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## High sensitivity cavity ring down spectroscopy of CO<sub>2</sub> overtone bands near 790 nm

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### ABSTRACT

The dyad bands of <sup>12</sup>C<sup>16</sup>O<sub>2</sub> near 790 nm have been recorded with a continuous-wave cavity ring-down spectrometer. Two cold bands and the two associated hot bands are observed in this region. High sensitivity of the  $1 \times 10^{-10}$ /cm level allows one to detect weak transitions with satisfied accuracy. The absolute line intensities have also been retrieved with an estimated accuracy of 2% for majority of the unblended lines. The vibrational transition dipole moment squared values and the empirical Herman–Wallis coefficients are presented for two cold bands. The comparison of the retrieved line positions and intensities with those given in the Carbon Dioxide Spectroscopic Databank shows clear deviation and indicates the empirical calculation can be further improved using the present spectroscopy data.

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### 1. Introduction

As the most important greenhouse gas, the concentration of carbon dioxide in the atmosphere increases by 35% since the beginning of the age of industrialization [1]. Carbon dioxide is a dominant species of the atmosphere of some rocky planets, such as Venus and Mars. Its high-resolution spectroscopy is not only used to monitor the evolution of carbon dioxide in the terrestrial atmosphere for policy makers, but also is an excellent tool for probing atmosphere to different depths. The present work is devoted to the four bands of <sup>12</sup>C<sup>16</sup>O<sub>2</sub> lying near 12 700 and 13 300 cm<sup>-1</sup>. One dyad corresponding to the upper state of the hot bands associated to the cold bands are noted as (10<sup>05</sup>)<sub>1,2</sub> and (11<sup>15</sup>)<sub>1,2</sub>. The corresponding HITRAN labels of these levels in Fermi resonance are (10051)–(10052) and (11151)–(11152).

The (10<sup>05</sup>)<sub>1,2</sub>–(00<sup>00</sup>)<sub>1</sub> cold bands were first observed by Adams and Dunham in the spectrum of the planet Venus in 1932. In 1953, these Venus bands were recorded with a long multipass cell and several atmospheres in the laboratory by Herzberg and Herzberg [2]. With the development

of high sensitivity laser spectroscopy techniques, the (10<sup>05</sup>)<sub>1,2</sub>–(00<sup>00</sup>)<sub>1</sub> bands were studied by photo acoustic (PA) [3], intra-cavity laser absorption spectroscopy (ICLAS) [4] and tunable diode laser spectroscopy (TDLs) [5,6]. Because of the large Doppler broadening and/or the lack of accurate reference standards in the region over 12 500 cm<sup>-1</sup>, the accuracy of ro-vibrational parameters for these vibrational states is limited. As a result, the HITRAN08 database [8] data corresponding to Venus bands above 9650 cm<sup>-1</sup> were taken from the CDS database [7].

Here we present the cavity ring-down spectroscopy (CRDS) of natural carbon dioxide sample near the 0.8 μm region. Superior sensitivity and resolution allow us to observe the weak bands with much better accuracy.

The present paper is organized as follows. In Section 2, the experimental procedure and the methodology of the analysis are presented. Section 3 is devoted to the band-by-band analysis and the modeling of the spectral parameters. Some discussions and conclusions are given in Section 4.

### 2. Experiment and data reduction

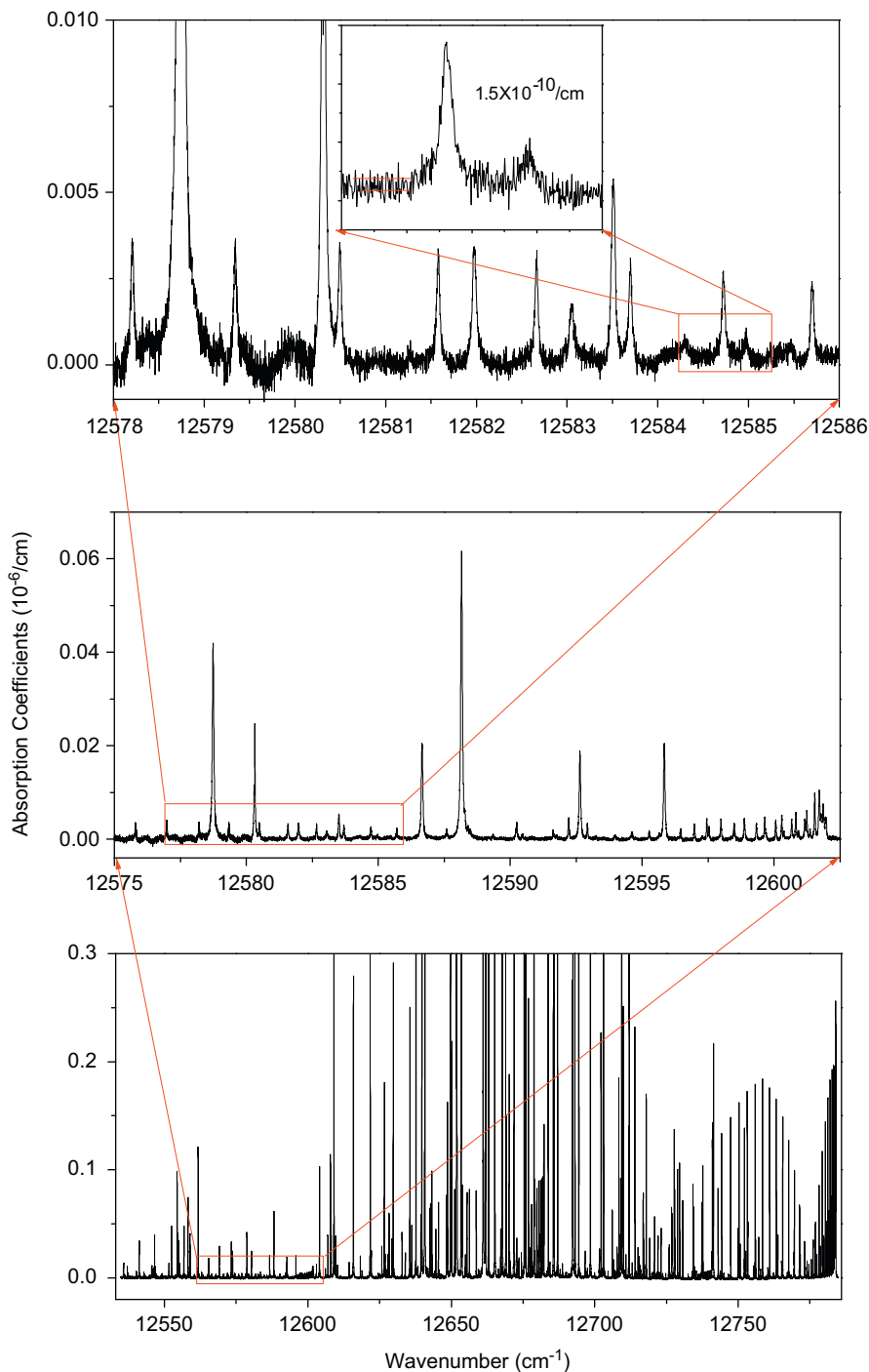
A continuous-wave (CW) CRDS spectrometer has been developed using a CW tunable Ti-sapphire laser over the

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spectral range of 780–830 nm. The details of the cavity ring-down spectrometer are presented in Refs. [9,10]. In brief, the structure of the setup is as follows: A CW tunable Ti:sapphire laser (Coherent 899-21) beam is carefully coupled into a 1.2 m long resonance cavity. The cavity mirrors (Los Gatos Inc.) have a reflectivity of 99.995% and one of the two mirrors is mounted on a piezoelectric

actuator (PI Inc.). The piezoelectric actuator is driven with a triangle wave from a function generator. The Ti:Sa laser is running in a step-scan mode controlled by a personal computer (PC). On each step, typically about 100 ring-down events are recorded with a fast digitizer (ADLINK PCI-9820). The digitizer is working at a sampling rate of 1 MS/s (mega-samples per second) with 14-bit resolution. A fitting



**Fig. 1.** Overview of the CRDS spectrum of carbon dioxide around 790 nm. Sample pressure: 103.3 Torr. Three successive enlargements illustrate the achieved signal to noise ratio. The insert shows the noise equivalent absorption of about  $1.5 \times 10^{-10}$ /cm.

program which follows the method proposed by Halmer et al. [11] is applied to fit the exponentially decay curve and to give the decay time  $\tau$ . The sample absorption coefficient,  $\alpha$ , can be derived from

$$\alpha = \frac{1}{c} \left( \frac{1}{\tau} - \frac{1}{\tau_0} \right) \quad (1)$$

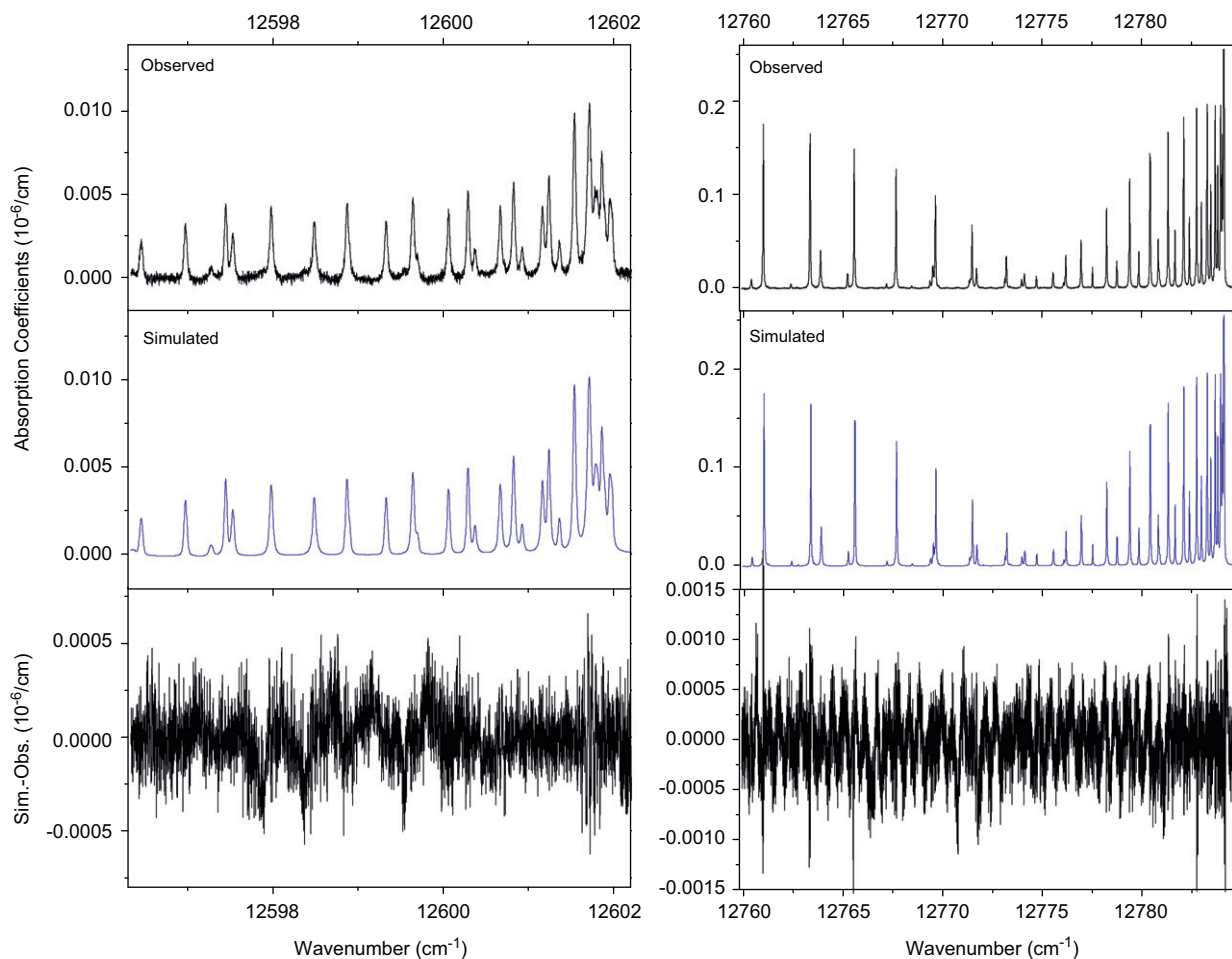
where  $c$  is the speed of light,  $\tau$  and  $\tau_0$  are the decay time of the cavity with and without sample, respectively.

Natural CO<sub>2</sub> gas sample was filled into the resonance cavity at room temperature. The sample pressure was 103.3 Torr measured with a capacitance manometer (MKS Baratron 627B) with an accuracy of 0.15%. The spectrum calibration is based on the readings given by a  $\lambda$ -meter (Burleigh WA1500) and has been described in details in Ref. [10]. It is checked and refined by using some reference lines for the whole region. The water line positions were taken from Ref. [12]. An overview of the CW-CRDS spectra is presented in Fig. 1, and three successive enlargements illustrate the quality of spectrum and good signal to noise ratio. The noise equivalent minimum detectable absorption loss is estimated to be  $1.5 \times 10^{-10}$ /cm.

### 3. Results

#### 3.1. Transition list

A total of four bands of <sup>12</sup>C<sup>16</sup>O<sub>2</sub> were detected near 790 nm. The line parameters of each observed line were retrieved using an interactive least squares multi-lines fitting procedure. Since the instrumental linewidth was estimated less than  $1 \times 10^{-4}$  cm<sup>-1</sup> [10] and is much smaller than the Doppler broadening, the instrumental profile was neglected in the fitting. A Voigt line profile was adopted and the Gaussian component width was fixed to the calculated Doppler width. Line position, integrated line absorbance, Lorentzian width of each line and a baseline were given by the fitting procedure (“Intwin” [13]). The position uncertainty of unblended and not-very-weak lines is estimated to be 0.001 cm<sup>-1</sup>. The main error on the line strength values comes from the line profile fitting, especially uncertainty on the baseline. The fitting error is estimated to be around 0.6% for well-isolated and unblended lines. Including the pressure uncertainty (0.15%) and the error from the temperature fluctuation (< 1%), the accuracy of the line intensities is estimated to



**Fig. 2.** Part of the observed CRDS spectrum (upper), simulated spectrum (middle) obtained as a sum of individual Voigt profiles, and the residuals (lower). Note that the weak lines in the left panels are about three orders of magnitude weaker than the strong lines in the right panels.

**Table 1**Line parameters of the  $(10^05)_1-(00^00)_1$  band of  $^{12}\text{C}^{16}\text{O}_2$ .

Line	Position	$S_{\text{obs}}$	$S_{\text{cal}}$	%	$ R _{\text{obs}}^2$
P 56	12683.0584*	2.58E-29	4.03E-29	-56.0	1.06E-11
P 54	12687.9967*	1.43E-28	5.94E-29	58.4	3.98E-11
P 52	12692.8145*	6.18E-29	8.61E-29	-39.2	1.19E-11
P 50	12697.5105	1.31E-28	1.23E-28	6.1	1.78E-11
P 48	12702.0833*	1.28E-28	1.72E-28	-34.4	1.25E-11
P 46	12706.5366*	2.57E-28	2.37E-28	7.6	1.82E-11
P 44	12710.8639	3.20E-28	3.21E-28	-0.3	1.68E-11
P 42	12715.0700	4.28E-28	4.28E-28	-0.1	1.69E-11
P 40	12719.1539	5.84E-28	5.60E-28	4.1	1.77E-11
P 38	12723.1134	7.18E-28	7.20E-28	-0.3	1.70E-11
P 36	12726.9496	9.09E-28	9.09E-28	0.0	1.70E-11
P 34	12730.6613	1.17E-27	1.13E-27	3.3	1.77E-11
P 32	12734.2508	1.37E-27	1.37E-27	0.1	1.71E-11
P 30	12737.7149	1.65E-27	1.64E-27	0.8	1.73E-11
P 28	12741.0550	2.00E-27	1.91E-27	4.1	1.79E-11
P 26	12744.2723	2.21E-27	2.19E-27	0.7	1.74E-11
P 24	12747.3632	2.48E-27	2.46E-27	0.7	1.74E-11
P 22	12750.3311	2.70E-27	2.70E-27	-0.1	1.73E-11
P 20	12753.1743	2.90E-27	2.90E-27	0.0	1.73E-11
P 18	12755.8914	3.06E-27	3.03E-27	1.0	1.75E-11
P 16	12758.4852	3.23E-27	3.08E-27	4.5	1.82E-11
P 14	12760.9533	3.03E-27	3.04E-27	-0.2	1.74E-11
P 12	12763.2977	2.89E-27	2.89E-27	0.2	1.75E-11
P 10	12765.5146	2.64E-27	2.63E-27	0.5	1.75E-11
P 8	12767.6089	2.14E-27	2.26E-27	-5.6	1.65E-11
P 6	12769.5763	1.81E-27	1.80E-27	0.6	1.76E-11
R 52	12771.3400	8.72E-29	8.98E-29	-3.0	1.64E-11
P 4	12771.4200	1.24E-27	1.25E-27	-1.2	1.73E-11
R 50	12773.0533	1.29E-28	1.28E-28	1.1	1.72E-11
P 2	12773.1374	6.20E-28	6.43E-28	-3.7	1.69E-11
R 48	12774.6433	1.78E-28	1.80E-28	-0.7	1.69E-11
R 0	12775.4777	3.22E-28	3.25E-28	-1.0	1.73E-11
R 2	12776.8842	9.43E-28	9.65E-28	-2.4	1.71E-11
R 44	12777.4545	3.17E-28	3.35E-28	-5.7	1.62E-11
R 4	12778.1618	1.58E-27	1.57E-27	0.8	1.77E-11
R 42	12778.6745	4.43E-28	4.47E-28	-0.8	1.70E-11
R 6	12779.3155	2.11E-27	2.10E-27	0.1	1.75E-11
R 40	12779.7708	6.07E-28	5.85E-28	3.7	1.78E-11
R 8	12780.3426	2.55E-27	2.56E-27	-0.0	1.75E-11
R 38	12780.7422	7.47E-28	7.52E-28	-0.7	1.71E-11
R 10	12781.2457	2.91E-27	2.91E-27	0.2	1.75E-11
R 36	12781.5900	9.66E-28	9.50E-28	1.7	1.75E-11
R 12	12782.0239	3.15E-27	3.15E-27	0.0	1.75E-11
R 34	12782.3122	1.18E-27	1.18E-27	0.2	1.73E-11
R 14	12782.6755	3.32E-27	3.27E-27	1.5	1.78E-11
R 32	12782.9117	1.41E-27	1.43E-27	-1.8	1.70E-11
R 16	12783.2012	3.32E-27	3.30E-27	0.8	1.76E-11
R 30	12783.3840	1.72E-27	1.71E-27	0.1	1.74E-11
R 18	12783.6037	3.24E-27	3.23E-27	0.4	1.75E-11
R 28	12783.7338	2.04E-27	2.01E-27	1.3	1.76E-11
R 20	12783.8796	3.05E-27	3.07E-27	-0.6	1.73E-11
R 26	12783.9571*	2.41E-27	2.31E-27	4.2	1.82E-11
R 22	12784.0290*	3.12E-27	2.86E-27	8.4	1.90E-11
R 24	12784.0534*	2.13E-27	2.59E-27	-22.0	1.43E-11

\*: Blended lines.

be 2% or less for a majority of the lines. For those blended lines, the error may reach 10% since the baseline uncertainty is supposed to be much larger (Fig. 2).

A total of 209  $^{12}\text{C}^{16}\text{O}_2$  line transitions was observed. The full line list is presented in Tables 1–3. The line strength values in the tables have been converted to the one with 98.42% as adopted in HITRAN and temperature at 296 K.

**Table 2**Line parameters of the  $(10^05)_2-(00^00)_1$  band of  $^{12}\text{C}^{16}\text{O}_2$ .

Line	Position	$S_{\text{obs}}$	$S_{\text{cal}}$	%	$ R _{\text{obs}}^2$
P 52	12592.9242	4.68E-29	4.70E-29	-0.4	9.11E-12
P 50	12597.4490	6.47E-29	6.60E-29	-2.0	8.87E-12
P 48	12601.8557	9.24E-29	9.13E-29	1.1	9.06E-12
P 46	12606.1380	1.28E-28	1.24E-28	3.3	9.17E-12
P 44	12610.3045	1.74E-28	1.66E-28	4.5	9.20E-12
P 42	12614.3578	2.18E-28	2.19E-28	-0.3	8.68E-12
P 40	12618.2869	2.79E-28	2.83E-28	-1.5	8.50E-12
P 38	12622.0995	3.49E-28	3.59E-28	-2.9	8.31E-12
P 36	12625.7986	4.45E-28	4.49E-28	-0.9	8.41E-12
P 34	12629.3751	5.65E-28	5.51E-28	2.5	8.63E-12
P 32	12632.8346	6.57E-28	6.64E-28	-1.0	8.28E-12
P 30	12636.1767	7.69E-28	7.85E-28	-2.1	8.13E-12
P 28	12639.4014	9.12E-28	9.11E-28	0.2	8.27E-12
P 26	12642.5097	1.05E-27	1.04E-27	1.4	8.32E-12
P 24	12645.5021	1.12E-27	1.15E-27	-3.4	7.89E-12
P 20	12651.1316*	1.27E-27	1.34E-27	-5.8	7.63E-12
P 18	12653.7721	1.37E-27	1.39E-27	-1.6	7.92E-12
P 16	12656.2953	1.36E-27	1.41E-27	-3.3	7.76E-12
P 14	12658.7015	1.41E-27	1.38E-27	1.8	8.13E-12
P 10	12663.1648	1.20E-27	1.19E-27	1.3	8.05E-12
P 6	12667.1618	7.70E-28	8.08E-28	-5.0	7.54E-12
P 2	12670.6908*	3.15E-28	2.88E-28	8.5	8.64E-12
R 0	12673.0331*	1.58E-28	1.46E-28	7.9	8.58E-12
R 50	12673.1670*	5.53E-29	6.81E-29	-23.2	7.38E-12
R 2	12674.4478	4.29E-28	4.32E-28	-0.7	7.85E-12
R 48	12674.5840*	1.19E-28	9.43E-29	20.5	1.13E-11
R 4	12675.7469	6.68E-28	7.02E-28	-5.1	7.53E-12
R 44	12677.0600*	1.85E-28	1.72E-28	7.2	9.51E-12
R 8	12677.9922	1.18E-27	1.15E-27	2.7	8.16E-12
R 42	12678.1191	2.20E-28	2.26E-28	-2.9	8.50E-12
R 10	12678.9400	1.26E-27	1.31E-27	-4.1	7.64E-12
R 40	12679.0563*	2.72E-28	2.93E-28	-7.4	8.07E-12
R 12	12679.7730	1.42E-27	1.42E-27	-0.2	7.96E-12
R 38	12679.8782	3.61E-28	3.72E-28	-3.2	8.33E-12
R 14	12680.4855	1.43E-27	1.49E-27	-3.8	7.71E-12
R 36	12680.5779	4.63E-28	4.65E-28	-0.6	8.47E-12
R 16	12681.0822	1.55E-27	1.50E-27	2.9	8.27E-12
R 34	12681.1608*	5.40E-28	5.72E-28	-5.8	7.99E-12
R 18	12681.5619	1.53E-27	1.48E-27	3.6	8.37E-12
R 32	12681.6247*	7.39E-28	6.90E-28	6.6	8.99E-12
R 20	12681.9232	1.43E-27	1.41E-27	1.0	8.18E-12
R 30	12681.9681	8.42E-28	8.17E-28	3.0	8.59E-12
R 22	12682.1687	1.31E-27	1.32E-27	-1.3	8.03E-12
R 28	12682.1957*	1.13E-27	9.50E-28	16.2	9.88E-12
R 24	12682.2989*	2.22E-27	1.21E-27	45.6	1.50E-11

\*: Blended lines.

### 3.2. Spectroscopic constants of the upper states

Four vibrational transitions were rotationally identified with the help of CDSD calculations. The standard expression for the vibration–rotation energy levels was used to determine the spectroscopic parameters:

$$F_v(J) = G_v + B_v J(J+1) - D_v J^2(J+1)^2 + H_v J^3(J+1)^3 \quad (2)$$

In Eq. (2),  $G_v$  is the vibrational term value,  $B_v$  is the rotational constant,  $D_v$  and  $H_v$  are the centrifugal distortion constants. The spectroscopic parameters for an upper state were fitted directly to the observed line positions of the respective band, and in the case of hot bands involving  $e$  and  $f$  components, the  $ee$  and  $ff$  sub bands were considered separately. The lower state rotational constants were constrained to their literature values [14] in the fitting.

**Table 3**Experimental line list of the  $(11^15)_1-(01^10)_1$  and  $(11^15)_2-(01^10)_1$  bands of  $^{12}\text{C}^{16}\text{O}_2$ .

$(11^15)_1-(01^10)_1$			$(11^15)_2-(01^10)_1$			$(11^15)_1-(01^10)_1$			$(11^15)_2-(01^10)_1$		
e-e			f-f			e-e			f-f		
Line	Position	$S_{\text{obs}}$	Line	Position	$S_{\text{obs}}$	Line	Position	$S_{\text{obs}}$	Line	Position	$S_{\text{obs}}$
P 45	12666.1326	1.36E-29	P 46	12664.0851	6.37E-29	P 37	12543.3148	1.17E-29	P 4	12588.4883	3.58E-29
P 35	12686.1202	3.43E-29	P 44	12668.3688	5.87E-30	P 35	12546.9619	1.29E-29	P 12	12580.4955	5.37E-29
P 33	12689.7533	8.82E-29	P 42	12672.5387	1.33E-29	P 33	12550.4989	3.18E-29	P 22	12567.9047	4.63E-29
P 27	12699.9100	9.92E-29	P 40	12676.5917	2.43E-29	P 31	12553.9097	4.28E-29	P 24	12565.0394	3.47E-29
P 19	12711.7223	1.08E-28	P 32	12691.5600	3.86E-29	P 29	12557.2064	4.16E-29	P 26	12562.0579	5.12E-29
P 17	12714.3680	9.45E-29	P 30	12694.9998	5.26E-29	P 27	12560.3839	4.43E-29	R 4	12595.2673	3.46E-29
P 13	12719.2879	8.62E-29	P 26	12701.5097	6.92E-29	P 25	12563.4461	2.90E-29	P 8	12584.7232	5.09E-29
P 11	12721.5622	8.04E-29	P 24	12704.5818	8.23E-29	P 23	12566.3886	6.28E-29	P 20	12570.6523	7.12E-29
P 9	12723.7132	7.52E-29	P 22	12707.5325	1.03E-28	P 19	12571.9186	8.21E-29	R 8	12597.5322	4.22E-29
P 7	12725.7397	6.73E-29	P 20	12710.3600	1.05E-28	P 17	12574.5126	7.57E-29	P 14	12578.2075	5.40E-29
P 3	12729.4259	4.49E-29	P 16	12715.6439	9.69E-29	P 15	12576.9854	6.92E-29	R 10	12598.4873	6.83E-29
R 1	12733.3243	2.06E-29	P 14	12718.1020	1.15E-28	P 13	12579.3425	4.98E-29	P 30	12555.7527	4.00E-29
R 3	12734.6778	4.03E-29	P 12	12720.4376	9.20E-29	P 11	12581.5796	5.25E-29	R 40	12598.9027	1.38E-29
R 43	12735.5764	1.45E-29	P 10	12722.6488	7.64E-29	P 9	12583.6979	4.73E-29	R 12	12599.3290	5.31E-29
R 5	12735.8990	9.31E-29	P 8	12724.7379	7.95E-29	P 7	12585.7025	3.79E-29	R 6	12596.4585	3.58E-29
R 41	12736.7030	1.32E-29	P 4	12728.5445	2.76E-29	P 5	12587.5885	3.94E-29	R 38	12599.6986	8.91E-30
R 7	12736.9958	9.49E-29	P 2	12730.2645	1.27E-29	P 3	12589.3511	1.09E-29	R 14	12600.0600	5.89E-29
R 9	12737.9706	9.37E-29	R 2	12734.0243	2.52E-29	R 1	12593.2495	9.09E-30	R 2	12593.9668	1.73E-29
R 37	12738.5911	3.47E-29	R 44	12735.1900	1.14E-29	R 3	12594.6137	4.39E-29	R 36	12600.3717	2.92E-29
R 11	12738.8175	1.06E-28	R 42	12736.3654	3.24E-29	R 7	12596.9782	4.94E-29	R 16	12600.6662	7.17E-29
R 35	12739.3492	3.53E-29	R 6	12736.4752	9.91E-29	R 9	12597.9827	7.86E-29	P 34	12548.9776	8.24E-29
R 13	12739.5447	1.10E-28	R 8	12737.5165	6.67E-29	R 11	12598.8696	6.55E-29	R 34	12600.9228	2.54E-29
R 33	12739.9862	2.54E-29	R 10	12738.4331	8.98E-29	R 13	12599.6423	8.83E-29	R 18	12601.1604	7.05E-29
R 15	12740.1456	1.12E-28	R 36	12739.1445	4.69E-29	R 15	12600.2888	7.38E-29	P 10	12582.6629	4.98E-29
R 31	12740.4977	4.04E-29	R 12	12739.2268	1.28E-28	R 17	12600.8225	9.39E-29	R 32	12601.3597	2.63E-29
R 17	12740.6231	1.06E-28	R 34	12739.8281	5.06E-29	R 19	12601.2364	9.61E-29	P 36	12545.4138	1.23E-29
R 27	12741.1551	3.08E-28	R 14	12739.8977	1.12E-28	R 21	12601.5357	1.61E-28	P 16	12575.8027	5.56E-29
			R 32	12740.3872	5.08E-29						
			R 16	12740.4443	1.22E-28						

The spectroscopic parameters retrieved from the fitting are presented in Table 4. The *rms* value of the (obs.-calc.) deviations are generally  $1 \times 10^{-3} \text{ cm}^{-1}$  which is consistent with the experimental accuracy. The corresponding spectroscopic parameters reported in the literature are also reviewed in italics and included in Table 4.

### 3.3. Vibrational transition dipole moment squared, and Herman–Wallis factor

The line intensity  $S(T_0)$  in  $\text{cm}^{-1}/(\text{cm}^{-2} \text{ mol})$  at the standard temperature  $T_0=296 \text{ K}$  can be deduced using the following equation:

$$S(T_0) = \frac{1}{4\pi\epsilon_0} \frac{8\pi^3\nu_0}{3hcQ(T_0)} |R|^2 L(J,\ell) e^{-hcE''/kT_0} [1 - e^{-hc\nu_0/kT_0}] \quad (3)$$

In Eq. (3),  $1/4\pi\epsilon_0 = 10^{-36} \text{ erg cm}^3 \text{ D}^{-2}$ ;  $h$  is Planck's constant;  $c$  is the vacuum speed of light;  $\nu_0$  is the transition wavenumber in  $\text{cm}^{-1}$ ;  $Q(T_0)$  is the total partition function at temperature  $T_0$ ;  $L(J,\ell)$  is the Hönl–London factor;  $J$  is the lower state rotational quantum number;  $\ell$  is the quantum number of the projection of the vibrational angular momentum on the molecular axis;  $E''$ , in  $\text{cm}^{-1}$  is the lower level energy; and  $k$  is the Boltzmann constant.

For those two parallel bands, the Hönl–London factor  $L(J,\ell)$  is equal to  $|m|$ , where  $m$  is  $-J$  for  $P$  branch, and  $J+1$  for  $R$  branch. For the isolated vibrational states of a linear molecule, the rotational dependence of the transition

dipole moment squared can be expressed with

$$|R|^2 = |R_0|^2 F(m) \quad (4)$$

where  $|R|^2$  is the vibrational transition dipole moment squared,  $F(m)$  is the empirical Herman–Wallis factor which can be interpreted with

$$F(m) = (1 + A_1 m + A_2 m^2)^2 \quad (5)$$

where  $A_1$  and  $A_2$  are the Herman–Wallis coefficients. In this case, the vibrational transition dipole moment squared and the Herman–Wallis coefficients are retrieved from the fitting of the line intensities corresponding to unblended transitions, and they are given in Table 4. The line intensities calculated with this set of Herman–Wallis coefficients are given in Tables 1 and 2 for the  $(10^05)_{1,2}-(00^00)_1$  cold bands. The blended lines marked with \* in the tables were excluded from the fit. In Fig. 3, the plot of the transition dipole moment squared versus rotational quantum number  $m$  is given for two cold bands in the upper and lower panels, respectively.

## 4. Discussion and conclusion

Significant progress on the carbon dioxide spectroscopy data has been made in the latest HITRAN [8] database owing to the Fourier transform spectroscopy measurements carried out in the Jet Propulsion Laboratory [15], CRDS observations in the 5851–7045  $\text{cm}^{-1}$  region from Laboratoire de Spectrométrie

**Table 4**

Spectroscopic constants (in  $\text{cm}^{-1}$ ), vibrational transition moments  $|R_\nu|^2$  (in  $\text{D}^2$ ; D, Debye), Herman–Wallis parameters of the  $^{12}\text{C}^{16}\text{O}_2$  bands observed in the present study.

States	$G_\nu$			$B_\nu$			$D_\nu \times 10^7$			
<i>Lower states constants</i>										
$(00^0)_1\text{e}$	0.00000			0.39021894			1.334088			
$(01^1)_1\text{e}$	667.3798265			0.390639109			1.35393			
$(01^1)_1\text{f}$	667.3798265			0.391254698			1.361606			
Band	$\Delta G_\nu^a$	$B_\nu$	$D_\nu \times 10^7$	$J_{\text{MAX}} P/R$	$n/N^b$	$\text{RMS}^c$	$ R ^2 \times 10^{11}$	$A_1 \times 10^5$	$A_2 \times 10^5$	
$(10^0)_2\text{e}-(00^0)_1\text{e}$ JMS1999 <sup>e</sup>	12672.28163(24) 12672.2833(1)	0.37563636(53) 0.37563425(9)	1.5828(21) 1.5695(3)	52/50	40/45	0.76	0.7901(78)	0.0 <sup>d</sup>	2.81(41)	
$(10^0)_1\text{e}-(00^0)_1\text{e}$ JMS1999 <sup>e</sup>	12774.72961(17) 12774.7310(1)	0.37454991(35) 0.3745506(2)	1.1249(13) 1.1264(5)	56/52	52/54	0.66	1.7503(52)	9.1(40)	-0.77(14)	
$(11^1)_2\text{e}-(01^1)_1\text{e}$ $(11^1)_2\text{f}-(01^1)_1\text{f}$	12591.78750(59) 12591.79144(68)	0.3759524(26) 0.3768050(29)	1.527(20) 1.514(19)	37/21 36/40	22/27 20/27	1.22 1.41				
$(11^1)_1\text{e}-(01^1)_1\text{e}$ $(11^1)_1\text{f}-(01^1)_1\text{f}$	12731.86183(35) 12731.86135(25)	0.3751385(13) 0.37583391(81)	1.1626(71) 1.1569(41)	45/43 46/44	22/27 25/29	0.89 0.70				

Note: The lower state constants were fixed at the values of Ref. [14]. The uncertainties are given in parenthesis in the unit of the last quoted digit.

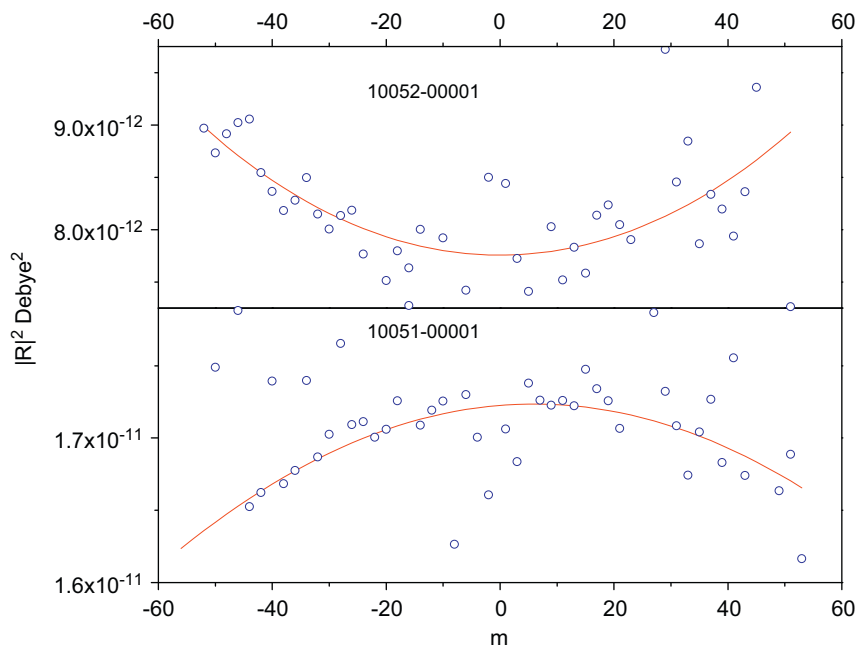
<sup>a</sup> Difference between the upper and lower vibrational term values.

<sup>b</sup>  $n$ : number of transitions included in the fit;  $N$ : number of assigned rotational transitions.

<sup>c</sup> Root mean square deviation (in  $10^{-3} \text{cm}^{-1}$ ).

<sup>d</sup> Values were fixed to zero.

<sup>e</sup> Values from Ref. [17].



**Fig. 3.** Experimental (open circles) and calculated (solid lines) values of the transitions dipole moment squared of the  $(10^0)_{1,2}$  cold bands of carbon dioxide. The calculated  $|R|^2$  values were obtained using the parameters given in Table 4.

Physique, UJF, Grenoble [16], and the high quality theoretical calculation (CDS). All lines above  $9650 \text{cm}^{-1}$  given in HITRAN08 are actually calculated results from CDS, including those four bands recorded in present measurement. Although as mentioned in the introduction part, the  $(10^0)_{1,2}-(00^0)_1$  bands have been studied with FTS, PA, ICLAS and TDLs before.

The stated accuracy of the ro-vibrational energy levels of the  $(10^0)_{1,2}$  state reaches  $1 \times 10^{-4} \text{cm}^{-1}$  with the  $(10^0)_{1,2}-(10^0)_{1,2}$  FT emission spectra near  $4.5 \mu\text{m}$  provided by Campargue et al. and verified by the Ritz principle [17]. However, the line position accuracy of TDLs is only within  $0.01 \text{cm}^{-1}$ . Therefore, on the one hand, we compared our

results with the CDSD calculations, on the other hand, the line positions of the  $(10^05)_{1,2}-(00^00)_1$  bands were also compared with the experimental values determined by Ritz principle calculations [17].

Fig. 4 shows the line position deviations of the observations from HITRAN08 values and Ritz ones in the upper and

lower panels, respectively. For previously reported  $(10^05)_{1,2}-(00^00)_1$  cold bands, it is obvious that the Ritz values agrees well with the line positions from present CW-CRDS measurement. However, the HITRAN08 values have systematic shifts of about  $0.005$  and  $0.002$   $\text{cm}^{-1}$  for the dyads, respectively. The largest deviation (HITRAN-obs.) is

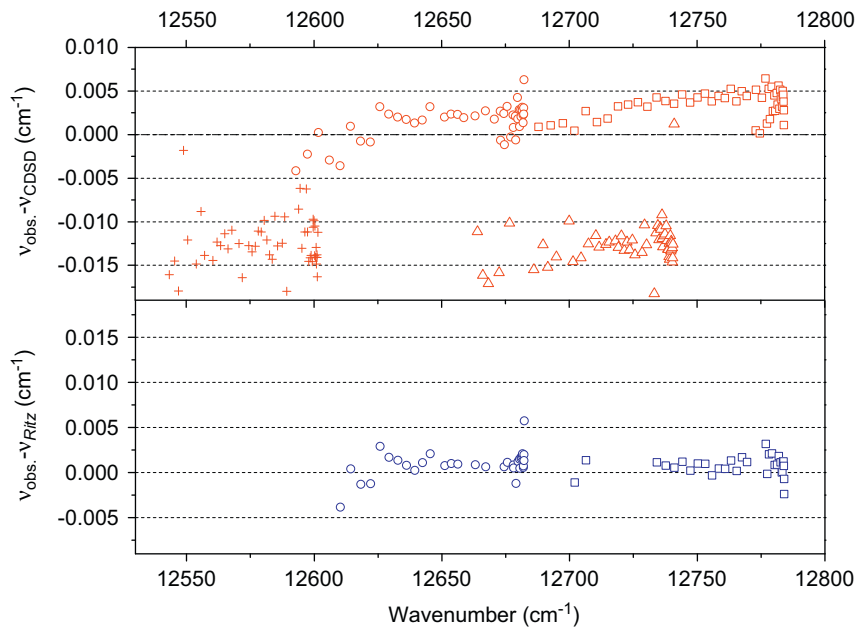


Fig. 4. Comparison of the experimental  $^{12}\text{C}^{16}\text{O}_2$  line positions and those given in HITRAN2008 database [8] (upper panel) and those from Ritz retrieval [17] (lower panel). Square:  $(10^05)_{1,2}-(00^00)_1$ ; circle:  $(10^05)_2-(00^00)_1$ ; triangle:  $(11^15)_{1,2}-(01^10)_1$ ; cross:  $(11^15)_2-(01^10)_1$ .

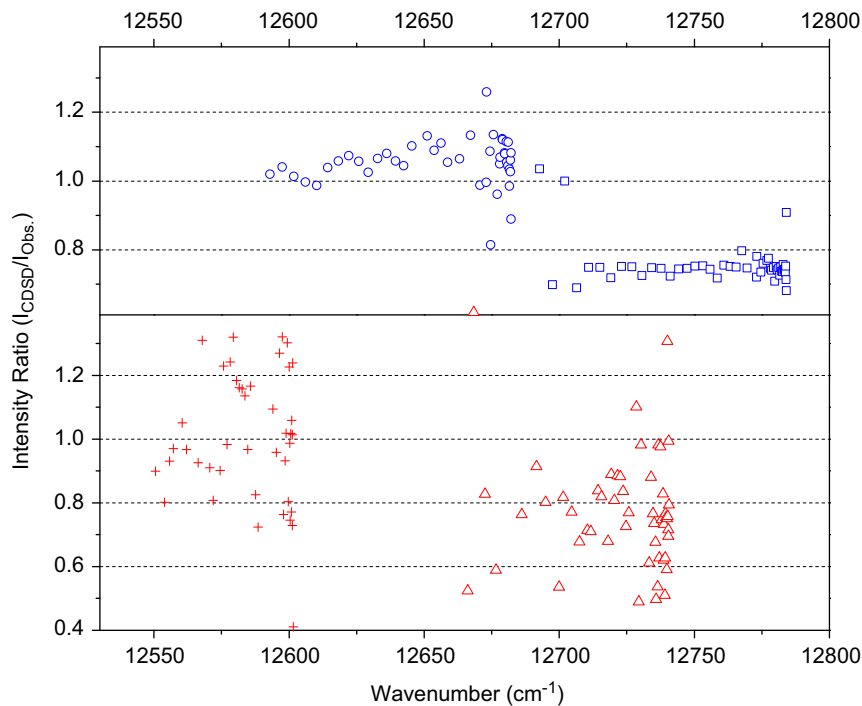


Fig. 5. Comparison of the experimental  $^{12}\text{C}^{16}\text{O}_2$  line intensities and the CDSD calculations. Upper panel: the  $(10^05)_{1,2}-(00^00)_1$  cold bands. Lower panel: the  $(11^15)_{1,2}-(01^10)_1$  hot bands.



$-0.026 \text{ cm}^{-1}$  for the  $R(1)$  line of e–e branch of the  $(11^15)_2-(01^10)_1$  band. The mean deviation for both hot bands is about  $-0.015 \text{ cm}^{-1}$ . Such deviation is consistent with the average residual of the CDS calculations.

The agreement of line intensities between different databases is another criterion to verify the present experimental accuracy. Now, there are three experimental intensities: ICLAS, TDLs and CRDS. Due to the principle of 2f spectrum, the TDLs intensities are not reliable and reproducible. The line intensities given in Refs. [5,6] are 20 times the CDS calculations on average. So only comparisons of the intensity values between the present work and the CDS calculations are presented for cold and hot bands in the upper and lower panels of Fig. 5, respectively. In fact, the  $(10^05)_{1,2}-(00^00)_1$  band intensities have been measured with ICLAS technique by Campargue et al. [4]. Although ICLAS is also very sensitive, due to the overlapped atmospheric water absorption in the 760–850 nm region, the uncertainties of the absolute intensities from ICLAS often exceed 20%. It is clear that the overall agreement is satisfactory for the  $(10^05)_2-(00^00)_1$  and  $(11^15)_2-(01^10)_1$  bands. As for the  $(10^05)_1-(00^00)_1$  and  $(11^15)_1-(01^10)_1$  bands, the CDS calculations are underestimated by 20%. No doubt that the present new experimental results will help for further improvement of the databases and other applications like the studies of the Venus atmosphere [18].

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