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journal homepage: [www.elsevier.com/locate/jqsrt](http://www.elsevier.com/locate/jqsrt)Line positions and N<sub>2</sub>-induced line parameters of the 00°3–00°0 band of <sup>14</sup>N<sub>2</sub><sup>16</sup>O by comb-assisted cavity ring-down spectroscopyG.-L. Liu<sup>a</sup>, J. Wang<sup>a,b</sup>, Y. Tan<sup>a,b</sup>, P. Kang<sup>a</sup>, Z. Bi<sup>c</sup>, A.-W. Liu<sup>a,b,\*</sup>, S.-M. Hu<sup>a</sup><sup>a</sup>Hefei National Laboratory for Physical Sciences at Microscale, University of Science and Technology of China, Hefei 230026, China<sup>b</sup>CAS Center for Excellence in Quantum Information and Quantum Physics, University of Science and Technology of China, Hefei 230026, China<sup>c</sup>National Institute of Metrology, Beijing 100013, China

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## ABSTRACT

Ro-vibrational transitions of the 00°3–00°0 band around 1.52 μm with line intensities in the order of 10<sup>-24</sup> to 10<sup>-23</sup> cm<sup>-1</sup>/(molecule·cm<sup>-2</sup>) have been recorded using a comb-assisted laser-locked cavity ring-down spectrometer with high sensitivity as well as high precision. In total, 88 line positions were determined with a sub-MHz uncertainty (1-σ), better than previous experimental results by 1–2 order of magnitude. N<sub>2</sub>-induced line shape parameters of 20 isolated transitions were derived by using the Voigt profile and the quadratic Speed-Dependent Voigt profile with relative uncertainties of 1–2% (1-σ). Comparisons of the line parameters determined in this work with literature experimental values are given.

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## 1. Introduction

Nitrous oxide (N<sub>2</sub>O) is an important trace constituent in the Earth's atmosphere as one of the major greenhouse gases in the troposphere, with a global warming potential of about 300 times greater than that of CO<sub>2</sub> [1,2]. Its contribution to the “dry” global greenhouse effect amounts to 6% as the Intergovernmental Panel on Climate Change (IPCC) claims [3]. Major efforts contribute the establishment of the network for the Total Carbon Column Observing Network (TCCON) [4,5], which use ground-based Fourier-transform infrared (FTIR) spectrometers distributed all over the world to measure atmospheric absorption spectra with solar radiation. It has been used to monitor the total column concentrations of the major greenhouse components in Earth's atmosphere. Accurate laboratory spectroscopic studies of its absorption line shapes in different spectral ranges are needed to enable satellite-based, ground-based, and airborne remote sensing measurements of N<sub>2</sub>O. The knowledge of the line parameters is essential for atmospheric retrievals and it has been shown for various molecules that non-Voigt effects like line mixing or speed dependence of broadening have to be accounted for in atmospheric retrievals [6,7].

Highly accurate line positions of N<sub>2</sub>O have been obtained by various methods. The results recently reported by Ting et al. in sub-Doppler regime have supplanted most of the previous studies in terms of accuracy of rotational transitions in N<sub>2</sub>O [8]. The R(7) line around 1.28 μm has been measured with the noise-immune cavity-enhanced optical heterodyne molecular spectroscopy (NICE-OHMS) technique [9]. Al Saif et al. measured frequencies of 72 lines in the ν<sub>1</sub> fundamental band of <sup>14</sup>N<sub>2</sub><sup>16</sup>O using a novel spectrometer that relies on locking an external-cavity quantum cascade laser around 7.8 μm to a Tm: based frequency comb at 1.9 μm [10]. Line parameters and the temperature dependences for the corresponding line-broadening coefficients have been derived from the Fourier-transform spectroscopy of nitrous oxide broadened by N<sub>2</sub>, O<sub>2</sub>, and N<sub>2</sub>O in the 4 μm and 8 μm spectral regions [11]. There are also reports for N<sub>2</sub>- and air-broadened line-widths and frequency-shifts for spectral lines in the range of 1800–4800 cm<sup>-1</sup> [11], self-broadened line widths and pressure-induced line shifts of N<sub>2</sub>O in the 1800–2630 cm<sup>-1</sup> region [12], and also N<sub>2</sub>- and O<sub>2</sub>-broadened half-widths and their temperature dependences between 216 and 296 K for lines in the 4.5 μm region corresponding to the ν<sub>3</sub> fundamental band [13]. Vitcu et al. investigated the 0310–0110 parallel Q-branch of N<sub>2</sub>O at 297 K in the pressure range of 11–30 Torr and determined self-broadened, pressure-induced shifts, and line-mixing coefficients [13]. Loos et al. reported highly accurate measurements of air-broadening, pressure-shift, speed dependence, and Rosenkranz line-mixing parameters for transitions in the ν<sub>3</sub> fundamental band of N<sub>2</sub>O [2]. Recently, the 00°2–00°0

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band used to monitor nitrous oxide by the TCCON network has been studied by Werwein et al. [14,15] at 2.26  $\mu\text{m}$ . The self- and air-induced line shape parameters were obtained with high accuracy for 41 lines of R branch with the maximum rotational quantum number of 40.

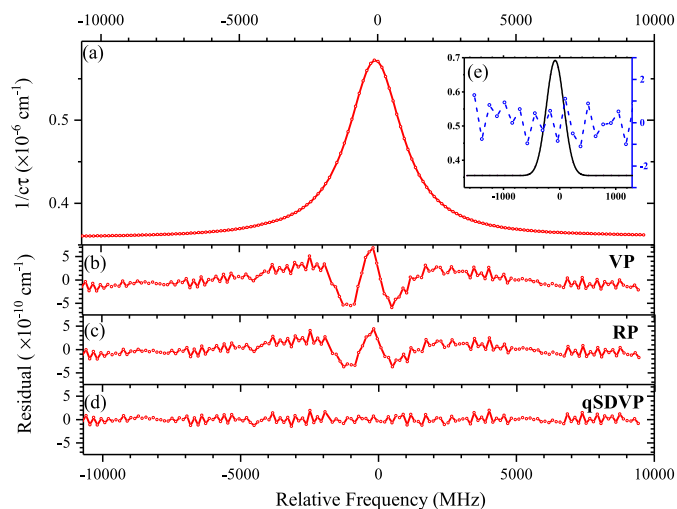
In this study, we present the study on the 00<sup>3</sup> – 00<sup>0</sup> band of nitrous oxide, including measurements of 88 lines at low pressures, and N<sub>2</sub>-broadened spectral line shapes of 20 well isolated lines. Line positions were determined and the N<sub>2</sub>-induced line broadening and shifting coefficients were derived from fit of the spectra using different line profiles.

## 2. Experimental details

The experimental setup is similar to the laser-locked cavity ring-down spectrometer described in Refs [16–20]. Briefly, the structure of the setup is as follows: the s-polarization probe laser is an external cavity diode laser (ECDL, Optica DL Pro-1550) which is locked to a temperature-stabilized ring-down (RD) Invar cavity using the Pound-Drever-Hall (PDH) method. The RD cavity is composed of a pair of high-reflectivity (99.996% at 1.5 – 1.7  $\mu\text{m}$ , Layertec GmbH Inc.) mirrors with a distance of 110.8 cm, leading to a free spectral range (FSR) of 135.27 MHz, a finesse of 78,000 and a mode width of about 1.6 kHz. The RD cavity is thermal-stabilized at 298.8 K with a fluctuation less than 50 mK. Its absolute frequency is calibrated by an optical frequency comb which is synthesized by an Er: fiber oscillator operated at 1.56  $\mu\text{m}$ . The repetition frequency ( $f_R \approx 180$  MHz) and carrier offset frequency ( $f_0$ ) of the comb are locked to accurate radio-frequency sources, both referenced to a Global Positioning System (GPS)-discipline rubidium clock (SRS FS725). The beat signals between the probe laser and the comb were recorded by a frequency counter (Agilent 53181A).

A separated p-polarization probe laser beam, frequency shifted by an acousto-optic modulator (AOM) and a fiber electro-optic modulator (EOM), is coupled into the RD cavity from the other side of the cavity and used for cavity ring-down spectroscopy (CRDS) measurements. The s- and p-polarization beams were separated with a combination of polarizing waveplates and Glan-Taylor prism for frequency locking and spectral probing. The AOM serves as a beam chopper, which is triggered by an external rectangle wave to shut off the CRDS-probing beam to initial a ring-down event. The ring-down curve is fit by an exponential decay function to derive the decay time  $\tau$ , and the sample absorption coefficient  $\alpha$  is determined from the change of the cavity loss rate:  $\alpha = (c\tau)^{-1} - (c\tau_0)^{-1}$ , where  $c$  is the speed of light, and  $\tau$  and  $\tau_0$  are decay times of the cavity with and without sample, respectively.

The Doppler-limited spectra were recorded with natural nitrous oxide sample (Nanjing ShangYuan 99.0% stated purity) at three pressures (1.0, 3.0, and 4.0 Pa) depending on the absorption intensities of the measured lines. In total, 88 lines with intensities stronger than  $1 \times 10^{-24}$   $\text{cm}^{-1}/(\text{molecule cm}^{-2})$  were studied. The N<sub>2</sub> gas sample with high stated purity of 99.99% (Nanjing ShangYuan) was used as the buffer gas. For the N<sub>2</sub>-broadened spectra, the total pressures varied from 1.0 kPa to 50.0 kPa with the N<sub>2</sub>O volume mixing ratios less than 0.1%. Sample pressures were measured by capacitance gauges, Pfeiffer Vacuum CCR 372 (full range 13.3 kPa) with a stated accuracy of 0.15%, and Shanghai Zhentai Instruments Co. CPCA-140Z (full range 100 kPa) with stated accuracy of 0.5%. The absorption spectra of each line at each experimental condition was recorded 30 times to reach enough signal-to-noise level. To avoid the interference from neighbor absorptions of other molecules and isotopologues, the N<sub>2</sub>-broadened spectra of 20 well-isolated transitions in the 0003 – 0000 band were measured in this work. Note that the FSR of the ring-down cavity was measured for each line with high pressure samples to correct the frequency shift due to dispersion.



**Fig. 1.** Examples of CRDS-spectrum for the P(19) line recorded with sample pressures of 1 Pa (a) and 50 kPa (e), along with the residuals retrieved with Voigt profile (b), Rautian profile (c), and quadratic speed-dependent Voigt profile (d). Note that the spectra refer to the left vertical axis, while the residuals refer to the right vertical axis. A factor of 10,000 enlargement was applied in the right vertical axis in the (e) layer.

## 3. Line positions

### 3.1. Line positions determination

The Doppler-limited spectra were fitted using a least-square fitting program assuming a Voigt profile with the Gaussian width fixed to the theoretical value of the Doppler broadening. The inserted plot of Fig. 1(e) shows the spectra of P(19) line recorded with a sample pressure of 1.0 Pa together with the fitting residuals of the measured spectra, which illustrate a noise equivalent absorption coefficient at the  $7.5 \times 10^{-11}$   $\text{cm}^{-1}$  level.

The self-induced shifts of studied transitions in this work have not been reported in literatures. As far as we know, the self-induced shifts have been reported for 177 lines of ten vibrational bands below 4400  $\text{cm}^{-1}$  in Refs [12,14,21]. The average value of the self-induced shifts was found to be  $-0.0015(6)$   $\text{cm}^{-1}/\text{atm}$  (1 atm = 101 325.0 Pa) encompassing all 136 transitions in nine vibrational bands below 2360  $\text{cm}^{-1}$  by Toth [12], which differs from the value  $-0.00405$   $\text{cm}^{-1}/\text{atm}$  adopted by Pollock et al. [21]. While the self-induced shifts show linear depending on  $J$  values for the 0002 – 0000 band by Werwein et al. [14], which vary between  $-0.00228$  and  $-0.00641$   $\text{cm}^{-1}/\text{atm}$ . The maximum absolute value of the self-induced shift is assumed not exceeding 0.01  $\text{cm}^{-1}/\text{atm}$ , which is about 12 kHz at a pressure of 4.0 Pa. Therefore, the self-induced shifts of the line center can be neglected in our Doppler-limited spectra.

The position of P(40) is determined to be 195 800 327.99 MHz ( $1 \text{ cm}^{-1} = 29\,979.2458 \text{ MHz}$ ) and the uncertainty budget is presented in Table 1. A statistical uncertainty of 0.08 MHz was obtained by averaging the results derived from 20 spectra recorded in half an hour. The frequency comb used for calibration has an uncertainty of 0.4 kHz due to the long term stability of  $2 \times 10^{-12}$  from the Rb clock. The frequency drift due to the thermal expansion of the cavity was smaller than 0.02 MHz in each scan according to the observation in Ref. [20]. The uncertainty in the driving frequencies of the AOM and EOM are negligible. As discussed above, an uncertainty of 0.01 MHz was given for possible contribution from the pressure shift at pressures less than 4.0 Pa. Since the amplitude of the fitting residual around peak center is at the noise level, we estimate that the shift due to the asymmetry in the line

**Table 1**  
1- $\sigma$  Uncertainty budget of the P(40) line in the  $3\nu_3$  band of  $^{14}\text{N}_2^{16}\text{O}$  (in MHz).

Source	Uncertainty	
	Type A	Type B
Statistical	0.08	
Frequency comb		<0.001
Cavity drift		0.02
EOM frequency		<0.001
AOM frequency		<0.001
Pressure shift		0.01
Line profile asymmetry		0.15
Total	0.17	

profile, if any, should be below 0.15 MHz, as the full Doppler width ( $\sim 360$  MHz) divided by the typical signal-to-noise ratio of 2400. The overall uncertainty (1- $\sigma$ , throughout this paper) of the P(40) line position is 0.17 MHz. In total, 88 lines were measured with the maximum  $J''$  value of 47 for the  $3\nu_3$  band of  $^{14}\text{N}_2^{16}\text{O}$ . Their line positions are given in Table 2. The statistical and systematic uncertainties are also included in Table 2.

### 3.2. Ro-vibrational spectroscopic constants

Rotational energies of the  $3\nu_3$  upper vibrational state can be given by the usual formula:

$$E(J) = G_v + B_v J(J+1) - D_v J^2(J+1)^2 + H_v J^3(J+1)^3 + \dots \quad (1)$$

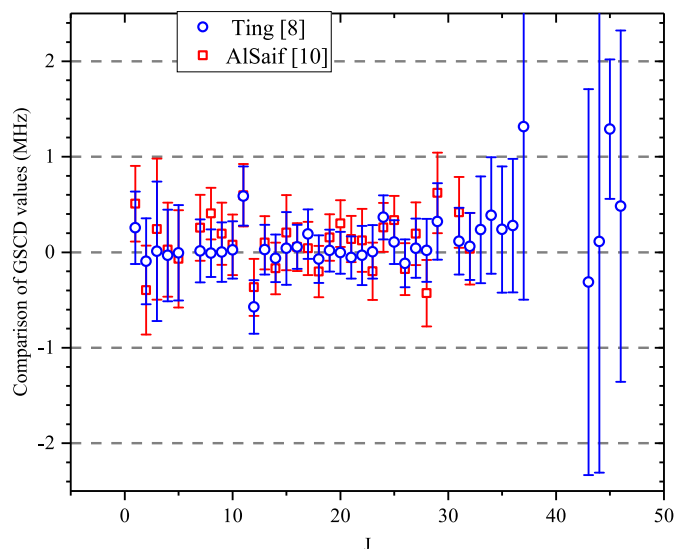
Where  $J$  is the angular momentum quantum number,  $G_v$  is the vibrational term,  $B_v$ ,  $D_v$ , and  $H_v$  are rotational and centrifugal distortion constants. The ro-vibrational constants can be derived from a fit of the energies given in Table 2. The ground state constants were constrained to the values given in Ref [8]. The spectroscopic constants are determined to be 197 289 025.234(56) MHz, 12,250.59678(29) MHz, 5.24157(38) kHz, and 1.74(14) mHz for  $G_v$ ,  $B_v$ ,  $D_v$ , and  $H_v$ , respectively. The root-mean-square deviation is 0.25 MHz, being consistent with the line position uncertainty.

### 3.3. Ground state combination difference comparison

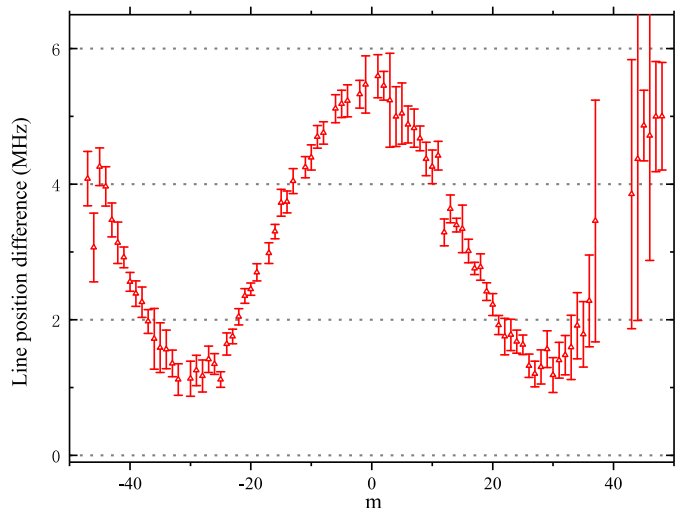
Ground state combination difference (GSCD) between the  $P(J+1)$  and  $R(J-1)$  transitions sharing the same  $J$  upper rotational state is independent on the upper energy level. The quantity value of GSCD can be calculated with the equation:  $\Delta(J) = R(J-1) - P(J+1)$ . The differences between the GSCD values obtained from the saturated absorption spectroscopy by Ting et al. [8], by Al Saif et al. ( $\nu=1$ ) [10], and those determined in this work are presented in Fig. 2 for a comparison. The averaged values with standard deviations ( $1\sigma$ ) are  $0.13 \pm 0.34$  and  $0.11 \pm 0.28$  MHz for the differences from Ting's [8] and Al Saif's [10] values, respectively, which coincide with the line position uncertainty.

### 3.4. Comparison to the line positions in HITRAN

The line-by-line parameters of  $3\nu_3$  band have been included in the HITRAN2004 database [22] for the first time with Toth's linelist [23]. The line positions and intensities have not been updated in HITRAN2016 [24]. The deviations from HITRAN values are plotted in Fig. 3. The differences show clear  $J$  dependence. The averaged difference with standard deviation ( $1\sigma$ ) is  $3.08 \pm 1.43$  MHz. The stated uncertainties are  $0.001 - 0.0001 \text{ cm}^{-1}$  (3–30 MHz) given in the HITRAN database, being consistent with the comparison given here.



**Fig. 2.** Comparisons of GSCD values obtained from Ting et al. [8] and Al Saif et al. [10] and those determined in this study with the rotational quantum number  $J$  of the upper state.



**Fig. 3.** Comparisons of line positions of  $^{14}\text{N}_2^{16}\text{O}$  for 88 transitions of  $3\nu_3$  band from the values in HITRAN2016 database with the quantum number  $m$  of the lower state ( $m$  is the  $-J$  in the  $P$ -branch and  $J+1$  in the  $R$ -branch).

## 4. Nitrogen-induced line shape parameters

$\text{N}_2$ -broadened spectra were fitted with the Voigt profile, Rautian profile and the quadratic Speed-Dependent Voigt (qSDV) profile, respectively. The nonlinear spectra fitting program was written based on the line shape model proposed by Ngo et al. [25]. The line center, intensity, collision broadening width, Dicke narrowing coefficient, speed-dependent parameters and the linear polynomial parameters for baseline were derived from the least-square fit. Note that the speed-dependence for shifting parameters were set to be zero in the fit. As shown in Fig. 1(a-d), the spectra of P(19) line was recorded at 50 kPa and fitted with different line profiles. The W-shaped structure of the fitting residuals presents in the fit of the Voigt profile, especially at high pressures. If the speed-dependence was neglected, the remained residuals from the fit of Rautian profile still showed obvious deviations above the noise level while the qSDV profile could fit the experimental spectra quite well to the noise level. The pressure-induced line shape parameters of a transition corresponds to the slope of the

**Table 2**

Line positions of the  $3\nu_3$  band of  $^{14}\text{N}_2^{16}\text{O}$  and the derived upper level energies (in MHz). Ground state rotational constants are from Ref. [8].

$J''$	$P(J'')$	Uncertainty		$J''$	$R(J'')$	Uncertainty		$J'$	$E'$
		Statis.	Sys.			Statis.	Sys.		
P(1)	197,263,901.97(42)	0.12	0.40					0	197,289,025.22(42)
P(2)	197,238,156.83(21)	0.06	0.20	R(0)	197,313,526.19(32)	0.09	0.31	1	197,313,526.32(40)
P(3)	197,211,789.70(40)	0.15	0.34	R(1)	197,337,405.40(21)	0.06	0.20	2	197,362,528.60(45)
P(4)	197,184,801.07(24)	0.12	0.21	R(2)	197,360,662.02(69)	0.15	0.68	3	197,436,031.64(73)
P(5)	197,157,190.83(20)	0.10	0.18	R(3)	197,383,296.29(44)	0.11	0.43	4	197,534,035.13(48)
P(6)	197,128,959.14(21)	0.08	0.19	R(4)	197,405,307.90(45)	0.10	0.44	5	197,656,538.47(50)
P(7)				R(5)	197,426,696.76(27)	0.08	0.26	6	197,803,541.04(27)
P(8)	197,070,631.88(17)	0.07	0.15	R(6)	197,447,462.84(28)	0.07	0.27	7	197,975,042.18(33)
P(9)	197,040,536.67(17)	0.06	0.16	R(7)	197,467,606.04(18)	0.06	0.17	8	198,171,041.00(25)
P(10)	197,009,820.54(19)	0.05	0.18	R(8)	197,487,126.13(25)	0.06	0.24	9	198,391,536.43(31)
P(11)	196,978,483.68(16)	0.05	0.15	R(9)	197,506,023.07(25)	0.05	0.24	10	198,636,527.41(30)
P(12)	196,946,526.46(23)	0.12	0.20	R(10)	197,524,296.45(21)	0.05	0.21	11	198,906,012.64(43)
P(13)	196,913,948.16(19)	0.04	0.18	R(11)	197,541,947.56(20)	0.05	0.19	12	199,199,991.01(40)
P(14)	196,880,749.75(16)	0.04	0.16	R(12)	197,558,973.63(20)	0.07	0.19	13	199,518,460.12(26)
P(15)	196,846,931.08(20)	0.04	0.19	R(13)	197,575,376.71(15)	0.04	0.15	14	199,861,419.25(25)
P(16)	196,812,492.54(15)	0.04	0.15	R(14)	197,591,156.05(35)	0.05	0.35	15	200,228,866.45(38)
P(17)	196,777,433.93(15)	0.04	0.15	R(15)	197,606,311.48(17)	0.07	0.16	16	200,620,799.64(23)
P(18)	196,741,755.69(21)	0.05	0.20	R(16)	197,620,842.98(15)	0.04	0.15	17	201,037,217.00(28)
P(19)	196,705,457.34(16)	0.06	0.15	R(17)	197,634,750.33(19)	0.07	0.18	18	201,478,116.03(25)
P(20)	196,668,539.95(16)	0.04	0.15	R(18)	197,648,033.60(15)	0.05	0.15	19	201,943,495.02(22)
P(21)	196,631,003.04(15)	0.05	0.15	R(19)	197,660,692.52(16)	0.07	0.15	20	202,433,351.18(22)
P(22)	196,592,846.96(16)	0.05	0.15	R(20)	197,672,727.10(15)	0.05	0.15	21	202,947,682.15(22)
P(23)	196,554,071.79(16)	0.05	0.15	R(21)	197,684,137.07(27)	0.08	0.26	22	203,486,485.19(31)
P(24)	196,514,677.68(16)	0.05	0.16	R(22)	197,694,922.38(23)	0.05	0.22	23	204,049,757.54(28)
P(25)	196,474,665.20(16)	0.06	0.15	R(23)	197,705,083.04(17)	0.05	0.16	24	204,637,496.60(30)
P(26)	196,434,033.50(16)	0.06	0.15	R(24)	197,714,618.89(16)	0.06	0.15	25	205,249,698.81(23)
P(27)	196,392,783.49(19)	0.08	0.18	R(25)	197,723,529.93(17)	0.06	0.16	26	205,886,361.46(26)
P(28)	196,350,915.32(24)	0.07	0.23	R(26)	197,731,815.71(19)	0.06	0.18	27	206,547,481.09(31)
P(29)	196,308,428.95(22)	0.09	0.20	R(27)	197,739,476.50(25)	0.07	0.24	28	207,233,054.42(34)
P(30)	196,265,324.61(29)	0.10	0.24	R(28)	197,746,511.77(27)	0.07	0.26	29	207,943,077.73(43)
P(31)				R(29)	197,752,922.32(26)	0.08	0.25	30	208,677,547.80(26)
P(32)	196,177,262.69(23)	0.12	0.20	R(30)	197,758,707.19(26)	0.09	0.25	31	209,436,460.53(36)
P(33)	196,132,305.27(20)	0.13	0.15	R(31)	197,763,866.54(29)	0.10	0.27	32	210,219,811.96(36)
P(34)	196,086,730.62(29)	0.14	0.25	R(32)	197,768,400.19(48)	0.11	0.46	33	211,027,598.20(58)
P(35)	196,040,538.87(37)	0.16	0.33	R(33)	197,772,308.27(49)	0.12	0.47	34	211,859,815.19(65)
P(36)	195,993,730.04(45)	0.17	0.41	R(34)	197,775,590.82(48)	0.13	0.46	35	212,716,458.64(67)
P(37)	195,946,304.12(17)	0.05	0.17	R(35)	197,778,247.09(68)	0.15	0.66	36	213,597,523.74(72)
P(38)	195,898,261.79(23)	0.06	0.22	R(36)	197,780,276.7(18)	0.2	1.8	37	214,503,006.1(19)
P(39)	195,849,602.95(19)	0.07	0.17	R(37)	-			38	215,432,902.40(22)
P(40)	195,800,327.99(17)	0.08	0.15	R(38)	-			39	216,387,206.32(20)
P(41)	195,750,436.47(17)	0.07	0.15	R(39)	-			40	217,365,912.99(21)
P(42)	195,699,929.32(32)	0.28	0.15	R(40)	-			41	218,369,018.14(35)
P(43)	195,648,806.27(25)	0.12	0.22	R(41)	-			42	219,396,516.17(30)
P(44)	195,597,067.60(29)	0.14	0.25	R(42)	197,779,313.4(20)	0.4	1.9	43	220,448,402.1(20)
P(45)	195,544,713.65(28)	0.12	0.25	R(43)	197,776,960.1(24)	0.4	2.3	44	221,524,670.1(24)
P(46)	195,491,745.71(51)	0.21	0.46	R(44)	197,773,980.77(52)	0.15	0.50	45	222,625,315.7(10)
P(47)	195,438,160.69(40)	0.23	0.33	R(45)	197,770,374.8(18)	0.6	1.7	46	223,750,331.5(19)
				R(46)	197,766,142.35(81)	0.21	0.79	47	224,899,713.01(84)
				R(47)	197,761,283.31(79)	0.25	0.76	48	226,073,454.37(83)

respective linear regressions. Fig. 4 shows the Lorentzian widths (upper panel) and the line centers (lower panel) with respect to the total pressures for R(7) (dot line) and P(19) (dash line) transitions. It is clear that the broadening coefficients retrieved from the qSDV profile (blue) are about 3.5% larger than the values from the Voigt profile (red). The fitted lines with line shape parameters cross the zero point. The self-induced components are negligible since the nitrous oxide volume mixing ratios are less than 0.1%. Table 3 summarized the retrieved  $\text{N}_2$ -broadening and shift parameters by Voigt profile and qSDV profile, as well as the speed-dependence parameter  $\gamma_2$  from linear fit of  $\Gamma_0$ ,  $\Delta_0$  and  $\Gamma_2$  resulting from line shape models on pressure. Due to the experimental limitation, we did not observe pressure induced shift parameters for transitions P(7) and P(31). These parameters were all given at 298.8 K which is the stabilized temperature of the ring-down cavity. The uncertainty of the line shape parameters retrieved in this work results from both temperature and pressure. The pressure gauges were calibrated at National Institute of

Metrology, China. The absolute relative uncertainties at different pressure series are 0.25% (<13.3 kPa) and 0.5% (>13.3 kPa). The temperature uncertainty of the ring-down cavity was estimated to be 0.05 K at maximum. For the temperature dependence of the line shape parameters modeled by the power law  $X(T, P) = P \cdot X(T_{\text{ref}}) \cdot (T_{\text{ref}}/T)^n$ , the assumed scaling factor for temperature dependence would be 99.3% for  $n = 0.75$  compared to the reference temperature 296 K. Therefore, the total errors given in Table 3 were calculated as a sum of the described uncertainties from experimental error sources and the statistical errors from the fitting procedure.

The pressure broadening and shift coefficients were fitted using a third-order polynomial function:

$$X(m) = a_0 + a_1|m| + a_2|m|^2 + a_3|m|^3, 2 \leq m \leq 45$$

$X$  represents for  $\gamma_0$  ( $\text{N}_2$ -induced broadening coefficient) and  $\delta_0$  ( $\text{N}_2$ -induced shift coefficient) with  $m = -J$  and  $m = J + 1$  for the P and R branch, respectively. Note that the broadening parameters for  $\text{N}_2\text{O}$  would only be extrapolated for  $m$  up to 45. As shown in

**Table 3**

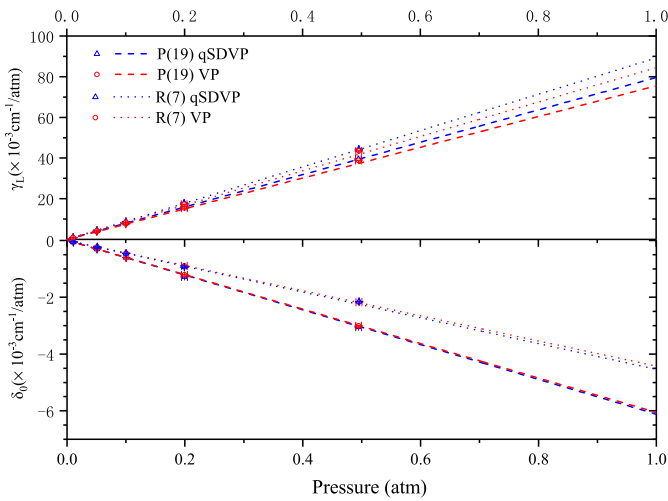
$N_2$ -broadening and shift parameters with  $1-\sigma$  uncertainty for the  $00^3 - 00^0$  band of  $^{14}N_2^{16}O$  at  $1.54\ \mu m$  at temperature 298.8 K.

Line	$\gamma_0$ (cm <sup>-1</sup> /atm)		$\gamma_2$ (cm <sup>-1</sup> /atm)		$\delta_0$ (cm <sup>-1</sup> /atm)	
	VP	qSDVP	qSDVP	VP	VP	qSDVP
P(45)	0.07010(77)	0.07281(43)	0.00632(33)	-0.006900(56)	-0.007034(38)	
P(41)	0.07045(70)	0.07318(38)	0.00602(12)	-0.006811(42)	-0.006965(41)	
P(31)	0.07185(48)	0.07494(39)	0.00677(21)	-	-	
P(28)	0.07191(70)	0.07576(43)	0.00704(13)	-0.00650 (10)	-0.00651 (12)	
P(22)	0.07593(89)	0.07804(41)	0.00749(14)	-0.006353(41)	-0.006405(97)	
P(19)	0.07755(93)	0.07980(41)	0.00800(17)	-0.006098(34)	-0.00624 (11)	
P(18)	0.07780(61)	0.08028(41)	0.00808(16)	-0.006079(40)	-0.006273(47)	
P(12)	0.08242(66)	0.08526(47)	0.00874(19)	-0.005637(40)	-0.005734(66)	
P(9)	0.0854(10)	0.08811(45)	0.00879(19)	-0.005387(62)	-0.00565 (13)	
P(7)	0.08733(65)	0.09018(47)	0.00910(21)	-	-	
P(3)	0.09354(78)	0.09582(62)	0.00957(60)	-0.00424 (14)	-0.00439 (14)	
R(0)	0.0995 (10)	0.10277(73)	0.01067(71)	-0.003037(79)	-0.00289 (14)	
R(3)	0.08908(99)	0.09345(58)	0.00909(49)	-0.003932(88)	-0.00394 (12)	
R(5)	0.0889(11)	0.09121(52)	0.00889(24)	-0.004194(36)	-0.00432 (13)	
R(7)	0.0865(11)	0.08907(53)	0.00898(34)	-0.004408(32)	-0.004537(94)	
R(12)	0.0815(10)	0.08426(48)	0.00871(19)	-0.004953(29)	-0.005003(37)	
R(15)	0.07904(97)	0.08164(43)	0.00849(09)	-0.005266(36)	-0.005357(49)	
R(17)	0.07556(74)	0.07989(43)	0.00813(14)	-0.005536(51)	-0.005607(62)	
R(19)	0.07647(88)	0.07883(42)	0.00787(12)	-0.005785(39)	-0.005938(56)	
R(21)	0.07561(89)	0.07782(41)	0.00773(18)	-0.005998(40)	-0.006064(68)	

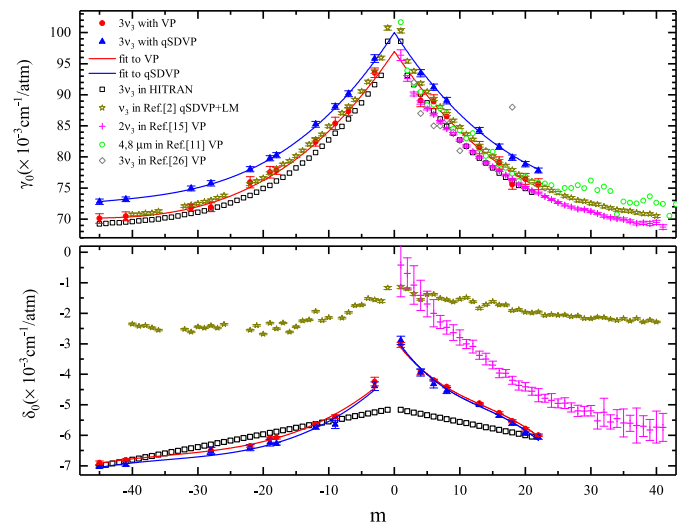
**Table 4**

Parameters for the polynomial function in Eq. (2) used to fit  $N_2$ -broadening and shift parameters retrieved by different line shape models as functions of  $m$ .

	$\gamma_0$ (cm <sup>-1</sup> /atm) for P and R branch			$\delta_0$ (cm <sup>-1</sup> /atm) for P branch		$\delta_0$ (cm <sup>-1</sup> /atm) for R branch	
	HITRAN [22]	This work (VP)	This work(qSDVP)	This work (VP)	This work (qSDVP)	This work (VP)	This work (qSDVP)
$a_0$	0.0964	0.09697(95)	0.10002(60)	$-3.90(21) \times 10^{-3}$	$-3.92(22) \times 10^{-3}$	$-2.86(14) \times 10^{-3}$	$-2.75(25) \times 10^{-3}$
$a_1$	$-1.72 \times 10^{-3}$	$-1.56(17) \times 10^{-3}$	$-1.63(11) \times 10^{-3}$	$-1.98(32) \times 10^{-4}$	$-2.14(31) \times 10^{-4}$	$-2.87(40) \times 10^{-4}$	$-3.22(79) \times 10^{-4}$
$a_2$	$3.81 \times 10^{-5}$	$3.01(84) \times 10^{-5}$	$3.44(53) \times 10^{-5}$	$5.1(15) \times 10^{-6}$	$5.7(14) \times 10^{-6}$	$1.39(35) \times 10^{-5}$	$1.64(72) \times 10^{-5}$
$a_3$	$-2.96 \times 10^{-7}$	$-1.9(12) \times 10^{-7}$	$-2.56(74) \times 10^{-7}$	$-4.9(21) \times 10^{-8}$	$-5.5(19) \times 10^{-8}$	$-3.40(93) \times 10^{-7}$	$-4.0(19) \times 10^{-7}$



**Fig. 4.** Linear regressions of the Lorentzian widths (upper panel) and the line centers (lower panel) with respect to the total pressures for R(7) (dot line) and P(19) (dash line) transitions. The line shape parameters retrieved with the qSDVP profile and Voigt profile (VP) are shown in blue and red color, respectively. For the purpose of a better illustration, the respective Doppler limited line positions of nitrous oxide were subtracted from the fitted line positions. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 5.** The pressure broadening and shift parameters retrieved in this work from two different line shape models were plotted on the upper and lower panels, as well as the air-broadening and shift parameters taken from HITRAN database (black square), Ref. [2] (fitted from qSDVP with line-mixing, brown star), Ref. [15] (fitted from VP, pink cross), the  $N_2$ -broadening parameters from Ref. [11] (fitted from VP, green open circle) and Ref. [26] (fitted from VP, open diamond); and a third-order polynomial function were used to fit as functions of  $m$ .

**Fig. 5.** the pressure broadening and shift parameters retrieved in this work from two different line shape models were plotted in the upper and lower panels and fitted to Eq. 2 as a function of  $m$ . Table 4 summarized the  $m$ -dependence parameters for  $N_2$ -broadening and shift coefficients which were fitted using the third-

order polynomial function described above. The P and R branch polynomials for the  $N_2$ -broadening coefficients were constrained to have the same values because the  $m$ -dependence for the P and R branches shows a symmetric pattern. For the region around  $m$  equal to zero, the polynomial fit did not represent well. The



comparison between  $\gamma_0$  retrieved in this work from both Voigt and qSDV profile shows in Fig. 5, and in general, the  $\gamma_0$  retrieved from qSDVP were slightly larger than that from Voigt profile. Furthermore, the  $\gamma_{\text{air}}$  value taken from HITRAN database [24] as well as the air-broadening  $\gamma_0$  value retrieved from qSDVP with line-mixing for the  $\nu_3$  band in Ref. [2] and that for the  $2\nu_3$  band in Ref. [15] shows good agreement with slight difference contributed from the  $\text{O}_2$ -broadening proportion and temperature dependence different from the reference temperature at 296 K. The  $\text{N}_2$ -broadening parameters taken from Refs. [11,26] retrieved with Voigt profile were also shown in Fig. 5, which are about 1–2% different from our measurements within the experimental uncertainties. As for the pressure-induced line shift vs. the  $m$  quantum number shown on the lower panel of Fig. 5, a clear asymmetry in the  $m$ -dependence for P and R branches was presented. Therefore, separated polynomial fit was performed according to Eq. 2, for the P and R branches, respectively. The same comparison between this work and the HITRAN database [24] shows clear deviations in both P and R branches. And the comparisons to the transitions of the  $\nu_3$  and  $2\nu_3$  bands of pressure-induced shift parameters present some tendency on vibrational quantum number.

## 5. Conclusion

We present the absorption spectroscopic analysis of the  $00^0_3 - 00^0_0$  band of  $^{14}\text{N}_2^{16}\text{O}$  near  $1.54\mu\text{m}$  recorded by a laser-locked cavity ring-down spectrometer referenced to an optical frequency comb. Doppler limited line positions were determined with sub-MHz uncertainty for 88 transitions.  $\text{N}_2$ -induced broadening and shift coefficients were obtained with a relative uncertainty of about 1% for 20 isolated transitions by using the Voigt and qSDV profile models. Deviations of 1–5 MHz were found between the line positions determined in this work and those given in the HITRAN line list based on FTS measurements by Toth [23]. The  $\text{N}_2$ -induced broadening coefficients for the  $3\nu_3$  band obtained in the present study are in good agreement with most of the literature values listed above for other bands [2,11,15,26].

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## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:10.1016/j.jqsrt.2019.03.004.

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