# The absorption spectrum of $\mathrm{H}_{2} \mathrm{~S}$ between 9540 and $10000 \mathrm{~cm}^{-1}$ by intracavity laser absorption spectroscopy with a vertical external cavity surface emitting laser ${ }^{2 /}$ 

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Dedicated to Professor H. Bürger on the occasion of his 65th birthday.


#### Abstract

An Intracavity Laser Absorption Spectrometer (ICLAS) based on a Vertical External Cavity Surface Emitting Laser (VECSEL) has been used to record the absorption spectrum of $\mathrm{H}_{2}$ S between 9540 and $10000 \mathrm{~cm}^{-1}$ with pressures up to $122 \mathrm{Torr}(160.5 \mathrm{hPa})$ and equivalent absorption path lengths up to 45 km . More than 1600 absorption lines were attributed to the transitions reaching the highly excited $\left(40^{ \pm}, 0\right),\left(30^{ \pm}, 2\right)$, and $\left(11^{+}, 4\right)$ states (local mode notation). The existing information relative to the $\left(40^{ \pm}, 0\right)$ local mode bright pair at $9911.02 \mathrm{~cm}^{-1}$ was considerably enlarged, while the other states are reported for the first time. Eight hundred and ninety two precise energy levels were derived, including 181 and 28 levels for the $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ and $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ minor isotopomers, respectively. These energy levels were fitted using a Watson-type rotational Hamiltonian and the spectroscopic parameters were obtained, yielding an rms deviation of $0.006 \mathrm{~cm}^{-1}$ for the $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ species - close to the experimental accuracy. The dark states- $\left(20^{+}, 4\right)$ and $\left(11^{+}, 4\right)$-at 9647.77 and $9744.88 \mathrm{~cm}^{-1}$, respectively, were found to perturb the observed energy levels and were then included into the final energy levels modeling. The $\left(40^{ \pm}, 0\right)$ states are very close to the local mode limit, i.e., with a mostly identical rotational structure. The $\left(30^{ \pm}, 2\right)$ states are separated by $0.077 \mathrm{~cm}^{-1}$ and this separation holds for most of the rotational sublevels. The resonance interactions between the three local mode pairs- $\left(40^{ \pm}, 0\right),\left(30^{ \pm}, 2\right)$, and $\left(20^{ \pm}, 4\right)$-and the $\left(11^{+}, 4\right)$ state affect in some cases specifically one of the component of the pair and then the energy separation of the corresponding near degenerate rotational levels. Line intensities were obtained on the basis of the relative intensities measured by ICLAS and from absolute values of the stronger lines measured separately by Fourier Transform Spectroscopy associated with a multipass cell. The transition intensities could be successfully modeled and the integrated band intensities are given and discussed.


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## 1. Introduction

Intracavity Laser Absorption Spectroscopy (ICLAS) is a highly sensitive absorption technique which has been extensively applied above $10000 \mathrm{~cm}^{-1}$ with Ti:sapphire

[^0]and dye lasers. An interesting development towards the near infrared region has been recently achieved in Grenoble by using Quantum Wells semiconductor structures as amplification media. After the first developments and the study of the dynamics of the Vertical External Cavity Surface Emitting Lasers (VECSEL) by Garnache et al. [1,2], ICLAS-VECSELs were used between 9400 and $10100 \mathrm{~cm}^{-1}$ for the overtone spectroscopy of propyne [3], $\mathrm{N}_{2} \mathrm{O}$ [4], and $\mathrm{CO}_{2}$ [5]. The present study is devoted to the absorption spectrum of hydrogen sulfide between 9500 and $10000 \mathrm{~cm}^{-1}$.

We have extensively studied the overtone spectrum of $\mathrm{H}_{2} \mathrm{~S}$ by ICLAS with Ti:sapphire and dyes above $10000 \mathrm{~cm}^{-1}$ [6-10]. Our last report was, for instance, devoted to the highest overtone transition of $\mathrm{H}_{2} \mathrm{~S}$ reported so far, observed in the $16180-16440 \mathrm{~cm}^{-1}$ region and corresponding to an excitation of the $\left(70^{ \pm}, 0\right)$ local mode pair [10]. The present investigation concerns the spectral region between 9540 and $10000 \mathrm{~cm}^{-1}$ involving mainly the $\left(40^{ \pm}, 0\right)$ local mode pair near $9911 \mathrm{~cm}^{-1}$. This spectral region was not previously investigated by any high sensitive laser technique and the existing information relative to the $\left(40^{ \pm}, 0\right)$ local mode pair was retrieved from Fourier Transform spectra recorded at Kitt Peak with a multipass cell with optical path lengths up to 433 m [11]. The increased sensitivity presently achieved has allowed to extend considerably the knowledge of the rotational structure of the $\left(40^{ \pm}, 0\right)$ local mode pair, while three states involving bending excitation could be newly detected from weak transitions.

## 2. Experiment

We used the experimental set-up based on a VECSEL configuration similar to that developed in [2] and described in [4]. The tuning of the wavelength is obtained by translating the sample position and varying the temperature between -30 and $+60^{\circ} \mathrm{C}$. The typical temperature tuning rate is $0.5 \mathrm{~cm}^{-1} /{ }^{\circ} \mathrm{C}$. The pump laser is a commercial diode lasing at 830 nm and the threshold power of the VECSEL was about 100 mW . The pump
was driven by a pulsed voltage. After the generation time, the output beam was deflected by an acousto-optic modulator into the grating spectrograph equipped with a 3724-pixels silicon array in its focal plane (see [4] for more details). The spectral region simultaneously recorded with a typical spectral resolution of $0.03 \mathrm{~cm}^{-1}$ was about $12 \mathrm{~cm}^{-1}$ within a few seconds. Generation times ranging between 200 and $400 \mu$ s corresponding to equivalent absorption path lengths of $30-60 \mathrm{~km}$ were adopted leading to a typical sensitivity of $\alpha \approx 10^{-9} \mathrm{~cm}^{-1}$. The wavenumber calibration procedure of the spectra requires two reference lines for each spectrograph position. In the high energy part of the considered spectral range, atmospheric water lines [12] could be used as reference. However, in the lower energy part, the water lines are too sparse and weak. For this purpose, the Fourier Transform Spectrum of $\mathrm{H}_{2} \mathrm{~S}$ was recorded in Hefei by using a Bruker 120 HR interferometer associated with a multipass cell to use some relatively strong absorption $\mathrm{H}_{2} \mathrm{~S}$ lines to calibrate the numerous supplementary weaker lines observed by ICLAS. A tungsten source, near-IR quartz beam splitter and a Ge detector were used. The unapodized resolution was $0.02 \mathrm{~cm}^{-1}$ (1/ maximum optical path difference). Scans (1150) were accumulated to improve the signal-to-noise ratio. The sample pressure and the absorption path length were $P=206 \mathrm{hPa}$ and $l=87 \mathrm{~m}$, respectively, leading to $P \times l$ value close to that of [11]. In term of sensitivity, the signal-to-noise ratio presently achieved is slightly larger than that of [11]. The calibration of the FT spectrum was performed with $\mathrm{H}_{2} \mathrm{O}$ lines taken from [12] leading to


Fig. 1. Overview of the absorption spectrum of $\mathrm{H}_{2} \mathrm{~S}$ between 9540 and $10000 \mathrm{~cm}^{-1}$. (a) FT spectrum used to calibrate ICLAS (resolution $0.02 \mathrm{~cm}^{-1}$, pressure 206 hPa , absorption path length 87 m ). (b) Experimental ICLAS-VECSEL stick spectrum recorded with an equivalent absorption path length 30 km and a pressure 35.5 hPa ( 27 Torr ). The absolute values of the line intensities were deduced from the FT spectrum. (c) Simulated spectrum of $\mathrm{H}_{2} \mathrm{~S}$. The line positions were calculated using the Hamiltonian parameters of Table 4.
an excellent agreement with the values obtained in [11]. From the comparison of the wavenumber values obtained by using independent reference lines, we estimate the absolute wavenumber accuracy of the ICLAS line positions to be better than $0.01 \mathrm{~cm}^{-1}$.

An overview of the FT and ICLAS spectra are presented in Fig. 1 while a comparison for two specific spectral regions is displayed in Figs. 2 and 3.

## 3. Rovibrational analysis

Among the 1630 absorption lines measured between 9541 and $10001 \mathrm{~cm}^{-1}$, about 1300 were assigned to the $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ species. The line list is attached to the present paper as Supplementary Material. The spectrum is dominated by transitions reaching the (301) and (202) pure stretching vibrational states (in normal mode (NM)


Fig. 2. The absorption spectrum of $\mathrm{H}_{2} \mathrm{~S}$ between 9785 and $9804 \mathrm{~cm}^{-1}$. (a) FT spectrum used to calibrate ICLAS (resolution $0.02 \mathrm{~cm}^{-1}$, pressure 206 hPa , absorption path length 87 m ). (b) Experimental ICLAS-VECSEL spectrum recorded with an equivalent absorption path lengths 30 km , pressure 35.5 hPa ( 27 Torr). (c) Simulated spectrum of $\mathrm{H}_{2} \mathrm{~S}$. The line positions were calculated using the Hamiltonian parameters of Table 4 .


Fig. 3. Same as Fig. 2 for the $9832-9846 \mathrm{~cm}^{-1}$ region. Note that the lines due to the $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ minor isotope, marked " 34 ," were not considered in the simulated spectrum.
notation) which form the $\left(40^{ \pm}, 0\right)$ local mode (LM) pair at $9911.023 \mathrm{~cm}^{-1}$. Compared to the previous FT study of [11], the higher sensitivity presently achieved has allowed increasing considerably the number of rotational levels. Interestingly, three weaker bands corresponding to the (221) and (122) vibrational levels $\left(\left(30^{ \pm}, 2\right)\right.$ in LM notation) and the highly excited bending level (141) ( $\left(20^{-}, 4\right)$ in LM notation) could be detected for the first time. The vibrational term values of the states under consideration are gathered in Table 1 together with their NM and LM labelings and the number of levels derived for each state.

Since a significant number of the analyzed transitions are weak single lines not included into Ground State Combination Difference (GSCD) relations, the assignment process relied greatly on the predictive calculations based on the rotational, centrifugal distortion, resonance, and transition moment parameters which were obtained and permanently refined by fitting the experimental energy levels and line intensities (see below). As a result of the spectrum assignment, 892 precise energy levels were derived for the three $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$, $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$, and $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ isotopomers by adding the ground state energies [13] to the identified transitions. The experimental accuracy calculated from the levels observed through several transitions is $0.003 \mathrm{~cm}^{-1}$. In contrast to the approach adopted in [9] where the same set of energy levels was derived for the $\left(40^{ \pm}, 1\right)$ states by treating simultaneously, in the $C_{s}$ symmetry group, the corresponding $A$ and $B$ transitions of the $\left(40^{ \pm}, 1\right)-$ (000) band, in this study, we derived separate energy
level sets for each component of the $\left(40^{ \pm}, 0\right)$ LM pair. The reason for this choice is the observation of a systematic shift of $0.005-0.010 \mathrm{~cm}^{-1}$ between the two sets of energy levels (the levels of the $\left(40^{+}, 0\right)$ state being slightly lower than those of the $\left(40^{-}, 0\right)$ state). This shift increases up to $0.025 \mathrm{~cm}^{-1}$ for high values of the rotational quantum number $J$. In addition, resonance interactions with the other considered vibrational states affect differently a number of levels of the $\left(40^{ \pm}, 0\right)$ pair and increase the separation up to $0.076 \mathrm{~cm}^{-1}$. As a result, 178 and 157 of the identified levels (compared to 73 and 47, respectively, in [11]) were assigned to the $\left(40^{+}, 0\right)$ and $\left(40^{-}, 0\right) \mathrm{H}_{2}{ }^{32} \mathrm{~S}$ local mode states, respectively, while $133,122,91$, and 2 were attributed to the $\left(30^{-}, 2\right),\left(30^{+}, 2\right),\left(20^{-}, 4\right)$, and $\left(11^{+}, 4\right) \mathrm{H}_{2}^{32} \mathrm{~S}$ states, respectively. These observed energy levels followed by experimental uncertainties, number of lines used for the energy level determination, and deviations from the calculated values (see below) are listed in Table 2 for the $\left(40^{ \pm}, 0\right)$ local mode pair and in Table 3 for the four other $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ states. A few energy levels marked by asterisk were found perturbed by dark states not included into our model and then excluded from the fit described hereafter.

Finally 654 of the 683 observed energy levels of $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ could be reproduced by a Watson-type effective Hamiltonian in $I^{r}$ representation used for vibrationally diagonal blocks. The resonance Fermi and Coriolis-type operators were taken of the following form:
$H^{F}=F_{k} J_{z}^{2}+F_{j} J^{2}+F_{x y} J_{x y}^{2}+\cdots$,

Table 1
Vibrational assignments, vibrational term values (in $\mathrm{cm}^{-1}$ ) and band intensities of the different levels of hydrogen sulfide studied between 9540 and $10000 \mathrm{~cm}^{-1}$

| Vibrational state |  | $N^{\text {c }}$ | $E_{v}$ |  |  | Band intensity ( $\times 10^{-4} \mathrm{~cm}^{-2} \mathrm{~atm}^{-1}$ ) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NM ${ }^{\text {a }}$ | $\mathrm{LM}^{\text {b }}$ |  | Obs. | Obs. - Calc. [4] | Obs. - Calc. [16] | Measured | Ref. [15] |
| $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ |  |  |  |  |  |  |  |
| 141 | $20^{-}, 4$ | 91 | 9647.167 | 0.35 | 0.23 | 0.142 | 0.10 |
| 042 | $20^{+}, 4$ | 0 | $9647.774^{\text {d }}$ | 0.53 | 0.11 | 0.001 | 0.002 |
| 240 | $11^{+}, 4$ | 2 | $9744.888^{\text {d }}$ | -0.89 | -0.92 | 0.002 | 0.001 |
| 221 | $30^{-}, 2$ | 133 | 9806.667 | 0.21 | 0.01 | 0.879 | 0.01 |
| 122 | $30^{+}, 2$ | 122 | 9806.733 | 0.16 | -0.07 | 0.382 | 3.76 |
| 301 | $40^{-}, 0$ | 178 | 9911.023 | -0.02 | 0.00 | 4.84 | 8.10 |
| 202 | $40^{+}, 0$ | 157 | 9911.023 | -0.04 | 0.00 | 1.31 | 0.15 |
| $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ |  |  |  |  |  |  |  |
| 301 | $40^{-}, 0$ | 17 | $9907.050^{\text {d }}$ |  | 0.01 |  |  |
| 202 | $40^{+}, 0$ | 11 | $9907.050^{\text {d }}$ |  | 0.01 |  |  |
| $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ |  |  |  |  |  |  |  |
| 221 | $30^{-}, 2$ | 34 | $9798.741^{\text {d }}$ |  | 0.02 |  |  |
| 122 | $30^{+}, 2$ | 14 | $9798.796^{\text {d }}$ |  | -0.06 |  |  |
| 301 | $40^{-}, 0$ | 81 | 9903.323 |  | 0.01 |  |  |
| 202 | $40^{+}, 0$ | 52 | $9903.313^{\text {d }}$ |  | 0.00 |  |  |

[^1]Table 2
Rotational energy levels $\left(\mathrm{cm}^{-1}\right)$ of the $\left(40^{-}, 0\right)$ and $\left(40^{+}, 0\right)$ vibrational states of $\mathrm{H}_{2}{ }^{32} \mathrm{~S}((301)$ and (202), respectively, in normal mode notation)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 0 | 0 | 0 | 9911.023 |  | 1 | -0.001 | 9911.023 |  | 1 | 0.004 |
| 1 | 0 | 1 | 9923.861 | 1 | 2 | 0.005 | 9923.848 |  | 1 | -0.005 |
| 1 | 1 | 1 | 9925.369 | 1 | 2 | -0.001 | 9925.365 |  | 1 | -0.002 |
| 1 | 1 | 0 | 9929.253 | 1 | 2 | 0.001 | 9929.248 | 2 | 2 | 0.001 |
| 2 | 0 | 2 | 9946.782 | 1 | 3 | -0.002 | 9946.782 | 4 | 2 | -0.002 |
| 2 | 1 | 2 | 9947.148 | 7 | 3 | 0.001 | 9947.145 | 3 | 4 | -0.001 |
| 2 | 1 | 1 | 9958.781 | 2 | 4 | -0.002 | 9958.771 |  | 1 | -0.009 |
| 2 | 2 | 1 | 9963.321 | 1 | 2 | 0.000 | 9963.315 | 1 | 2 | -0.004 |
| 2 | 2 | 0 | 9966.048 | 1 | 3 | 0.001 | 9966.038 | 2 | 2 | -0.005 |
| 3 | 0 | 3 | 9978.420 | 2 | 2 | -0.001 | 9978.417 | 3 | 2 | -0.002 |
| 3 | 1 | 3 | 9978.362 | 1 | 4 | -0.003 | 9978.359 | 2 | 2 | -0.003 |
| 3 | 1 | 2 | 10000.085 | 2 | 3 | 0.001 | 10000.079 | 1 | 2 | -0.004 |
| 3 | 2 | 2 | 10001.776 | 2 | 4 | 0.000 | 10001.771 | 1 | 4 | -0.004 |
| 3 | 2 | 1 | 10011.380 | 1 | 4 | 0.001 | 10011.378 | 9 | 2 | 0.002 |
| 3 | 3 | 1 | 10020.386 | 1 | 3 | 0.002 | 10020.379 | 2 | 2 | -0.002 |
| 3 | 3 | 0 | 10021.960 | 1 | 2 | -0.004 | 10021.960 | 3 | 3 | 0.000 |
| 4 | 0 | 4 | 10018.758 | 1 | 3 | 0.001 | 10018.753 |  | 1 | 0.004 |
| 4 | 1 | 4 | 10018.752 | 2 | 4 | -0.001 | 10018.752 |  | 1 | 0.007 |
| 4 | 1 | 3 | 10050.636 | 2 | 5 | 0.001 | 10050.632 | 3 | 3 | 0.000 |
| 4 | 2 | 3 | 10050.250 |  | 1 | -0.004 | 10050.246 | 3 | 3 | -0.006 |
| 4 | 2 | 2 | 10070.299 | 2 | 4 | -0.004 | 10070.298 | 2 | 3 | -0.005 |
| 4 | 3 | 2 | 10074.776 | 2 | 3 | -0.006 | 10074.781 | 1 | 4 | -0.001 |
| 4 | 3 | 1 | 10081.965 | 1 | 5 | 0.000 | 10081.974 | 1 | 2 | 0.011 |
| 4 | 4 | 1 | 10096.654 | 2 | 3 | 0.001 | 10096.643 | 3 | 3 | -0.007 |
| 4 | 4 | 0 | 10097.431 | 2 | 3 | 0.000 | 10097.423 | 1 | 2 | -0.004 |
| 5 | 0 | 5 | 10068.041 | 3 | 3 | -0.001 | 10068.040 |  | 1 | 0.002 |
| 5 | 1 | 5 | 10068.041 | 1 | 3 | 0.000 | 10068.040 |  | 1 | 0.003 |
| 5 | 1 | 4 | 10108.908 | 2 | 3 | 0.005 | 10108.894 | 1 | 2 | -0.005 |
| 5 | 2 | 4 | 10108.835 | 2 | 4 | 0.002 | 10108.825 |  | 1 | -0.001 |
| 5 | 2 | 3 | 10140.683 | 7 | 4 | 0.004 | 10140.678 | 9 | 5 | 0.001 |
| 5 | 3 | 3 | 10139.266 | 1 | 5 | -0.002 | 10139.259 | 2 | 3 | -0.008 |
| 5 | 3 | 2 | 10157.452 | 6 | 3 | 0.000 | 10157.446 | 3 | 4 | -0.005 |
| 5 | 4 | 2 | 10166.293 | 1 | 4 | -0.001 | 10166.295 | 5 | 4 | 0.002 |
| 5 | 4 | 1 | 10171.039 | 3 | 4 | -0.004 | 10171.035 | 1 | 2 | -0.005 |
| 5 | 5 | 1 | 10192.175 | 1 | 2 | 0.000 | 10192.169 | 3 | 4 | -0.003 |
| 5 | 5 | 0 | 10192.515 | 2 | 2 | 0.001 | 10192.506 | 4 | 3 | -0.006 |
| 6 | 0 | 6 | 10126.250 | 1 | 4 | 0.005 | 10126.249 |  | 1 | 0.010 |
| 6 | 1 | 6 | 10126.248 | 3 | 3 | 0.003 | 10126.249 | 1 | 2 | 0.010 |
| 6 | 1 | 5 | 10176.186 | 3 | 4 | -0.002 | 10176.179 | 3 | 3 | -0.006 |
| 6 | 2 | 5 | 10176.175 | 1 | 2 | -0.002 | 10176.177 |  | 1 | 0.004 |
| 6 | 2 | 4 | 10216.619 | 1 | 3 | 0.001 | 10216.618 |  | 1 | 0.003 |
| 6 | 3 | 4 | 10216.306 | 1 | 2 | -0.002 | 10216.303 | 4 | 3 | -0.001 |
| 6 | 3 | 3 | 10248.568 | 4 | 5 | 0.007 | 10248.564 | 4 | 2 | 0.004 |
| 6 | 4 | 3 | 10244.860 | 2 | 3 | 0.011 | 10244.839 | 4 | 3 | -0.009 |
| 6 | 4 | 2 | 10261.839 | 3 | 4 | -0.001 | 10261.839 | 2 | 2 | 0.001 |
| 6 | 5 | 2 | 10276.440 | 6 | 3 | 0.005 | 10276.434 | 3 | 4 | -0.001 |
| 6 | 5 | 1 | 10279.178 | 2 | 4 | 0.003 | 10279.176 | 4 | 2 | 0.003 |
| 6 | 6 | 1 | 10306.923 | 2 | 2 | -0.001 | 10306.920 | 4 | 3 | -0.001 |
| 6 | 6 | 0 | 10307.062 | 1 | 2 | 0.001 | 10307.061 | 2 | 2 | 0.001 |
| 7 | 0 | 7 | 10193.376 | 1 | 3 | 0.002 | 10193.375 |  | 1 | 0.005 |
| 7 | 1 | 7 | 10193.376 | 1 | 3 | 0.001 | 10193.375 |  | 1 | 0.005 |
| 7 | 1 | 6 | 10252.363 | 1 | 3 | 0.002 | 10252.369 | 2 | 3 | 0.002 |
| 7 | 2 | 6 | 10252.364 | 2 | 3 | 0.002 | 10252.363 | 1 | 2 | -0.004 |
| 7 | 2 | 5 | 10301.528 | 2 | 3 | -0.001 | 10301.509 | 2 | 5 | 0.003 |
| 7 | 3 | 5 | 10301.721 | 1 | 4 | 0.010 | 10301.710 | 4 | 2 | 0.001 |
| 7 | 3 | 4 | 10341.767 | 1 | 2 | 0.009 | 10341.759 | 4 | 3 | 0.005 |
| 7 | 4 | 4 | 10340.698 | 2 | 4 | 0.005 | 10340.697 | 4 | 2 | 0.006 |
| 7 | 4 | 3 | 10374.291 | 4 | 3 | -0.010 | 10374.267 | 3 | 4 | -0.012 |
| 7 | 5 | 3 | 10366.689 | 4 | 3 | -0.004 | 10366.689 | 6 | 2 | -0.004 |
| 7 | 5 | 2 | 10383.952 | 3 | 2 | 0.002 | 10383.949 | 1 | 3 | 0.000 |
| 7 | 6 | 2 | 10405.297 | 1 | 2 | -0.002 | 10405.297 | 1 | 2 | -0.002 |

Table 2 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 7 | 6 | 1 | 10406.699 | 6 | 2 | 0.005 | 10406.689 | 2 | 2 | -0.004 |
| 7 | 7 | 1 | 10440.808 | 1 | 2 | -0.007 |  |  |  |  |
| 7 | 7 | 0 | 10440.863 | 3 | 2 | -0.005 | 10440.869 |  | , | 0.002 |
| 8 | 0 | 8 | 10269.405 | 2 | 3 | 0.004 | 10269.398 |  | 1 | 0.001 |
| 8 | 1 | 8 | 10269.406 | 2 | 3 | 0.004 | 10269.398 |  | 1 | 0.001 |
| 8 | 1 | 7 | 10337.441 | 2 | 3 | -0.001 | 10337.437 | 1 | 2 | -0.006 |
| 8 | 2 | 7 | 10337.438 | 4 | 4 | 0.000 | 10337.437 | 1 | 2 | -0.002 |
| 8 | 2 | 6 | 10395.804 | 3 | 4 | -0.003 | 10395.797 | 4 | 2 | 0.005 |
| 8 | 3 | 6 | 10395.800 | 5 | 4 | -0.004 | 10395.807 | 4 | 4 | 0.012 |
| 8 | 3 | 5 | 10444.510 | 3 | 4 | -0.006 | 10444.557* |  | 1 | 0.031 |
| 8 | 4 | 5 | 10444.352 | 3 | 3 | -0.003 | 10444.275 | 5 | 3 | 0.014 |
| 8 | 4 | 4 | 10484.196 | 3 | 4 | 0.009 | 10484.185 | , | 2 | -0.008 |
| 8 | 5 | 4 | 10481.401 | 4 | 2 | -0.005 | 10481.411 | 6 | 3 | 0.008 |
| 8 | 5 | 3 | 10518.161 | 4 | 3 | 0.003 | 10518.161 | 3 | 2 | 0.001 |
| 8 | 6 | 3 | 10504.935 | 4 | 2 | -0.001 | 10504.942 | 3 | 2 | 0.009 |
| 8 | 6 | 2 | 10552.907 | 1 | 2 | -0.008 | 10552.922 | 8 | 2 | 0.005 |
| 8 | 7 | 2 | 10524.368 |  | 1 | -0.001 | 10524.377 | 4 | 4 | 0.001 |
| 8 | 7 | 1 | 10553.563 | 2 | 2 | -0.002 | 10553.559 | 7 | 2 | -0.003 |
| 8 | 8 | 1 | 10593.723 | 3 | 2 | 0.000 | 10593.726 | 3 | 3 | 0.002 |
| 8 | 8 | 0 | 10593.742 | 1 | 2 | 0.000 |  |  |  |  |
| 9 | 0 | 9 | 10354.319 | 2 | 2 | -0.001 | 10354.317 |  | 1 | 0.001 |
| 9 | 1 | 9 | 10354.319 | 2 | 2 | -0.001 | 10354.317 |  | 1 | 0.001 |
| 9 | 1 | 8 | 10431.385 | 1 | 2 | 0.000 | 10431.379 | 5 | 2 | -0.001 |
| 9 | 2 | 8 | 10431.384 | 1 | 2 | -0.001 | 10431.379 | 5 | 2 | -0.001 |
| 9 | 2 | 7 | 10498.701 | 2 | 2 | 0.000 | 10498.699 | 4 | 2 | 0.003 |
| 9 | 3 | 7 | 10498.704 | 5 | 4 | 0.004 | 10498.697 | 2 | 2 | 0.001 |
| 9 | 3 | 6 | 10556.321 | 1 | 2 | 0.004 |  |  |  |  |
| 9 | 4 | 6 | 10556.274 | 2 | 3 | 0.003 |  |  |  |  |
| 9 | 4 | 5 | 10604.288 | 3 | 3 | -0.013 | 10604.266* | 1 | 2 | -0.031 |
| 9 | 5 | 5 | 10603.508* | 4 | 4 | -0.034 |  |  |  |  |
| 9 | 5 | 4 | 10644.039 | 1 | 2 | 0.009 | 10644.042 | 2 | 3 | 0.013 |
| 9 | 6 | 4 | 10638.202 | 5 | 3 | 0.002 |  |  |  |  |
| 9 | 6 | 3 | 10660.007 | 2 | 2 | 0.002 | 10659.988 | 1 | 3 | -0.013 |
| 9 | 7 | 3 | 10719.415 | 1 | 2 | 0.002 |  |  |  |  |
| 9 | 7 | 2 | 10719.157 |  | 1 | 0.010 | 10719.132 | 4 | 2 | 0.016 |
| 9 | 8 | 2 | 10683.701* | 3 | 2 | -0.023 | 10683.731 |  | 1 | 0.004 |
| 9 | 8 | 1 | 10680.155 | 3 | 2 | 0.002 | 10680.181* | 2 | 3 | 0.028 |
| 9 | 9 | 1 | 10765.509 | 4 | 2 | 0.001 |  |  |  |  |
| 9 | 9 | 0 |  |  |  |  | 10765.516 |  | 1 | -0.005 |
| 10 | 0 | 10 | 10448.115 |  | 1 | 0.000 | 10448.103 |  | 1 | -0.006 |
| 10 | 1 | 10 | 10448.115 |  | 1 | 0.000 | 10448.103 |  | 1 | -0.006 |
| 10 | 1 | 9 | 10534.182 | 1 | 2 | 0.001 | 10534.173 | 6 | 2 | -0.003 |
| 10 | 2 | 9 | 10534.182 | 1 | 2 | 0.000 | 10534.173 | 6 | 2 | -0.003 |
| 10 | 2 | 8 | 10610.408 | 2 | 3 | 0.001 | 10610.403 | 2 | 2 | 0.001 |
| 10 | 3 | 8 | 10610.409 | 3 | 3 | 0.002 | 10610.403 | 2 | 2 | 0.000 |
| 10 | 3 | 7 | 10676.903 | 5 | 4 | 0.005 | 10676.897 | 2 | 3 | 0.009 |
| 10 | 4 | 7 | 10676.899 |  | 1 | 0.003 | 10676.898 | 2 | 2 | 0.011 |
| 10 | 4 | 6 | 10733.660 | 2 | 3 | 0.003 | 10733.662 |  | 1 | 0.008 |
| 10 | 5 | 6 | 10733.485 | 4 | 3 | 0.004 |  |  |  |  |
| 10 | 5 | 5 | 10780.946 | 3 | 2 | -0.009 |  |  |  |  |
| 10 | 6 | 5 | 10778.919 | 5 | 2 | -0.017 | 10778.918 |  | 1 | -0.014 |
| 10 | 6 | 4 | 10821.025 | 4 | 2 | -0.002 |  |  |  |  |
| 10 | 7 | 4 | 10810.037 | 1 | 2 | -0.017 | 10810.046 | 2 | 2 | -0.007 |
| 10 | 7 | 3 | 10832.656 | 3 | 3 | -0.013 | 10832.686 | 3 | 2 | 0.013 |
| 10 | 8 | 3 | 10904.297 |  | 1 | -0.003 | 10904.292 | 3 | 2 | -0.016 |
| 10 | 8 | 2 | 10904.172 | 1 | 2 | -0.010 |  |  |  |  |
| 10 | 9 | 2 | 10862.042 |  | 1 | 0.004 | 10862.044 | 3 | 2 | 0.002 |
| 10 | 9 | 1 | 10860.195 | 1 | 2 | -0.004 | 10860.197 |  | 1 | -0.005 |
| 10 | 10 | 1 | 10956.077 |  | 1 | 0.013 |  |  |  |  |
| 10 | 10 | 0 | 10956.066 |  | 1 | -0.001 |  |  |  |  |
| 11 | 0 | 11 | 10550.773 | 3 | 2 | 0.003 | 10550.761 |  | 1 | -0.004 |
| 11 | 1 | 11 | 10550.773 | 3 | 2 | 0.003 | 10550.761 |  | 1 | -0.004 |

Table 2 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 11 | 1 | 10 | 10645.813 | 2 | 2 | 0.002 | 10645.826 |  | 1 | 0.009 |
| 11 | 2 | 10 | 10645.813 | 2 | 2 | 0.002 | 10645.826 |  | 1 | 0.009 |
| 11 | 2 | 9 | 10730.920 | 1 | 2 | 0.006 | 10730.913 | 7 | 2 | 0.005 |
| 11 | 3 | 9 | 10730.920 | 1 | 2 | 0.007 | 10730.913 | 7 | 2 | 0.005 |
| 11 | 3 | 8 | 10806.226 | 2 | 2 | 0.001 | 10806.221 | 11 | 2 | 0.002 |
| 11 | 4 | 8 | 10806.232 | 2 | 4 | 0.006 | 10806.220 | 8 | 3 | 0.001 |
| 11 | 4 | 7 |  |  |  |  | 10871.779 | 5 | 3 | 0.017 |
| 11 | 5 | 7 | 10871.782 | 5 | 3 | -0.015 | 10871.807 | 1 | 2 | 0.006 |
| 11 | 5 | 6 | 10927.648 | 1 | 2 | 0.008 | 10927.651* |  | 1 | 0.019 |
| 11 | 6 | 6 | 10927.090 | 2 | 2 | 0.001 |  |  |  |  |
| 11 | 6 | 5 | 10974.500* | 3 | 2 | 0.024 |  |  |  |  |
| 11 | 7 | 5 | 10969.906 | 4 | 2 | 0.003 |  |  |  |  |
| 11 | 8 | 4 | 10998.440 | 6 | 2 | 0.003 |  |  |  |  |
| 11 | 8 | 3 | 11023.145 |  | 1 | 0.001 |  |  |  |  |
| 11 | 11 | 1 | 11165.486 |  | 1 | 0.000 |  |  |  |  |
| 11 | 11 | 0 | 11165.481 |  | 1 | -0.006 |  |  |  |  |
| 12 | 0 | 12 | 10662.269 |  | 1 | 0.000 | 10662.252 |  | 1 | -0.011 |
| 12 | 1 | 12 | 10662.269 |  | 1 | 0.000 | 10662.252 |  | 1 | -0.011 |
| 12 | 1 | 11 | 10766.269 |  | 1 | 0.003 | 10766.266 | 1 | 2 | -0.006 |
| 12 | 2 | 11 | 10766.269 |  | 1 | 0.003 | 10766.266 | 1 | 2 | -0.006 |
| 12 | 2 | 10 | 10860.203 | 3 | 3 | 0.003 | 10860.197 | 6 | 2 | 0.003 |
| 12 | 3 | 10 | 10860.203 | 4 | 3 | 0.003 | 10860.197 | 6 | 2 | 0.003 |
| 12 | 3 | 9 | 10944.288 | 5 | 2 | 0.007 | 10944.284 |  | 1 | 0.010 |
| 12 | 4 | 9 | 10944.284 | 1 | 2 | 0.002 | 10944.283 |  | 1 | 0.010 |
| 12 | 4 | 8 | 11018.629 | 3 | 2 | 0.011 | 11018.629 |  | 1 | 0.011 |
| 12 | 5 | 8 | 11018.629 |  | 1 | -0.001 | 11018.632 |  | 1 | 0.002 |
| 12 | 5 | 7 | 11083.106* |  | 1 | 0.028 |  |  |  |  |
| 12 | 6 | 7 |  |  |  |  | 11083.229 |  | 1 | -0.017 |
| 12 | 8 | 4 | 11229.155 | 4 | 2 | -0.007 |  |  |  |  |
| 13 | 0 | 13 | 10782.595 | 2 | 2 | 0.002 | 10782.587 |  | 1 | 0.002 |
| 13 | 1 | 13 | 10782.595 | 2 | 2 | 0.002 | 10782.587 |  | 1 | 0.002 |
| 13 | 1 | 12 | 10895.527 | 1 | 2 | -0.004 | 10895.521 | 3 | 2 | -0.001 |
| 13 | 2 | 12 | 10895.527 | 1 | 2 | -0.004 | 10895.521 | 3 | 2 | -0.001 |
| 13 | 2 | 11 | 10998.257 |  | 1 | 0.001 | 10998.248 |  | 1 | 0.003 |
| 13 | 3 | 11 | 10998.257 | 1 | 2 | 0.001 | 10998.248 |  | 1 | 0.003 |
| 13 | 3 | 10 | 11091.062 | 1 | 2 | 0.001 | 11091.048 | 2 | 2 | -0.001 |
| 13 | 4 | 10 | 11091.061 | 1 | 2 | 0.000 | 11091.048 | 2 | 2 | -0.001 |
| 13 | 4 | 9 |  |  |  |  | 11174.131 |  | 1 | -0.018 |
| 13 | 5 | 9 | 11174.131* |  | 1 | -0.018 |  |  |  |  |
| 13 | 5 | 8 |  |  |  |  | 11247.607 |  | 1 | -0.003 |
| 13 | 6 | 8 | 11247.607 |  | 1 | 0.003 |  |  |  |  |
| 13 | 7 | 7 | 11311.458 |  | 1 | 0.006 |  |  |  |  |
| 14 | 0 | 14 | 10911.723 |  | 1 | 0.002 | 10911.707 |  | 1 | -0.004 |
| 14 | 1 | 14 | 10911.723 |  | 1 | 0.002 | 10911.707 |  | 1 | -0.004 |
| 14 | 1 | 13 | 11033.569 | 7 | 2 | -0.002 | 11033.555 | 3 | 2 | -0.004 |
| 14 | 2 | 13 | 11033.569 | 7 | 2 | -0.002 | 11033.555 | 3 | 2 | -0.004 |
| 14 | 2 | 12 | 11145.044 |  | 1 | 0.002 | 11145.044 |  | 1 | -0.014 |
| 14 | 3 | 12 | 11145.044 |  | 1 | 0.002 | 11145.044 |  | 1 | -0.014 |
| 14 | 3 | 11 | 11246.528 | 7 | 2 | -0.008 |  |  |  |  |
| 14 | 4 | 11 | 11246.528 | 6 | 2 | -0.008 |  |  |  |  |
| 15 | 0 | 15 | 11049.636 |  | 1 | 0.006 | 11049.616 |  | 1 | -0.001 |
| 15 | 1 | 15 | 11049.636 |  | 1 | 0.006 | 11049.616 |  | 1 | -0.001 |
| 15 | 1 | 14 | 11180.371 |  | 1 | 0.002 | 11180.361 |  | 1 | 0.009 |
| 15 | 2 | 14 | 11180.366 | 5 | 2 | -0.003 | 11180.361 |  | 1 | 0.009 |
| 15 | 2 | 13 | 11300.589 |  | 1 | 0.000 |  |  |  |  |
| 15 | 3 | 13 | 11300.589 |  | 1 | 0.000 |  |  |  |  |
| 16 | 0 | 16 | 11196.324* |  | 1 | 0.030 | 11196.278 |  | 1 | -0.002 |
| 16 | 1 | 16 | 11196.324* |  | 1 | 0.030 | 11196.278 |  | 1 | -0.002 |
| 16 | 1 | 15 | 11335.899 |  | 1 | 0.000 | 11335.873 |  | 1 | -0.002 |
| 16 | 2 | 15 | 11335.899 |  | 1 | 0.000 | 11335.873 |  | 1 | -0.002 |
| 17 | 0 | 17 |  |  |  |  | 11351.690 |  | 1 | 0.001 |

Table 2 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 17 | 1 | 17 |  |  |  |  | 11351.690 |  | 1 | 0.001 |
| 18 | 0 | 18 |  |  |  |  | 11515.753 |  | 1 | -0.009 |
| 18 | 1 | 18 |  |  |  |  | 11515.753 |  | 1 | -0.009 |

Note. Asterisks denote the energy levels not included in the fit. $\sigma$ denotes the experimental uncertainty of the level in $10^{-3} \mathrm{~cm}^{-1} . N$ is the number of observed transitions used to calculate the upper energy level. $\Delta$ is the difference between the experimental and calculated values of the energy in $\mathrm{cm}^{-1}$.

Table 3
Rotational energy levels $\left(\mathrm{cm}^{-1}\right)$ of the $\left(30^{-}, 2\right),\left(30^{+}, 2\right),\left(20^{-}, 4\right)$, and $\left(11^{+}, 4\right)$ vibrational states of $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$

| $J$ | $K_{a}$ | $K_{c}$ | $\left(30^{-}, 2\right)$ |  |  |  | $\left(30^{+}, 2\right)$ |  |  |  | $\left(20^{-}, 4\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 0 | 0 | 0 | 9806.667 |  | 1 | 0.006 | 9806.733 |  | 1 | -0.004 | 9647.167 |  | 1 | 0.000 |
| 1 | 0 | 1 | 9820.091 | 6 | 2 | 0.002 | 9820.170* |  | 1 | 0.022 | 9661.231 | 1 | 2 | -0.001 |
| 1 | 1 | 1 | 9821.725 |  | 1 | -0.001 | 9821.788 | 1 | 2 | -0.003 | 9663.144 |  | 1 | 0.005 |
| 1 | 1 | 0 | 9826.305 | 5 | 2 | 0.003 | 9826.377 | 3 | 2 | -0.003 | 9668.445 | 7 | 2 | -0.003 |
| 2 | 0 | 2 | 9843.620 | 1 | 3 | -0.003 | 9843.652 | 1 | 2 | 0.005 | 9685.478 | 4 | 2 | 0.007 |
| 2 | 1 | 2 | 9844.003 | 1 | 2 | 0.001 | 9844.027 | 2 | 3 | -0.001 | 9685.746 | 5 | 3 | -0.009 |
| 2 | 1 | 1 | 9857.712 | 4 | 3 | -0.005 | 9857.775 |  | 1 | 0.000 | 9701.876 | 2 | 3 | -0.004 |
| 2 | 2 | 1 | 9862.618 | 3 | 2 | 0.004 | 9862.683 | 1 | 2 | -0.004 | 9707.542 | 3 | 3 | 0.004 |
| 2 | 2 | 0 | 9865.911 | 3 | 3 | -0.001 | 9865.998 |  | 1 | 0.002 | 9711.353 | 1 | 2 | -0.013 |
| 3 | 0 | 3 | 9875.631 |  | 1 | 0.002 | 9875.711 |  | 1 | -0.010 | 9717.997 | 8 | 3 | 0.006 |
| 3 | 1 | 3 | 9875.620 | 1 | 3 | -0.001 | 9875.709 |  | 1 | -0.005 | 9718.013 | 5 | 2 | -0.012 |
| 3 | 1 | 2 | 9901.112 | 1 | 2 | -0.004 | 9901.148 | 2 | 3 | 0.006 | 9747.660 | 6 | 3 | 0.001 |
| 3 | 2 | 2 | 9902.863 | 1 | 4 | -0.001 | 9902.887 | 3 | 2 | -0.007 | 9749.772 | 5 | 3 | 0.006 |
| 3 | 2 | 1 | 9914.341 | 2 | 3 | 0.001 | 9914.401 | 3 | 3 | 0.003 | 9763.031 |  | 1 | 0.004 |
| 3 | 3 | 1 | 9924.051 | 1 | 2 | 0.006 | 9924.130 | 1 | 2 | 0.004 | 9774.186 | 1 | 3 | -0.004 |
| 3 | 3 | 0 | 9926.041 | 1 | 3 | 0.007 | 9926.123 | 1 | 2 | 0.000 | 9776.498 | 1 | 2 | -0.003 |
| 4 | 0 | 4 | 9916.301 | 1 | 4 | -0.003 | 9916.375 |  | 1 | -0.001 | 9759.061 | 6 | 3 | 0.001 |
| 4 | 1 | 4 | 9916.298 | 1 | 3 | -0.001 | 9916.374 |  | 1 | 0.003 | 9759.058 |  | 1 | -0.005 |
| 4 | 1 | 3 | 9953.156 | 2 | 4 | -0.002 | 9953.557 |  | 1 | 0.007 | 9801.918 | 2 | 3 | 0.005 |
| 4 | 2 | 3 | 9953.148 | 3 | 2 | 0.001 | 9953.537 | 3 | 3 | -0.003 | 9802.102 | 2 | 3 | 0.006 |
| 4 | 2 | 2 | 9976.809 | 4 | 3 | 0.000 | 9976.845 | 2 | 2 | 0.009 | 9829.370 | 2 | 2 | -0.002 |
| 4 | 3 | 2 | 9981.477 | 1 | 3 | 0.001 | 9981.503 | 2 | 3 | -0.007 | 9834.864 | 4 | 3 | -0.005 |
| 4 | 3 | 1 | 9990.254 | 3 | 5 | 0.001 | 9990.319 | 3 | 2 | 0.006 | 9844.992 | 1 | 2 | 0.010 |
| 4 | 4 | 1 | 10006.065 | 2 | 2 | 0.002 | 10006.147 | 7 | 2 | -0.005 | 9863.071 |  | 1 | 0.005 |
| 4 | 4 | 0 | 10007.095 | 5 | 2 | 0.005 | 10007.185 |  | 1 | 0.000 | 9864.270 | 4 | 3 | 0.003 |
| 5 | 0 | 5 | 9965.780 | 2 | 3 | -0.007 | 9965.854 |  | 1 | -0.004 | 9808.824 | 4 | 2 | 0.008 |
| 5 | 1 | 5 | 9965.782 | 2 | 3 | -0.004 | 9965.854 |  | 1 | -0.003 | 9808.817 | 3 | 2 | 0.003 |
| 5 | 1 | 4 | 10013.453 | 3 | 3 | 0.004 | 10013.552 | 2 | 2 | 0.000 | 9864.182 | 6 | 2 | -0.010 |
| 5 | 2 | 4 | 10013.431 | 2 | 4 | 0.008 | 10013.535 | 1 | 2 | 0.009 | 9864.205 | 4 | 3 | 0.002 |
| 5 | 2 | 3 | 10050.533 | 6 | 3 | 0.001 | 10050.555 | 5 | 4 | 0.007 | 9905.505 | 17 | 2 | 0.000 |
| 5 | 3 | 3 | 10049.108 | 4 | 4 | 0.010 | 10049.104 | 5 | 3 | -0.001 | 9907.246 | 1 | 3 | -0.002 |
| 5 | 3 | 2 | 10070.627 | 5 | 4 | -0.001 | 10070.660 | 2 | 3 | 0.003 | 9930.482 | 1 | 2 | -0.008 |
| 5 | 4 | 2 | 10079.937 | 4 | 4 | 0.001 | 10079.967 |  | 1 | 0.006 | 9941.365 |  | 1 | 0.003 |
| 5 | 4 | 1 | 10085.925 | 1 | 2 | -0.001 | 10085.987 |  | 1 | 0.004 | 9948.243 |  | 1 | 0.000 |
| 5 | 5 | 1 | 10108.644 | 5 | 2 | -0.001 | 10108.745 |  | 1 | 0.003 | 9974.044 | 2 | 2 | 0.004 |
| 5 | 5 | 0 | 10109.123 | 4 | 2 | -0.009 | 10109.224 | 3 | 4 | -0.005 | 9974.600 |  | 1 | -0.005 |
| 6 | 0 | 6 | 10024.085 | 5 | 3 | -0.001 | 10024.162 |  | 1 | 0.008 | 9867.271 |  | 1 | 0.002 |
| 6 | 1 | 6 | 10024.082 | 5 | 3 | -0.003 | 10024.162 |  | 1 | 0.008 | 9867.272 |  | 1 | 0.003 |
| 6 | 1 | 5 | 10082.364 | 4 | 4 | -0.001 | 10082.442 | 1 | 2 | -0.007 | 9934.997 | 3 | 3 | -0.006 |
| 6 | 2 | 5 | 10082.356 | 7 | 3 | -0.001 | 10082.441 | 1 | 3 | -0.001 | 9935.000 |  | 1 | 0.001 |
| 6 | 2 | 4 | 10129.538 | 2 | 4 | -0.003 | 10129.576 | 4 | 2 | -0.003 | 9989.325 | 2 | 3 | -0.013 |
| 6 | 3 | 4 | 10129.208 | 1 | 2 | -0.001 | 10129.248 | 4 | 3 | -0.001 | 9989.403 | 1 | 2 | 0.020 |
| 6 | 3 | 3 | 10166.634 | 4 | 3 | -0.003 | 10166.606 | 2 | 3 | -0.005 | 10028.073 | 3 | 2 | -0.005 |
| 6 | 4 | 3 | 10162.832 | 3 | 2 | -0.002 | 10162.835 | 5 | 3 | 0.000 |  |  |  |  |
| 6 | 4 | 2 | 10182.841 | 5 | 3 | 0.003 | 10182.874 |  | 1 | 0.001 | 10051.274 | 1 | 2 | -0.004 |
| 6 | 5 | 2 | 10198.212 |  | 1 | 0.007 | 10198.320 | 4 | 2 | 0.001 | 10069.239 |  | 1 | -0.003 |
| 6 | 5 | 1 | 10201.691 | 1 | 2 | -0.006 | 10201.956 | 6 | 2 | -0.001 | 10073.394 | 10 | 4 | 0.012 |
| 6 | 6 | 1 | 10231.668 | 1 | 2 | -0.008 | 10231.791 | 1 | 2 | -0.003 |  |  |  |  |
| 6 | 6 | 0 | 10231.879 | 6 | 3 | -0.004 | 10232.005 |  | 1 | 0.002 | 10107.105 | 3 | 2 | -0.010 |

Table 3 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(30^{-}, 2\right)$ |  |  |  | $\left(30^{+}, 2\right)$ |  |  |  | $\left(20^{-}, 4\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 7 | 0 | 7 | 10091.194 | 3 | 2 | -0.005 | 10091.260 |  | 1 | -0.002 | 9934.411 | 6 | 2 | -0.007 |
| 7 | 1 | 7 | 10091.193 | 3 | 2 | -0.005 | 10091.260 |  | 1 | -0.002 | 9934.411 | 6 | 2 | -0.007 |
| 7 | 1 | 6 | 10160.061 | 5 | 3 | -0.005 | 10160.156 | 4 | 3 | 0.004 | 10014.489 | 5 | 3 | -0.002 |
| 7 | 2 | 6 | 10160.064 | 2 | 3 | -0.001 | 10160.153 | 5 | 3 | 0.003 | 10014.489 | 8 | 4 | 0.000 |
| 7 | 2 | 5 | 10217.597 | 7 | 2 | 0.008 | 10217.705 | 3 | 2 | -0.001 | 10081.056 | 1 | 2 | -0.002 |
| 7 | 3 | 5 | 10217.540 | 4 | 3 | -0.014 | 10217.643* |  | 1 | -0.026 | 10081.052 | 2 | 3 | 0.013 |
| 7 | 3 | 4 | 10264.198 |  | 1 | -0.005 | 10264.239 | 4 | 3 | -0.003 |  |  |  |  |
| 7 | 4 | 4 | 10263.128 | 4 | 4 | 0.006 | 10263.166 | 3 | 4 | 0.008 | 10133.847 | 4 | 2 | -0.007 |
| 7 | 4 | 3 | 10302.100 | 4 | 4 | -0.014 | 10293.921 | 2 | 2 | -0.003 | 10169.006 | 3 | 2 | 0.000 |
| 7 | 5 | 3 | 10302.089 | 5 | 2 | -0.009 | 10293.932 | 6 | 3 | 0.009 | 10178.169 | 8 | 2 | 0.004 |
| 7 | 5 | 2 | 10313.629 | 1 | 4 | -0.012 | 10313.917 | 3 | 2 | -0.011 |  |  |  |  |
| 7 | 6 | 2 | 10336.485 | 2 | 4 | 0.001 | 10336.605 | 3 | 2 | 0.004 | 10218.430 | 2 | 2 | 0.003 |
| 7 | 6 | 1 |  |  |  |  | 10338.579 |  | 1 | 0.003 | 10220.700 |  | 1 | 0.004 |
| 7 | 7 | 1 | 10375.035 | 8 | 3 | 0.005 | 10375.207 | 4 | 3 | 0.005 | 10261.103 | 3 | 2 | -0.001 |
| 7 | 7 | 0 | 10375.039 | 6 | 3 | -0.002 | 10375.230 | 4 | 2 | -0.005 | 10261.218* |  | 1 | -0.035 |
| 8 | 0 | 8 | 10167.082 | 4 | 3 | 0.006 | 10167.152 |  | 1 | 0.006 | 10010.267 | 6 | 2 | 0.011 |
| 8 | 1 | 8 | 10167.082 | 4 | 3 | 0.006 | 10167.152 |  | 1 | 0.006 | 10010.267 | 6 | 2 | 0.011 |
| 8 | 1 | 7 | 10246.316 | 5 | 4 | -0.001 | 10247.070* | 3 | 2 | 0.027 | 10102.660 |  | 1 | -0.019 |
| 8 | 2 | 7 | 10246.315 | 4 | 3 | -0.008 | 10247.070 | 3 | 2 | 0.001 | 10102.662 |  | 1 | -0.017 |
| 8 | 2 | 6 | 10314.548 | 4 | 3 | -0.005 | 10314.647 | 9 | 2 | -0.011 | 10181.325 | 4 | 3 | -0.002 |
| 8 | 3 | 6 | 10314.540 | 6 | 3 | 0.001 | 10314.647 | 10 | 2 | -0.001 | 10181.322 |  | 1 | 0.005 |
| 8 | 3 | 5 | 10371.262 |  | 1 | -0.005 | 10371.335 |  | 1 | -0.010 | 10246.073 | 5 | 2 | 0.001 |
| 8 | 4 | 5 | 10370.968 | 2 | 2 | -0.008 | 10371.059 | 3 | 3 | 0.002 |  |  |  |  |
| 8 | 4 | 4 | 10417.375 | 5 | 3 | 0.007 | 10417.413 |  | 1 | -0.004 | 10296.605 |  | 1 | 0.006 |
| 8 | 5 | 4 | 10414.430 | 1 | 2 | -0.001 | 10414.506 | 3 | 2 | 0.000 |  |  |  |  |
| 8 | 5 | 3 | 10441.828 | 6 | 4 | 0.007 | 10456.279 |  | 1 | 0.010 | 10328.284 |  | 1 | 0.008 |
| 8 | 6 | 3 | 10442.327* |  | 1 | -0.041 | 10456.353 | 6 | 2 | 0.003 |  |  |  |  |
| 8 | 6 | 2 | 10464.224 | 2 | 3 | 0.009 | 10464.441 |  | 1 | -0.011 | 10353.912 | 3 | 2 | -0.017 |
| 8 | 7 | 2 | 10494.648 | 3 | 2 | 0.019 | 10494.917 |  | 1 | 0.005 |  |  |  |  |
| 8 | 7 | 1 | 10495.554 | 3 | 2 | 0.002 | 10495.880 |  | 1 | -0.002 |  |  |  |  |
| 8 | 8 | 1 | 10538.246 |  | 1 | 0.007 | 10538.718 |  | 1 | -0.002 | 10436.449* |  | 1 | -0.017 |
| 8 | 8 | 0 | 10538.275 | 4 | 2 | 0.001 | 10538.758 |  | 1 | 0.001 | 10436.452 |  | 1 | 0.003 |
| 9 | 0 | 9 | 10251.765 | 6 | 3 | -0.002 | 10251.833 |  | 1 | -0.003 | 10094.725 |  | 1 | 0.000 |
| 9 | 1 | 9 | 10251.765 | 6 | 3 | -0.002 | 10251.833 |  | 1 | -0.003 | 10094.725 |  | 1 | 0.000 |
| 9 | 1 | 8 | 10341.786 | 6 | 3 | 0.009 | 10341.876 | 7 | 2 | -0.001 | 10199.581 |  | 1 | 0.005 |
| 9 | 2 | 8 | 10341.785 | 5 | 3 | 0.009 | 10341.876 | 7 | 2 | -0.001 | 10199.581 |  | 1 | 0.005 |
| 9 | 2 | 7 | 10420.119 | 3 | 2 | 0.000 | 10420.252 |  | 1 | -0.008 | 10290.222 | 5 | 3 | 0.002 |
| 9 | 3 | 7 | 10420.117 | 1 | 2 | 0.008 | 10420.252 |  | 1 | -0.001 | 10290.225 | 6 | 3 | 0.008 |
| 9 | 3 | 6 |  |  |  |  | 10487.574 | 5 | 2 | 0.002 |  |  |  |  |
| 9 | 4 | 6 | 10487.204 | 2 | 3 | -0.009 |  |  |  |  | 10367.257 |  | 1 | -0.004 |
| 9 | 4 | 5 | 10543.013 | 4 | 2 | 0.006 | 10543.164* |  | 1 | -0.042 |  |  |  |  |
| 9 | $5$ | 5 | 10542.106 | 2 | 2 | -0.001 |  |  |  |  |  |  |  |  |
|  | 5 | 4 |  |  |  |  | 10589.106 |  | 1 | 0.009 |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 9 | 6 | 4 | 10582.619 | 5 | 3 | 0.006 |  |  |  |  |  |  |  |  |
| 9 | 7 | 2 | 10634.719 |  | 1 | -0.011 | 10633.933 |  | 1 | 0.009 |  |  |  |  |
| 9 | 8 | 2 | 10672.409 | 1 | 2 | -0.014 |  |  |  |  |  |  |  |  |
| 9 | 8 | 1 |  |  |  |  | 10629.653 | 2 | 2 | -0.005 |  |  |  |  |
| 9 | 9 | 1 | 10721.339 | 2 | 2 | -0.003 |  |  |  |  |  |  |  |  |
| 10 | 0 | 10 | 10345.225 | 4 | 3 | -0.003 | 10345.294 |  | 1 | -0.004 | 10187.960 |  | 1 | -0.005 |
| 10 | 1 | 10 | 10345.225 | 4 | 3 | -0.003 | 10345.294 |  | 1 | -0.004 | 10187.960 |  | 1 | -0.005 |
| 10 | 1 | 9 | 10445.812 | 3 | 3 | 0.004 | 10445.915 | 6 | 2 | 0.004 |  |  |  |  |
| 10 | 2 | 9 | 10445.812 | 3 | 3 | 0.004 | 10445.915 | 6 | 2 | 0.004 |  |  |  |  |
| 10 | 2 | 8 | 10534.532 | 4 | 2 | -0.008 | 10534.802* | 5 | 2 | 0.100 |  |  |  |  |
| 10 | 3 | 8 | 10534.532 | 5 | 2 | -0.006 | 10534.802* | 5 | 2 | 0.101 |  |  |  |  |
| 10 | 3 | 7 | 10611.683 | 4 | 2 | -0.011 |  |  |  |  | 10496.560 |  | 1 | 0.005 |
| 10 | 4 | 7 | 10611.676 | 5 | 2 | 0.005 |  |  |  |  | 10496.547 |  | 1 | 0.006 |
| 10 | 4 | 6 | 10677.355* | 2 | 2 | -0.083 |  |  |  |  |  |  |  |  |
| 10 | 6 | 5 |  |  |  |  | 10729.369 | 3 | 2 | -0.007 |  |  |  |  |
| 10 | 6 | 4 | 10778.665 | 5 | 2 | -0.002 |  |  |  |  |  |  |  |  |
| 10 | 7 | 3 | 10793.028 | 1 | 2 | 0.002 |  |  |  |  |  |  |  |  |
| 10 | 8 | 3 |  |  |  |  | 10870.058 | 7 | 2 | 0.005 |  |  |  |  |

Table 3 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(30^{-}, 2\right)$ |  |  |  | $\left(30^{+}, 2\right)$ |  |  |  | $\left(20^{-}, 4\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 10 | 10 | 1 | 10923.682 |  | 1 | 0.008 |  |  |  |  |  |  |  |  |
| 10 | 10 | 0 | 10923.669 | 1 | 2 | -0.009 |  |  |  |  |  |  |  |  |
| 11 | 0 | 11 | 10447.448 | 5 | 2 | -0.002 | 10447.516 |  | 1 | -0.004 | 10289.814 |  | 1 | 0.001 |
| 11 | 1 | 11 | 10447.448 | 5 | 2 | -0.002 | 10447.516 |  | 1 | -0.004 | 10289.814 |  | 1 | 0.001 |
| 11 | 1 | 10 | 10558.602 | 4 | 3 | 0.005 | 10558.707 | 6 | 2 | 0.006 | 10419.529 |  | 1 | 0.006 |
| 11 | 2 | 10 | 10558.602 | 4 | 3 | 0.005 | 10558.707 | 6 | 2 | 0.006 | 10419.529 |  | 1 | 0.006 |
| 11 | 2 | 9 | 10657.725* | 5 | 2 | 0.068 | 10657.857 | 7 | 2 | 0.005 | 10534.032 |  | 1 | -0.009 |
| 11 | 3 | 9 | 10657.724* | 4 | 2 | 0.067 | 10657.857 | 8 | 2 | 0.005 | 10534.032 |  | 1 | -0.009 |
| 11 | 3 | 8 | 10744.948* |  | 1 | -0.045 |  |  |  |  |  |  |  |  |
| 11 | 4 | 8 | 10744.950* | 1 | 2 | -0.039 |  |  |  |  |  |  |  |  |
| 11 | 5 | 7 | 10820.744 | 6 | 2 | 0.002 |  |  |  |  |  |  |  |  |
| 12 | 0 | 12 | 10558.423 | 4 | 2 | 0.005 | 10558.496 | 6 | 2 | 0.005 |  |  |  |  |
| 12 | 1 | 12 | 10558.423 | 4 | 2 | 0.005 | 10558.496 | 6 | 2 | 0.005 |  |  |  |  |
| 12 | 1 | 11 | 10680.136 | 4 | 3 | 0.002 | 10680.241 |  | 1 | 0.000 |  |  |  |  |
| 12 | 2 | 11 | 10680.136 | 4 | 3 | 0.002 | 10680.241 |  | 1 | 0.000 |  |  |  |  |
| 12 | 2 | 10 | 10789.516* | 4 | 2 | 0.027 | 10789.704* |  | 1 | -0.033 | 10669.008 |  | 1 | 0.001 |
| 12 | 3 | 10 | 10789.516* | 4 | 2 | 0.027 | 10789.704* |  | 1 | -0.033 | 10669.008 |  | 1 | 0.001 |
| 13 | 0 | 13 | 10678.123 | 1 | 2 | 0.004 | 10678.192 |  | 1 | 0.000 |  |  |  |  |
| 13 | 1 | 13 | 10678.123 | 1 | 2 | 0.004 | 10678.192 |  | 1 | 0.000 |  |  |  |  |
| 13 | 1 | 12 | 10810.402 | 2 | 2 | -0.006 | 10810.520 |  | 1 | -0.001 |  |  |  |  |
| 13 | 2 | 12 | 10810.402 | 2 | 2 | -0.006 | 10810.520 |  | 1 | -0.001 |  |  |  |  |
| 13 | 2 | 11 | 10930.035 | 6 | 2 | 0.001 |  |  |  |  |  |  |  |  |
| 13 | 3 | 11 | 10930.035 | 5 | 3 | 0.000 |  |  |  |  |  |  |  |  |
| 14 | 0 | 14 | 10806.530 |  | 1 | -0.005 | 10806.604 |  | 1 | -0.004 |  |  |  |  |
| 14 | 1 | 14 | 10806.530 |  | 1 | -0.005 | 10806.604 |  | 1 | -0.004 |  |  |  |  |
| 14 | 1 | 13 | 10949.407 |  | 1 | 0.002 |  |  |  |  |  |  |  |  |
| 14 | 2 | 13 | 10949.407 |  | 1 | 0.002 |  |  |  |  |  |  |  |  |
| 14 | 2 | 12 |  |  |  |  | 11079.799 |  | 1 | -0.001 |  |  |  |  |
| 14 | 3 | 12 |  |  |  |  | 11079.799 |  | 1 | -0.001 |  |  |  |  |
| 15 | 0 | 15 | 10943.648 |  | 1 | -0.001 | 10943.727 |  | 1 | 0.003 |  |  |  |  |
| 15 | 1 | 15 | 10943.648 |  | 1 | -0.001 | 10943.727 |  | 1 | 0.003 |  |  |  |  |
|  |  |  | $\left(11^{+}, 4\right)$ |  |  |  |  |  |  |  |  |  |  |  |
| 8 | 6 | 3 | 10444.693 | 5 | 2 | -0.004 |  |  |  |  |  |  |  |  |
| 9 | 7 | 2 | 10637.662 | 1 | 2 | -0.004 |  |  |  |  |  |  |  |  |

Note. Asterisks denote the energy levels not included in the fit. $\sigma$ denotes the experimental uncertainty of the level in $10^{-3} \mathrm{~cm}^{-1} . N$ is the number of observed transitions used to calculate the upper energy level. $\Delta$ is the difference between the experimental and calculated values of the energy in $\mathrm{cm}^{-1}$.

$$
\begin{align*}
H^{C}= & C_{x z}\left\{J_{x}, J_{z}\right\}+C_{x z j}\left\{J_{x}, J_{z}\right\} J^{2}+C_{x z j j}\left\{J_{x}, J_{z}\right\} J^{4} \\
& +C_{x z k j}\left\{J_{x}, J_{z}^{3}\right\} J^{2}+C_{y k}\left\{\mathrm{i} J_{y}, J_{z}^{2}\right\}+\cdots \tag{2}
\end{align*}
$$

with $\{A, B\}=A B+B A$ and $J_{x y}^{2}=J_{x}^{2}-J_{y}^{2}$.
The considered vibrational states belong to the first pentadecade of interacting states, if we follow the conventional polyad structure for water-like molecules. Among the fifteen vibrational states included in this pentadecade, nine are located in the analyzed spectral region and could contribute to the observed spectrum. They are the $\left(20^{-}, 4\right),\left(20^{+}, 4\right),\left(11^{+}, 4\right),\left(30^{-}, 2\right)$, $\left(30^{+}, 2\right),\left(40^{-}, 0\right),\left(40^{+}, 0\right),\left(21^{+}, 2\right)$, and $\left(21^{-}, 2\right)$ states with vibrational energies predicted [10] at 9646.814, 9647.248, 9745.777, 9806.461, 9806.574, 9911.043, $9911.059,9993.438$, and $10004.541 \mathrm{~cm}^{-1}$, respectively. Preliminary calculations performed with rotational parameters estimated from lower vibrational states [10] have shown that the $\left(11^{+}, 4\right)$ and $\left(20^{+}, 4\right)$ dark states should be included into consideration since they perturb
significantly some of the experimentally observed states (see below). On the other hand, the $\left(21^{+}, 2\right)$ and $\left(21^{-}, 2\right)$ states, though being only 82 and $93 \mathrm{~cm}^{-1}$ higher in energy than the $\left(40^{ \pm}, 0\right)$ bright states, have higher bending excitation leading to a rapid detuning of the rotational levels compared to those of the $\left(40^{ \pm}, 0\right)$ LM pair. In consequence, these two states were not included in the effective Hamiltonian model and only the subset of seven states listed in Table 1 was considered. They consist in three nearly local mode pairs- $\left(20^{ \pm}, 4\right),\left(30^{ \pm}, 2\right)$, $\left(40^{ \pm}, 0\right)$-and the $\left(11^{+}, 4\right)$ separate state.

As previously studied experimentally and theoretically (see [9] and references quoted therein), at the local mode limit, the rotational structure is predicted to be identical for the two components of a LM pair, the Coriolis resonance parameter $C_{y}$ between the two components vanishes and, in case of interaction between two LM pairs, similar resonance parameters should be identical. In the present case, no one of the studied LM pairs could be considered as a strict LM pair: the

Table 4
Vibrational energies and rotational and coupling constants for the $\left(40^{ \pm}, 0\right),\left(30^{ \pm}, 2\right),\left(20^{ \pm}, 4\right)$, and $\left(11^{+}, 4\right)$ vibrational states of $\mathrm{H}_{2}{ }^{32} \mathrm{~S}, \mathrm{H}_{2}{ }^{33} \mathrm{~S}$, and $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$.
$\mathrm{H}_{2}{ }^{32} \mathrm{~S}: 683$ energy levels ( 654 included in the fit), 84 adjusted parameters ( 30 resonance and 54 diagonal), rms: $0.0061 \mathrm{~cm}^{-1}$

| $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ | $\left(40^{-}, 0\right)$ | $\left(40^{+}, 0\right)$ | $\left(30^{-}, 2\right)$ | $\left(30^{+}, 2\right)$ | $\left(20^{-}, 4\right)$ | $\left(20^{+}, 4\right)$ | $\left(11^{+}, 4\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $E_{v}$ | 9911.023710(2100) | 9911.0194490(9200) | 9806.660901(2400) | 9806.737202(2500) | 9647.167216(3000) | 9647.77480(2500) | 9744.88812(2900) |
| $A$ | 9.667 | 56(3100) | 10.4778561(5700) | 10.4819222(5500) | 11.5291843(9400) | $11.622228(2200)$ | 11.565604(2600) |
| $B$ | 8.563 | 3(1100) | 9.1670864(3900) | $9.1654446(4400)$ | 9. 7602913(9400) | 9.737 | 9.769 |
| C | 4.4760 | 22(4200) | 4.41872748 (7500) | 4. $418111085(8000)$ | 4.3549973 (2200) | $4.3447418(2600)$ | 4.395 |
| $\Delta_{k}$ | 3.38237 | 00) $\times 10^{-3}$ | $5.49316(1300) \times 10^{-3}$ | $5.684617(1500) \times 10^{-3}$ | $6.6638(1400) \times 10^{-3}$ | $9.40 \times 10^{-3}$ | 7.7093(1000) $\times 10^{-3}$ |
| $\Delta_{j k}$ | -1.22039 | (3800) $\times 10^{-3}$ | $-3.47217(1000) \times 10^{-3}$ | $-3.47785(1100) \times 10^{-3}$ | $-3.66514(7700) \times 10^{-3}$ | $-4.84 \times 10^{-3}$ | $-3.90911(5700) \times 10^{-3}$ |
| $\Delta_{j}$ | 3.392678 | (1900) $\times 10^{-4}$ | $8.849960(5900) \times 10^{-4}$ | $8.698304(6700) \times 10^{-4}$ | $1.24315(1000) \times 10^{-3}$ | $1.22 \times 10^{-3}$ | $1.22 \times 10^{-3}$ |
| $\delta_{k}$ | -1.14213 | 900) $\times 10^{-4}$ |  |  | $1.24679(3200) \times 10^{-3}$ | $5.53 \times 10^{-4}$ | $5.53 \times 10^{-4}$ |
| $\delta_{j}$ | 1.341842 | 300) $\times 10^{-4}$ | $4.127841(3400) \times 10^{-4}$ | $4.052017(3500) \times 10^{-4}$ | $5.84446(2900) \times 10^{-4}$ | $5.80 \times 10^{-4}$ | $5.80 \times 10^{-4}$ |
| $H_{k}$ | 1.12309 | 00) $\times 10^{-6}$ | $2.2604(1100) \times 10^{-6}$ | $5.6113(1100) \times 10^{-6}$ | $2.01611(3500) \times 10^{-5}$ | $1.70 \times 10^{-5}$ | $1.70 \times 10^{-5}$ |
| $H_{k j}$ |  | $\times 10^{-6}$ | $-2.84 \times 10^{-8}$ | $-2.84 \times 10^{-8}$ | $-2.13 \times 10^{-6}$ | $-2.13 \times 10^{-6}$ | $-2.13 \times 10^{-6}$ |
| $H_{j k}$ | -1.4 | $\times 10^{-6}$ | $-1.78082(6200) \times 10^{-6}$ | $-2.61153(5600) \times 10^{-6}$ | $-3.22 \times 10^{-6}$ | $-3.22 \times 10^{-6}$ | $-3.22 \times 10^{-6}$ |
| $H_{j}$ |  | $\times 10^{-7}$ | $5.29 \times 10^{-7}$ | $5.29 \times 10^{-7}$ | $8.1019(2500) \times 10^{-7}$ | $8.86 \times 10^{-7}$ | $8.86 \times 10^{-7}$ |
| $h_{k}$ | 1.92339 | 00) $\times 10^{-6}$ | $3.3728(1000) \times 10^{-6}$ | $3.27(1000) \times 10^{-6}$ | $1.47572(2500) \times 10^{-5}$ | $7.78 \times 10^{-6}$ | $7.78 \times 10^{-6}$ |
| $h_{k j}$ |  | $\times 10^{-7}$ | $-7.3702(3200) \times 10^{-7}$ | $-7.22(3200) \times 10^{-7}$ | $-3.1664(1100) \times 10^{-6}$ | $-1.30 \times 10^{-6}$ | $-1.30 \times 10^{-6}$ |
| $h_{j}$ |  | $\times 10^{-7}$ | $2.65 \times 10^{-7}$ | $2.65 \times 10^{-7}$ | $4.41 \times 10^{-7}$ | $4.41 \times 10^{-7}$ | $4.41 \times 10^{-7}$ |
| $L_{k}$ |  | $\times 10^{-9}$ | $-1.70 \times 10^{-8}$ | $-1.70 \times 10^{-8}$ | $-1.60 \times 10^{-7}$ | $-1.60 \times 10^{-7}$ | $-1.60 \times 10^{-7}$ |
| $L_{k j}$ |  | $\times 10^{-9}$ | $2.12 \times 10^{-8}$ | $2.12 \times 10^{-8}$ | $7.05 \times 10^{-8}$ | $7.05 \times 10^{-8}$ | $7.05 \times 10^{-8}$ |


| Coupling constants for $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $F_{k} \times 10^{2}$ | $F_{j} \times 10^{2}$ |  |  |  |  |
| $\left(30^{-}, 2\right)-\left(40^{-}, 0\right)$ | $1.45465(3700)$ | 2.82026(3200) |  |  |  |  |
| $\left(40^{+}, 0\right)-\left(30^{+}, 2\right)$ | $1.53515(2600)$ | $2.79966(1100)$ |  |  |  |  |
| $\left(11^{+}, 4\right)-\left(30^{+}, 2\right)$ | -1.37138(5500) | -1.64260(1800) |  |  |  |  |
|  | $C_{x z k} \times 10^{4}$ | $C_{y k} \times 10^{5}$ | $C_{x z} \times 10^{2}$ | $C_{x z j} \times 10^{4}$ | $C_{x z k j} \times 10^{6}$ | $C_{x z j j} \times 10^{6}$ |
| $\left(30^{+}, 2\right)-\left(20^{-}, 4\right)$ | -8.6800(1400) |  | $1.6328(1400)$ | 3.0980(2100) |  |  |
| $\left(30^{+}, 2\right)-\left(40^{-}, 0\right)$ |  |  | -2.57804(7500) | $1.72811(9900)$ |  |  |
| $\left(30^{+}, 2\right)-\left(30^{-}, 2\right)$ |  | 8.6424(7600) | -48.83210(4600) |  |  |  |
| $\left(40^{+}, 0\right)-\left(40^{-}, 0\right)$ | -3.80850(4500) |  | -51.77609(1900) | -4.51853(3700) | 4.45897(3900) | -1.06601(2200) |
| $\left(40^{+}, 0\right)-\left(30^{-}, 2\right)$ |  |  | -2.84623 (7300) | $2.1094(1000)$ |  |  |
| $\left(20^{+}, 4\right)-\left(20^{-}, 4\right)$ | 17.208(1600) |  | -33.6733(2000) |  |  | $4.1356(5100)$ |
| $\left(20^{+}, 4\right)-\left(30^{-}, 2\right)$ | -7.8479(4800) |  | $2.3682(2600)$ | 2.9640 (3600) |  |  |
| $\left(11^{+}, 4\right)-\left(20^{-}, 4\right)$ |  |  | -6.88843(6200) |  |  |  |
| $\left(11^{+}, 4\right)-\left(40^{-}, 0\right)$ | $1.99020(6000)$ |  |  |  |  |  |
| $\left(11^{+}, 4\right)-\left(30^{-}, 2\right)$ | -5.2058(2000) |  |  | $1.2148(1100)$ |  |  |

Minor isotopomers ${ }^{\text {a }}$
$\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ : 28 energy levels ( 27 included in the fit), 3 adjusted parameters, standard deviation: $0.010 \mathrm{~cm}^{-1}$

| $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ | $\left(40^{ \pm}, 0\right)$ | $\left(30^{-}, 2\right)$ | $\left(30^{+}, 2\right)$ | $\left(20^{-}, 4\right)$ | $\left(20^{+}, 4\right)$ | $\left(11^{+}, 4\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $E_{v}$ | $9907.050108(7700)$ | 9802.7012 | 9802.7668 | 9643.0336 | 9643.8174 | 9740.8740 |
| A | 9.6170666(7400) | 10.45901 | 10.46307 | 11.50845 | 11.60132 | 11.54480 |
| B | $8.591797(2100)$ | 9.167061 | 9.165419 | 9.760263 | 9.736973 | 9.768972 |
| C | 4.47229100 | 4.415036 | 4.414420 | 4.351358 | 4.341112 | 4.391328 |
| $\Delta_{k}$ | $3.3752 \times 10^{-3}$ | $5.4816 \times 10^{-3}$ | $5.6726 \times 10^{-3}$ | $6.6497 \times 10^{-3}$ | $9.3802 \times 10^{-3}$ | $7.6930 \times 10^{-3}$ |

Table 4 (continued)
Table 4 (continued
$\mathrm{H}_{2}{ }^{34} \mathrm{~S}: 181$ energy levels ( 175 included in the fit), 11 adjusted parameters, standard deviation: $0.0068 \mathrm{~cm}^{-1}$

| $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ | $\left(40^{-}, 0\right)$ | $\left(40^{+}, 0\right)$ | $\left(30^{-}, 2\right)$ | $\left(30^{+}, 2\right)$ | $\left(20^{-}, 4\right)$ | $\left(20^{+}, 4\right)$ | $\left(11^{+}, 4\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $E_{v}$ | 9903.320290(1800) | 9903.313489(1100) | 9798.741532(2300) | 9798.796482(4500) | 9638.90 | 9639.86 | 9736.86 |
| A | 9.632 | 42(1200) | 10.4398208(2200) | 10.445430 | 11.48904 | 11.58176 | 11.52533 |
| $B$ | 8.56 | 808(6200) | 9.167038 | $9.1665765(6300)$ | 9.760240 | 9.736949 | 9.768949 |
| $C$ | 4.46 | 478(1800) | $4.41176398(4600)$ | 4.41112214(8200) | 4.347974 | 4.337735 | 4.387912 |
| $\Delta_{k}$ | 3.367 | $\times 10^{-3}$ | $5.4692 \times 10^{-3}$ | $5.6598 \times 10^{-3}$ | $6.6347 \times 10^{-3}$ | $9.3590 \times 10^{-3}$ | $7.6756 \times 10^{-3}$ |

Note. All the results are in $\mathrm{cm}^{-1}$ and quoted errors are one standard deviation. Parameters presented without quoted errors were constrained to the given value (see text). All the other diagonal and resonance vibrational parameters were fixed to the $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ values.
$\left(40^{ \pm}, 0\right)$ states have very close but not absolutely coinciding rotational structure, the rotational levels of the $\left(30^{ \pm}, 2\right)$ pair differ by about $0.077 \mathrm{~cm}^{-1}$ while the separation between the components of the $\left(20^{ \pm}, 4\right)$ pair is even larger and reaches a value of $0.607 \mathrm{~cm}^{-1}$. Consequently, in the process of refinement of the Hamiltonian parameters, we could not keep identical the rotational and centrifugal distortion parameters of the components of the LM pairs without a noticeable loss in the quality of the energy levels reproduction. Thus, we varied independently the vibrational energies $E_{v}$ of the $\left(40^{ \pm}, 0\right)$ states as well as all rotational and centrifugal distortion parameters for the other LM pairs. As a consequence, of the strong resonance coupling with the bright states three and four parameters were varied for the $\left(20^{+}, 4\right)$ and $\left(11^{+}, 4\right)$ dark states, respectively, leading to values which might be considered as effective as, in fact, only two energy levels of the $\left(11^{+}, 4\right)$ dark state are experimentally determined (see below). We intend to adopt a resonance scheme which describes in a similar way and amplitude the resonance interaction between the LM pairs. Indeed, Table 4 shows that the resonance parameters between LM pairs, have close, though not coinciding values. For instance, the same coupling parameters with close values account for the interaction between the $\left(20^{+}, 4\right)$ and $\left(30^{-}, 2\right)$ states on one hand, and between the $\left(20^{-}, 4\right)$ and $\left(30^{+}, 2\right)$ states on the other hand.

An rms deviation of $0.0061 \mathrm{~cm}^{-1}$ was achieved by varying 54 diagonal and 30 resonance parameters listed in Table 4 with $68 \%$ confidence intervals. Parameters without confidence interval were fixed to the corresponding values of the $\left(20^{-}, 0\right)$ state for the $\left(40^{ \pm}, 0\right)$ pair, of the $\left(10^{-}, 2\right)$ state for the $\left(30^{ \pm}, 2\right)$ pair, and of the $\left(00^{+}, 4\right)$ state for the $\left(20^{ \pm}, 4\right)$ pair and the $\left(11^{+}, 4\right)$ state [14]. The necessity to account for strong interaction with two highly excited bending dark states- $\left(20^{+}, 4\right)$ and $\left(11^{+}, 4\right)-$ led to a relative large number of varied resonance parameters: 10 of them concern indeed this interaction.

A remarkable example of strong resonance coupling is the interaction between the $\left(40^{ \pm}, 0\right)$ [725] levels at 10301.528 and $10301.509 \mathrm{~cm}^{-1}$, respectively, and the $\left(30^{ \pm}, 2\right)$ [743] levels at 10302.100 and $10302.089 \mathrm{~cm}^{-1}$, respectively. The resulting wavefunctions of these levels correspond to a nearly equal mixing of the four resonating states. A second example is the strong interaction between the $\left(11^{+}, 4\right)$ dark state and the $\left(40^{ \pm}, 0\right)$ and $\left(30^{ \pm}, 2\right)$ pairs which induces an important intensity borrowing leading to the observation of extra lines reaching the $\left(11^{+}, 4\right)$ [863] and $\left(11^{+}, 4\right)$ [972] levels observed at 10444.693 and $10637.662 \mathrm{~cm}^{-1}$, respectively (see Fig. 3). As mentioned above, this kind of "nonsymmetric" interactions with, for instance, the single $\left(11^{+}, 4\right)$ state, induces sometimes an increase of the energy separation between specific rotational levels of

Table 5
Rotational energy levels $\left(\mathrm{cm}^{-1}\right)$ of the $\left(40^{-}, 0\right)$ and $\left(40^{+}, 0\right)$ vibrational states of $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 2 | 0 | 2 | 9942.787 |  | 1 | -0.014 |  |  |  |  |
| 2 | 1 | 2 |  |  |  |  | 9943.143 |  | 1 | 0.005 |
| 2 | 2 | 0 | 9961.973 | 3 | 2 | -0.009 |  |  |  |  |
| 3 | 2 | 2 | 9997.721* |  | 1 | 0.022 |  |  |  |  |
| 4 | 0 | 4 | 10014.693 |  | 1 | -0.007 | 10014.693 |  | 1 | -0.006 |
| 4 | 1 | 4 | 10014.693 |  | 1 | 0.000 | 10014.693 |  | 1 | -0.001 |
| 4 | 1 | 3 | 10046.542 |  | 1 | -0.015 |  |  |  |  |
| 5 | 0 | 5 | 10063.940 | 1 | 2 | -0.006 | 10063.942 | 3 | 2 | -0.003 |
| 5 | 1 | 5 | 10063.942 | 3 | 2 | -0.002 |  |  |  |  |
| 5 | 5 | 1 | 10187.369 |  | 1 | 0.001 |  |  |  |  |
| 6 | 0 | 6 | 10122.109 | 4 | 2 | 0.009 | 10122.113 |  | 1 | 0.015 |
| 6 | 1 | 6 | 10122.105 |  | 1 | 0.005 | 10122.109 | 4 | 2 | 0.010 |
| 7 | 0 | 7 | 10189.176 |  | 1 | 0.001 | 10189.162 |  | 1 | -0.012 |
| 7 | 1 | 7 | 10189.176 |  | 1 | 0.001 | 10189.162 |  | 1 | -0.012 |
| 8 | 0 | 8 | 10265.155 |  | 1 | 0.014 |  |  |  |  |
| 8 | 1 | 8 | 10265.155 |  | 1 | 0.014 |  |  |  |  |
| 9 | 0 | 9 |  |  |  |  | 10349.998 |  | 1 | 0.009 |
| 9 | 1 | 9 |  |  |  |  | 10349.998 |  | 1 | 0.010 |
| 11 | 0 | 11 | 10546.270 |  | 1 | -0.008 | 10546.261 |  | 1 | -0.016 |
| 11 | 1 | 11 | 10546.270 |  | 1 | -0.008 |  |  |  |  |

Note. $\sigma$ denotes the experimental uncertainty of the level in $10^{-3} \mathrm{~cm}^{-1} . N$ is the number of observed transitions used to calculate the upper energy level. $\Delta$ is the difference between the experimental and calculated values of the energy in $\mathrm{cm}^{-1}$.

Table 6
Rotational energy levels $\left(\mathrm{cm}^{-1}\right)$ of the $\left(40^{-}, 0\right)$ and $\left(40^{+}, 0\right)$ vibrational states of $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 0 | 0 | 0 | 9903.323 |  | 1 | 0.003 |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  | 9916.140 |  | 1 | 0.003 |
| 1 | 1 | 1 | 9917.637 | 2 | 2 | 0.007 |  |  |  |  |
| 1 | 1 | 0 | 9921.512 |  | 1 | -0.004 |  |  |  |  |
| 2 | 0 | 2 | 9939.039 |  | 1 | 0.008 |  |  |  |  |
| 2 | 1 | 2 | 9939.394 |  | 1 | 0.013 | 9939.386 | 3 | 2 | 0.005 |
| 2 | 1 | 1 | 9951.029 | 2 | 2 | -0.001 |  |  |  |  |
| 2 | 2 | 1 |  |  |  |  | 9955.494 |  | 1 | 0.009 |
| 2 | 2 | 0 | 9958.242 | 2 | 2 | 0.008 |  |  |  |  |
| 3 | 0 | 3 | 9970.612 |  | 1 | 0.000 | 9970.604 |  | 1 | -0.003 |
| 3 | 1 | 3 | 9970.558 | 1 | 2 | 0.000 | 9970.554 |  | 1 | 0.000 |
| 3 | 1 | 2 | 9992.270 |  | 1 | -0.003 | 9992.275 | 9 | 3 | 0.003 |
| 3 | 2 | 2 | 9993.914 | 3 | 2 | 0.002 | 9993.911 | 1 | 2 | -0.001 |
| 3 | 2 | 1 | 10003.546 | 2 | 2 | -0.012 | 10003.547 |  | 1 | -0.007 |
| 3 | 3 | 1 | 10012.415 | 1 | 2 | 0.005 |  |  |  |  |
| 3 | 3 | 0 |  |  |  |  | 10014.010 |  | 1 | 0.002 |
| 4 | 0 | 4 | 10010.892 |  | 1 | 0.006 |  |  |  |  |
| 4 | 1 | 3 | 10042.713 | 2 | 2 | 0.001 |  |  |  |  |
| 4 | 2 | 3 |  |  |  |  | 10042.336 | 2 | 2 | -0.010 |
| 4 | 2 | 2 | 10062.428 |  | 1 | 0.001 | 10062.419 |  | 1 | -0.006 |
| 4 | 3 | 2 | 10066.772 |  | 1 | -0.006 | 10066.781 | 5 | 2 | 0.003 |
| 4 | 3 | 1 | 10074.039 | 9 | 2 | 0.006 | 10074.031 |  | 1 | 0.002 |
| 4 | 4 | 1 |  |  |  |  | 10088.505* |  | 1 | 0.026 |
| 4 | 4 | 0 | 10089.276 | 3 | 2 | -0.004 |  |  |  |  |
| 5 | 0 | 5 | 10060.087 | 3 | 2 | -0.007 | 10060.089 | 5 | 2 | 0.002 |
| 5 | 1 | 5 | 10060.089 | 4 | 3 | -0.004 | 10060.087 | 3 | 2 | 0.001 |
| 5 | 2 | 4 | 10100.837 |  | 1 | -0.006 |  |  |  |  |
| 5 | 2 | 3 | 10132.613 |  | 1 | 0.002 | 10132.598 | 5 | 2 | -0.009 |
| 5 | 3 | 3 | 10131.267 |  | 1 | 0.001 |  |  |  |  |
| 5 | 3 | 2 |  |  |  |  | 10149.477 | 2 | 2 | -0.008 |
| 5 | 4 | 2 | $10158.095$ | 1 | 2 | $-0.005$ | 10158.124* |  | 1 | 0.024 |
| 5 | 4 | 1 | 10162.919 |  | 1 | -0.017 | 10162.936 |  | 1 | 0.004 |

Table 6 (continued)

| $J$ | $K_{a}$ | $K_{c}$ | $\left(40^{-}, 0\right)$ |  |  |  | $\left(40^{+}, 0\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 5 | 5 | 1 | 10183.765 | 5 | 2 | 0.010 |  |  |  |  |
| 5 | 5 | 0 |  |  |  |  | 10184.118 |  | 1 | 0.015 |
| 6 | 0 | 6 | 10118.206 | 3 | 3 | 0.002 | 10118.202 |  | 1 | 0.005 |
| 6 | 1 | 6 | 10118.205 | 4 | 2 | 0.001 | 10118.205 | 4 | 2 | 0.009 |
| 6 | 1 | 5 | 10168.074 | 3 | 3 | -0.001 |  |  |  |  |
| 6 | 2 | 5 | 10168.079 |  | 1 | 0.014 | 10168.070 |  | 1 | 0.012 |
| 6 | 2 | 4 | 10208.442 |  | 1 | -0.006 |  |  |  |  |
| 6 | 3 | 4 | 10208.153 |  | 1 | -0.006 |  |  |  |  |
| 6 | 4 | 3 |  |  |  |  | 10236.742 |  | 1 | -0.010 |
| 6 | 4 | 2 | 10253.748 | 8 | 2 | 0.007 |  |  |  |  |
| 6 | 5 | 2 |  |  |  |  | 10267.984 | 4 | 2 | -0.014 |
| 6 | 6 | 0 | 10298.354 |  | 1 | 0.005 |  |  |  |  |
| 7 | 0 | 7 | 10185.226 | 1 | 2 | -0.004 | 10185.227 |  | 1 | 0.004 |
| 7 | 1 | 7 | 10185.226 | 1 | 2 | -0.004 | 10185.227 |  | 1 | 0.004 |
| 7 | 1 | 6 | 10244.133 |  | 1 | -0.002 | 10244.127 | 4 | 2 | -0.001 |
| 7 | 2 | 6 | 10244.129 | 5 | 3 | -0.006 | 10244.122 |  | 1 | -0.005 |
| 7 | 2 | 5 | 10293.615 |  | 1 | 0.001 | 10293.590* |  | 1 | -0.020 |
| 7 | 3 | 5 | 10293.418 | 2 | 2 | 0.002 |  |  |  |  |
| 7 | 4 | 4 | 10332.413 | 7 | 3 | 0.011 |  |  |  |  |
| 7 | 5 | 3 | 10358.468* |  | 1 | -0.031 |  |  |  |  |
| 7 | 5 | 2 |  |  |  |  | 10375.663 |  | 1 | 0.013 |
| 7 | 6 | 2 | 10396.553 |  | 1 | -0.008 |  |  |  |  |
| 7 | 7 | 1 | 10431.745 |  | 1 | -0.008 |  |  |  |  |
| 8 | 0 | 8 | 10261.138 | 2 | 3 | -0.001 | 10261.135 |  | 1 | 0.003 |
| 8 | 1 | 8 | 10261.139 |  | 1 | 0.000 | 10261.135 |  | 1 | 0.003 |
| 8 | 1 | 7 | 10329.076 | 12 | 2 | -0.001 | 10329.064 |  | 1 | -0.006 |
| 8 | 2 | 7 |  |  |  |  | 10329.065 | 1 | 2 | -0.006 |
| 8 | 2 | 6 | 10387.361 | 8 | 3 | 0.001 |  |  |  |  |
| 8 | 3 | 6 | 10387.350 | 4 | 2 | -0.005 | 10387.359 |  | 1 | -0.001 |
| 8 | 3 | 5 | 10436.023 |  | 1 | -0.008 |  |  |  |  |
| 8 | 4 | 4 | 10475.610 |  | 1 | 0.012 |  |  |  |  |
| 8 | 5 | 3 | 10509.391 |  | 1 | 0.003 |  |  |  |  |
| 8 | 7 | 2 |  |  |  |  | 10515.793 |  | 1 | 0.004 |
| 9 | 0 | 9 | 10345.922 |  | 1 | -0.003 | 10345.908 |  | 1 | -0.008 |
| 9 | 1 | 9 | 10345.921 |  | 1 | -0.003 | 10345.908 |  | 1 | -0.008 |
| 9 | 1 | 8 | 10422.863 | 2 | 2 | -0.009 | 10422.860 | 1 | 2 | -0.005 |
| 9 | 2 | 8 | 10422.863 | 2 | 2 | -0.009 | 10422.860 | 1 | 2 | -0.005 |
| 9 | 2 | 7 | 10490.098 |  | 1 | 0.005 | 10490.092 | 1 | 3 | 0.006 |
| 9 | 3 | 7 | 10490.096 | 6 | 3 | 0.004 | 10490.092 | 1 | 2 | 0.006 |
| 9 | 3 | 6 | 10547.629 |  | 1 | -0.007 |  |  |  |  |
| 9 | 4 | 6 | 10547.597 | 1 | 2 | 0.003 |  |  |  |  |
| 10 | 0 | 10 | 10439.586 |  | 1 | 0.014 |  |  |  |  |
| 10 | 1 | 10 | 10439.586 |  | 1 | 0.014 |  |  |  |  |
| 10 | 1 | 9 | 10525.507 | 7 | 2 | -0.001 | 10525.500 |  | 1 | -0.001 |
| 10 | 2 | 9 | 10525.513 |  | 1 | 0.005 | 10525.500 |  | 1 | -0.001 |
| 10 | 2 | 8 | 10601.622 | 8 | 2 | -0.001 | 10601.616 |  | 1 | 0.000 |
| 10 | 3 | 8 | 10601.623 | 7 | 2 | 0.000 | 10601.615 |  | 1 | -0.002 |
| 11 | 0 | 11 | 10542.074 |  | 1 | 0.007 | 10542.052 |  | 1 | -0.006 |
| 11 | 1 | 11 | 10542.074 |  | 1 | 0.007 | 10542.052 |  | 1 | -0.006 |
| 11 | 1 | 10 | 10636.957 |  | 1 | -0.012 |  |  |  |  |
| 11 | 2 | 10 | 10636.957 |  | 1 | -0.012 |  |  |  |  |
| 12 | 0 | 12 | 10653.379 |  | 1 | -0.012 | 10653.388 |  | 1 | 0.006 |
| 12 | 1 | 12 | 10653.379 |  | 1 | -0.012 | 10653.388 |  | 1 | 0.006 |
| 12 | 2 | 10 | 10850.996* |  | 1 | -0.019 |  |  |  |  |
| 12 | 3 | 10 | 10850.996* |  | 1 | -0.019 |  |  |  |  |
| 13 | 0 | 13 | 10773.517 |  | 1 | -0.010 |  |  |  |  |
| 13 | 1 | 13 | 10773.517 |  | 1 | -0.010 |  |  |  |  |
| 13 | 2 | 11 | 10988.850 |  | 1 | 0.001 |  |  |  |  |
| 13 | 3 | 11 | 10988.850 |  | 1 | 0.001 |  |  |  |  |
| 14 | 0 | 14 | 10902.462 |  | 1 | 0.011 |  |  |  |  |
| 14 | 1 | 14 | 10902.462 |  | 1 | 0.011 |  |  |  |  |

Note. Asterisks denote the energy levels not included in the fit. $\sigma$ denotes the experimental uncertainty of the level in $10^{-3} \mathrm{~cm}^{-1} . N$ is the number of observed transitions used to calculate the upper energy level. $\Delta$ is the difference between the experimental and calculated values of the energy in $\mathrm{cm}^{-1}$.

Table 7
Rotational energy levels $\left(\mathrm{cm}^{-1}\right)$ of the $\left(30^{-}, 2\right)$ and $\left(30^{+}, 2\right)$ vibrational states of $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$

| $J$ | $K_{a}$ | $K_{c}$ | $\left(30^{-}, 2\right)$ |  |  |  | $\left(30^{+}, 2\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}$ | $\sigma$ | $N$ | $\Delta$ |
| 1 | 0 | 1 | 9812.158 |  | 1 | 0.001 |  |  |  |  |
| 2 | 0 | 2 | 9835.648 |  | 1 | 0.002 |  |  |  |  |
| 2 | 1 | 1 | 9849.731 |  | 1 | -0.009 |  |  |  |  |
| 2 | 2 | 1 | 9854.558 |  | 1 | 0.011 |  |  |  |  |
| 2 | 2 | 0 | 9857.861 |  | 1 | -0.006 |  |  |  |  |
| 3 | 0 | 3 | 9867.586 |  | 1 | -0.011 | 9867.688 |  | 1 | 0.013 |
| 3 | 1 | 3 | 9867.588 | 3 | 2 | -0.002 |  |  |  |  |
| 3 | 2 | 2 | 9894.766 |  | 1 | 0.005 |  |  |  |  |
| 3 | 2 | 1 | 9906.286 | 3 | 3 | 0.000 |  |  |  |  |
| 3 | 3 | 1 | 9915.829 | 1 | 2 | 0.016 |  |  |  |  |
| 4 | 0 | 4 | 9908.206 |  | 1 | -0.002 | 9908.268 |  | 1 | 0.005 |
| 4 | 1 | 4 | 9908.206 |  | 1 | 0.003 | 9908.268 |  | 1 | 0.009 |
| 4 | 1 | 3 |  |  |  |  | 9945.381 |  | 1 | 0.000 |
| 4 | 2 | 3 |  |  |  |  | 9945.015 |  | 1 | 0.006 |
| 4 | 2 | 2 | 9968.690 | 8 | 2 | 0.001 |  |  |  |  |
| 4 | 3 | 1 | 9982.065 |  | 1 | -0.008 |  |  |  |  |
| 4 | 4 | 1 | 9997.594 |  | 1 | -0.011 | 9997.690 |  | 1 | -0.009 |
| 4 | 4 | 0 | 9998.657 |  | 1 | -0.001 |  |  |  |  |
| 5 | 0 | 5 | 9957.614 |  | 1 | 0.002 |  |  |  |  |
| 5 | 1 | 5 | 9957.614 |  | 1 | 0.003 |  |  |  |  |
| 5 | 4 | 2 | 10071.471 |  | 1 | 0.012 |  |  |  |  |
| 5 | 5 | 1 | 10099.905 |  | 1 | 0.005 |  |  |  |  |
| 5 | 5 | 0 | 10100.374 |  | 1 | -0.010 |  |  |  |  |
| 6 | 0 | 6 | 10015.819 | 2 | 2 | 0.002 | 10015.862 |  | 1 | -0.009 |
| 6 | 1 | 6 | 10015.817 |  | 1 | 0.000 | 10015.862 |  | 1 | -0.009 |
| 6 | 1 | 5 | 10073.998 |  | 1 | 0.001 | 10074.079 |  | 1 | -0.003 |
| 6 | 2 | 5 | 10073.999 |  | 1 | 0.010 | $10074.078$ |  | 1 | 0.003 |
| 6 | 3 | 4 |  |  |  |  | 10120.834 |  | 1 | -0.001 |
| 6 | 4 | 2 | 10174.475 |  | 1 | -0.006 |  |  |  |  |
| 7 | 0 | 7 | 10082.818 | 3 | 2 | -0.005 | 10082.867 |  | 1 | -0.007 |
| 7 | 1 | 7 | 10082.818 | 3 | 2 | -0.005 | 10082.867 |  | 1 | -0.007 |
| 8 | 2 | 6 | 10305.814 | 1 | 2 | 0.002 |  |  |  |  |
| 9 | 1 | 9 | 10243.141 |  | 1 | 0.003 |  |  |  |  |
| 9 | 2 | 8 | 10332.986 |  | 1 | -0.008 |  |  |  |  |
| 9 | 3 | 7 | 10411.204 |  | 1 | 0.004 |  |  |  |  |
| 10 | 0 | 10 | 10336.448 | 8 | 2 | -0.004 |  |  |  |  |
| 10 | 1 | 10 | 10336.456 |  | 1 | 0.005 | 10336.522 |  | 1 | 0.011 |

Note. $\sigma$ denotes the experimental uncertainty of the level in $10^{-3} \mathrm{~cm}^{-1} . N$ is the number of observed transitions used to calculate the upper energy level. $\Delta$ is the difference between the experimental and calculated values of the energy in $\mathrm{cm}^{-1}$.
the $\left(40^{ \pm}, 0\right)$ LM states. For instance, the [845] energy levels are separated by $0.076 \mathrm{~cm}^{-1}$. A similar situation was encountered and analyzed in our recent study of the $\left(40^{ \pm}, 1\right)-(000)$ overtone transition near $11000 \mathrm{~cm}^{-1}[9]$.

As soon as the transitions of the main isotope species were assigned, it was possible to identify transitions reaching the $\left(40^{ \pm}, 0\right)$ and $\left(30^{ \pm}, 2\right)$ states of the $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ and even of the $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ isotopomers which were present in natural abundance ( $4.22 \%$ and $0.78 \%$, respectively) in the sample. The observed energy levels of the $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ and $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ vibrational states are listed in Tables 5-7, respectively. The rotational and $\Delta_{k}$ centrifugal distortion constants for the vibrational states of $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ and $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ were estimated from the corresponding $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ parameters using simple isotopic relations [9], while the vibrational term value, $E_{v}$, parameters were estimated using Eq. (4) of [9]. All higher order parameters as well
as the coupling constants were simply fixed to the main isotopomer values. This procedure seems to be very accurate as only 11 parameters were needed to be refined to reproduce 175 observed energy levels of the $\mathrm{H}_{2}{ }^{34} \mathrm{~S}$ isotope within $0.0068 \mathrm{~cm}^{-1}$ while 3 parameters were varied to fit 27 energy levels of the $\mathrm{H}_{2}{ }^{33} \mathrm{~S}$ isotope with an rms deviation of $0.010 \mathrm{~cm}^{-1}$. The corresponding sets of rotational parameters are included in Table 4.

## 4. Intensity considerations

The approximate relative intensity values were derived for each absorption line from the peak depth values measured by ICLAS. By using the stronger lines observed in the FT spectrum, the ICLAS intensities were
normalized to obtain absolute intensity values. Taking into account the precision of the normalization procedure and possible saturation of the strongest lines, we estimate the experimental accuracy of our measured intensities to $25-30 \%$ on average with possible errors up to $100 \%$ for the weakest lines. The transition moment parameters were obtained by fitting 1183 (including doublets) line intensities ( 160 transitions for the $\left(20^{-}, 4\right)$ state, 342 for the $\left(40^{-}, 0\right), 323$ for the $\left(30^{-}, 2\right), 170$ for the $\left(30^{+}, 2\right)$, and 185 for the $\left(40^{+}, 0\right)$, state). An rms deviation of $18.3 \%$ was achieved by varying 25 parameters. The resulting line intensities are included in Supplementary Material attached to the present paper, which lists 1630 observed line positions and intensities with the corresponding rovibrational assignment and calculated intensities. In the case of blended lines, only transitions contributing to the experimental intensity value by more than $8 \%$ were, in general, included in the line list. The quality of the spectrum reproduction is exemplified in Figs. 1-3, which show an overview and some specific sections of the spectrum. In particular, the $9832-9846 \mathrm{~cm}^{-1}$ spectral region displayed in Fig. 3 shows that the intensity of the extra lines reaching rotational sublevels of the $\left(11^{+}, 4\right)$ dark state are very well reproduced, supporting, the resonance scheme adopted for the effective Hamiltonian. Despite the good overall agreement between the calculated and observed intensities, poorer results were obtained for some strongly perturbed transitions. This is in particular the case for the transitions reaching the $\left(40^{ \pm}, 0\right)$ [725] and the $\left(30^{ \pm}, 2\right)[743]$ levels which are strongly interacting.

It is interesting to note that the mixing coefficients of the wavefunctions corresponding to the fourfold energy levels clusters of the local mode pair are highly sensitive to the resonance scheme adopted. As a result, the calculated intensity distribution between the components of the local mode pair is rather unstable for transitions reaching fourfold energy levels clusters: according to the interaction scheme, the calculated intensity is transferred between the two components of the $\left(40^{ \pm}, 0\right) \mathrm{LM}$ pair leading to ambiguities in the vibrational assignments. However, the total intensity of the four involved transitions is unchanged. Despite the fact that only doubly degenerate transitions were included into the fit of the dipolar moment parameters, the intensity prediction for very strong fourfold degenerate experimental lines of the $\left(40^{ \pm}, 0\right)-(000)$ bands is very satisfactory (see the line list). We have some evidence that the intensity redistribution between the components of the $\left(40^{ \pm}, 0\right)$ LM pair is correctly reproduced by our model: the calculations show that transitions reaching fourfold clustered levels with $J \geqslant 7$ and $K_{a}=0,1$ have noticeably different frequencies and the corresponding experimental center of the (blended) line generally coincides with that calculated for the most intense component. For example, the center of the line at $9689.582 \mathrm{~cm}^{-1}$ with
an experimental intensity of $1.1 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~atm}^{-1}$ is close to the calculated position of the doubly degenerated line $\left(40^{+}, 0\right)$ [ 15015 ]-[16116], [15 1115 ]-[160 16] ( $9689.583 \mathrm{~cm}^{-1}$ ) calculated with an intensity of $9.9 \times 10^{-8} \mathrm{~cm}^{-2} \mathrm{~atm}^{-1}$, while the component of the same fourfold cluster- $\left(40^{-}, 0\right)$ [15015]-[16016], [15115][16116] is predicted at $9689.595 \mathrm{~cm}^{-1}$ with a significantly weaker intensity $\left(4.8 \times 10^{-8} \mathrm{~cm}^{-2} \mathrm{~atm}^{-1}\right)$. In consequence, the line intensities were used as an important criterion in the choice of the optimal set of resonance parameters between the components of the $\left(40^{ \pm}, 0\right)$ LM pair. Further refinements of the theoretical modeling of the line intensities would require more accurate intensity measurements.

The integrated band intensities were obtained as the sum of the individual calculated line intensities larger than $2.5 \times 10^{-9} \mathrm{~cm}^{-2} / \mathrm{atm}$. They are included in Table 1 where the results of the intensity calculations of [15] are also given for comparison. We emphasize that the integrated intensities estimated for the $\left(20^{+}, 4\right)$ and $\left(11^{+}, 4\right)$ dark states are very approximate. It should be noted also that the vibrational band intensities calculated in [15] may, in case of strong rovibrational coupling, significantly differ from our integrated values. However, the integrated band intensities for the 1st and 2 nd hexads as well as for the 1st decade of $\mathrm{H}_{2} \mathrm{~S}$ [14] were found in satisfactory agreement with the results of [15] with maximum deviations of $\pm 100 \%$. Much larger discrepancies are noted in the higher excited spectral region presently considered, especially for the $\left(30^{ \pm}, 2\right)-(000)$, and $\left(40^{+}, 0\right)-(000)$ bands (see Table 1). Part of this discrepancy may result from different vibrational assignment of absorption lines resulting from the large mixing of the wavefunctions of the clustered levels. In this case, the comparison of the sum of the integrated intensities reaching the two components of the LM pair is probably more meaningful. Still the discrepancies are too considerable to be explained by this reason indicating that the electric dipole moment function of $\mathrm{H}_{2} \mathrm{~S}$ derived in [15] is not accurate for the highly excited vibrational transitions. The difficulty of intensity calculations from a dipole moment function in $\mathrm{H}_{2} \mathrm{~S}$ has been previously analyzed as resulting of the dramatic consequences on the calculated intensities of a small change of the potential energy surface [15-18]. In this context, the potential function and the ab initio dipole moment surface calculated by Tyuterev et al. [16,18] will be highly valuable for such intensity calculations.

## 5. Conclusion

The present investigation of the near infrared spectrum of $\mathrm{H}_{2} \mathrm{~S}$ illustrates the performances of the ICLASVECSEL method. The use of VECSELs as amplification
media gives access to the near infrared spectrum with compact, simple diode pumped ICLAS spectrometer.

The detailed analysis of the $\mathrm{H}_{2} \mathrm{~S}$ spectrum between 9540 and $10000 \mathrm{~cm}^{-1}$ has allowed determining 892 energy levels. This number should be compared to a total number of 4175 levels used as input data in the determination of the potential energy surface of [17]. A complicate interaction system involving seven vibrational states, four of them being evidenced for the first time, has been successfully modeled. A comparison of the vibrational term values included in Table 1 shows a good agreement with the values predicted by the effective Hamiltonian model of [10]. The comparison with the values calculated from the potential function of [16] is also given and shows an excellent agreement for the three isotopomers. The larger deviations (up to $0.9 \mathrm{~cm}^{-1}$ ) observed for the dark levels of $\mathrm{H}_{2}{ }^{32} \mathrm{~S}$ are probably due to the effective character of the experimental term value which was extrapolated from a fit of very few rotational levels observed through local resonance interaction with bright states.

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tional term values calculated from the potential energy surface of [16].

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[^0]:    ${ }^{4}$ Supplementary data for this article are available on ScienceDirect.

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[^1]:    ${ }^{\text {a }}$ Normal mode labeling.
    ${ }^{\mathrm{b}}$ Local mode labeling.
    ${ }^{\mathrm{c}}$ Number of observed levels.
    ${ }^{\mathrm{d}}$ Effective value (see the text).

