘HDMF,’’ respectively. We label our proposed scheme as ‘‘Proposed’’ or ‘‘gIRIC.’’

### B. Results and Discussions

First, we compare the SEP performance of our scheme with those of existing strategies in the (1, 2, 1) system, as shown in Fig. 3. Since we mainly aim at verifying the lower SEP achieved by the proposed scheme,  $D$  adopts gIRIC-SD. Based on the fact that these benchmarks, except FIC, do not take the  $S$ – $D$  link into consideration, our gIRIC achieves the best SEP behavior throughout the range of SNR. Among all benchmarks, RI exploits the orthogonality of the in-phase and quadrature-phase components of the symbol to distinguish the information and interference, which is similar to our gIRIC when  $\theta_1 = 1$  and  $\theta_2 = j$ . FIC also considers the effect of the  $S$ – $D$  link, which leads to a faster decrease in SEP within a high SNR.

Second, we compare the performance between gIRIC-noSD and gIRIC-SD in  $(N_S, 2, 1)$  systems ( $N_S = 1/2/3$ ). In Fig. 4, we set

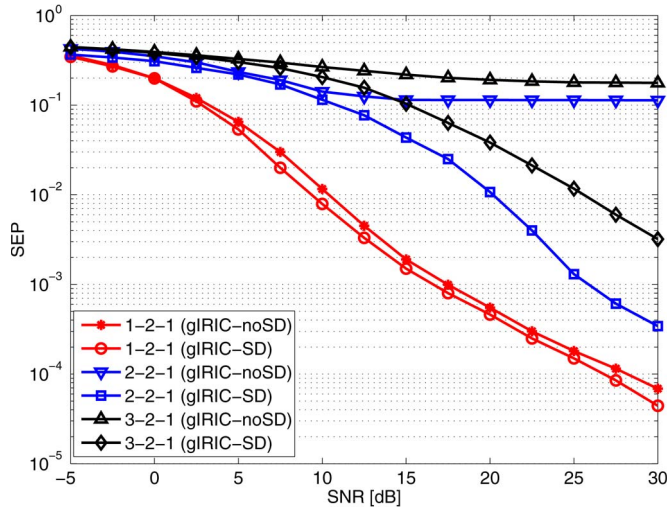


Fig. 5. SEP comparisons between the proposed gIRIC-noSD and gIRIC-SD in the  $(N_S, 2, 1)$  system.  $\gamma_{S_i D} = \gamma - 5$  dB.

$\gamma_{S_i D} = \gamma - 10$  dB, which suggests that sources are far away from the destination. Under this assumption, the signal strength of direct link is so weak that the SEP behavior of gIRIC-noSD is similar to that of gIRIC-SD. Under a low SNR region, we recommend gIRIC-noSD since both of the detecting modes achieve similar performance. Although each  $|h_{S_i D}|$  is small, the value of  $\sum_{i=1}^{N_S} |h_{S_i D}|^2$  increases with the growth of  $N_S$ . Thus, at the high SNR region, gIRIC-noSD substantially degrades the SEP in the  $(3, 2, 1)$  system. Taking the mobility of the sources into account, we change  $\gamma_{S_i D}$ . The SEP of gIRIC-noSD in either  $(2, 2, 1)$  or  $(3, 2, 1)$  system deteriorates due to  $\gamma_{S_i D} = \gamma - 5$  dB, as shown in Fig. 5, which shows the necessity of performing detecting modes' selection at  $D$ .

## VII. CONCLUSION

In this paper, we have proposed a new scheme named gIRIC in a two-path relay system. In gIRIC, CFNC and ML detection are performed to separate each source symbol and the IRI. Taking direct links into consideration, we introduced two switching rules for destination to select a suitable detecting mode between gIRIC-noSD and gIRIC-SD. Then, the bounds of average e2e SEP and throughput were derived. In addition, numerical simulation results verified the SEP improvement of gIRIC and the effects of direct links.

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## Performance Analysis of Two-Way AF MIMO Relaying of OSTBCs With Imperfect Channel Gains

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**Abstract**—In this paper, we consider the relaying of orthogonal space-time block codes (OSTBCs) in a two-way amplify-and-forward (AF) multiple-input-multiple-output (MIMO) relay system with estimated channel state information (CSI). A simple four-phase protocol is used for training and OSTBC data transmission. Decoding of OSTBC data at a user terminal is performed by replacing the exact CSI by the estimated CSI in a maximum-likelihood (ML) decoder. Tight approximations for the moment-generating function (MGF) of the received signal-to-noise ratio (SNR) at a user is derived under Rayleigh fading by ignoring the higher order noise terms. Analytical average error performance of the considered cooperative scheme is derived by using the MGF expression. Moreover, the analytical diversity order of the considered scheme is also obtained for certain system configurations. It is shown by simulations and analysis that the channel estimation does not affect the diversity order of the OSTBC-based two-way AF MIMO relay system.

**Index Terms**—Amplify-and-forward (AF) protocol, channel estimation, cooperative diversity, M-ary phase-shift keying (M-PSK), multiple-input-multiple-output (MIMO) system, orthogonal space-time block codes (OSTBCs), Rayleigh fading, symbol error rate (SER), two-way relaying.

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