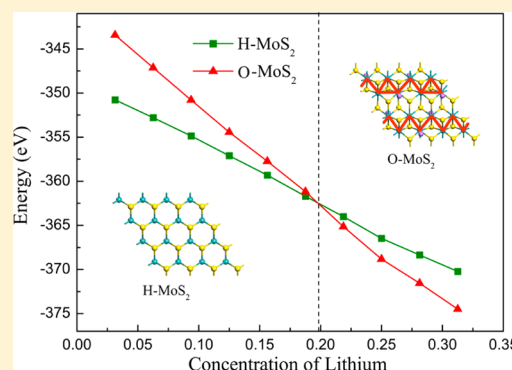


Structures and Phase Transition of a MoS<sub>2</sub> MonolayerM. Kan,<sup>†</sup> J. Y. Wang,<sup>‡</sup> X. W. Li,<sup>§</sup> S. H. Zhang,<sup>§</sup> Y. W. Li,<sup>†</sup> Y. Kawazoe,<sup>||</sup> Q. Sun,<sup>\*,†,§,⊥</sup> and P. Jena<sup>⊥</sup><sup>†</sup>Department of Materials Science and Engineering, <sup>‡</sup>College of Chemistry and Molecular Engineering, and <sup>§</sup>Center for Applied Physics and Technology, Peking University, Beijing 100871, China<sup>||</sup>Institute for Material Research, Tohoku University, Sendai 980-8577, Japan<sup>⊥</sup>Department of Physics, Virginia Commonwealth University, Richmond, Virginia 23284, United States

**ABSTRACT:** As an inorganic cousin of graphene, MoS<sub>2</sub> monolayer has attracted considerable attention. However, a full understanding of its structure and stability is still lacking due to its dependence on experimental synthesis conditions. Using first-principle calculations combined with Boltzmann transport equation, we have extensively studied the geometry, energetics, electronic structure, optical absorption, and carrier mobility of various phases of MoS<sub>2</sub>. We have not only identified the stable phases of a MoS<sub>2</sub> monolayer, but also clarified the specific conditions under which different phases are formed. The possible pathways for transitions among different phases are also discussed.



## I. INTRODUCTION

The study of two-dimensional (2D) monolayer materials has been a topic of current interest since the first report of the successful fabrication of a 2D single layered graphene by Novoselov et al. in 2004.<sup>1</sup> Among these, molybdenum disulfide (MoS<sub>2</sub>) sheet, a transition metal dichalcogenide (TMD), has attracted considerable attention due to its important role in lithium ion battery (LIB),<sup>2</sup> flexible electronic device,<sup>3</sup> photoluminescence,<sup>4</sup> valleytronics,<sup>5,6</sup> and field effect transistors. The technological importance of MoS<sub>2</sub> is further enhanced due to its exceptional properties such as amplification of electrical signals at room temperature with much less power consumption than traditional silicon or even graphene, high room temperature current on/off ratios, ultralow standby power dissipation, and high mobility rate comparable to silicon.<sup>7</sup>

Similar to graphene, monolayer MoS<sub>2</sub> can be extracted from the bulk using mechanical or solvent-based exfoliation method.<sup>7,8</sup> The former method always leads to a 2D trigonal prismatic phase (labeled as H-MoS<sub>2</sub>), which is found to be a semiconductor<sup>9</sup> with a direct band gap between the occupied  $d_{z^2}$  and the empty  $d_{x^2-y^2,xy}$  orbitals. The H-MoS<sub>2</sub> phase has the space group of  $P6/mmc$  and is believed to be a stable configuration under normal condition.<sup>10</sup> On the other hand, the solvent-based exfoliation method<sup>11,12</sup> results in different octahedral coordinated phases. The dependence of the structure on experimental synthesis method has been puzzling scientists for a long time. For example, the structure of MoS<sub>2</sub> was originally proposed to be TiS<sub>2</sub> type with nearly ideal octahedral configuration with each Mo atom bonded with six S atoms, which is referred to as T-MoS<sub>2</sub>.<sup>13–15</sup> X-ray diffraction study suggested a tetramerization model,<sup>16</sup> while another

study<sup>17</sup> showed that the Mo atoms are shifted from their positions to form trigonal clusters in the octahedral MoS<sub>2</sub>. The AFM image of a single layer MoS<sub>2</sub> on mica indicated no superlattice formation,<sup>18</sup> while a STM study of the surface layer of restacked MoS<sub>2</sub> indicated a superstructure caused by the formation of zigzag chains.<sup>19</sup> Later, electron crystallography study<sup>12</sup> suggested that the restacked MoS<sub>2</sub> is more like WTe<sub>2</sub> with zigzag Mo–Mo chains rather than that of TiS<sub>2</sub>. This is labeled as ZT-MoS<sub>2</sub>. Furthermore, Rocquefelte et al.<sup>20</sup> proposed that lithium inserted MoS<sub>2</sub> possesses distorted octahedral coordinated structure with rhombus shape connected Mo–Mo chains, which is referred to as DT-MoS<sub>2</sub>. Recently, significant progress has been achieved in the fabrication of MoS<sub>2</sub> nanotubes with octahedral coordination under substitutional rhenium doping.<sup>21</sup> Eda et al.<sup>22</sup> have synthesized a single layer of exfoliated MoS<sub>2</sub> consisting of both trigonal prismatic and octahedral phases with matching lattices so that they form chemically homogeneous atomic and electronic heterostructures with potential for novel molecular functionalities.

From the above, we see that unlike graphene, the structures of MoS<sub>2</sub> monolayer are complicated and confusing. Currently, there is no theoretical study available to clarify the relationships among different structures reported in experiments. This study is aimed at bridging this gap. Our main objective is to understand the specific condition that stabilizes a particular phase and how phase transitions between different phases can be induced. We also study the geometric, electronic, and optical

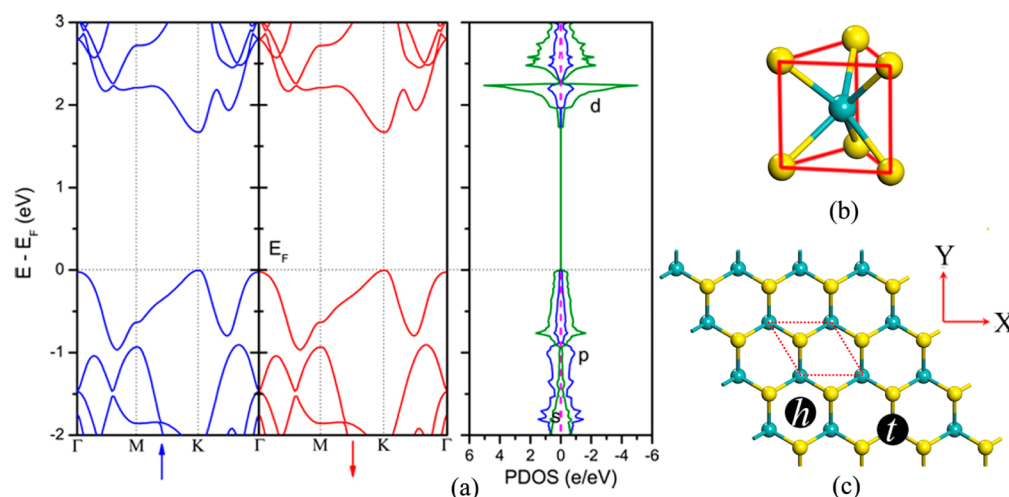
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Table 1. Optimized Geometrical Parameters and Energy of H-MoS<sub>2</sub>, T-MoS<sub>2</sub>, and ZT-MoS<sub>2</sub><sup>a</sup>

	<i>a</i> /Å	<i>b</i> /Å	$\alpha$ /deg	Mo–S/Å	Mo–Mo/Å	<i>E</i> /eV
H-MoS <sub>2</sub>	3.19	3.19	120.0	2.41	3.18	0
T-MoS <sub>2</sub>	3.19	3.19	120.0	2.43	3.18	0.85
ZT-MoS <sub>2</sub>	6.35	6.55	119.0	2.45 (2.39, 2.51)	3.29 (2.77, 3.81)	0.51

<sup>a</sup>For ZT-MoS<sub>2</sub>, the Mo–S bond length is in the range of 2.39–2.51 Å with an average length of 2.45 Å. The Mo–Mo bond length is in the range of 2.77–3.81 Å with an average length of 3.29 Å. The relative energy *E* is given using H-MoS<sub>2</sub> as the reference.



**Figure 1.** (a) Band structure, PDOS, (b) structural unit, and (c) geometrical structure of trigonal prismatic coordinated (H-MoS<sub>2</sub>) 2D MoS<sub>2</sub>. (The green and yellow spheres represent the Mo and S atoms, respectively. The two possible Li adsorption sites *t* and *h* are denoted in (c).)

properties of different phases. A fundamental understanding of these topics is important to fully harness the technological potential of MoS<sub>2</sub>.

Our results based on density functional theory (DFT) calculations show that while a trigonal prismatic H-MoS<sub>2</sub> is the most stable phase, the octahedral coordinated phases can also exist under specific conditions. According to our DFT study and analysis, ZT-MoS<sub>2</sub>, which is a charge density wave (CDW) state, can be stable at low temperature. When ZT-MoS<sub>2</sub> gains some energy from the outside, the CDW state becomes unstable turning to an undistorted octahedral coordinated phase (T-MoS<sub>2</sub>) without Mo–Mo clustering. Moreover, lithium adsorption and electron charging can stabilize another octahedral coordinated structure (DT-MoS<sub>2</sub>). We find that the trigonal prismatic H-MoS<sub>2</sub> is a direct semiconductor with a band gap of 1.67 eV, and the ZT-MoS<sub>2</sub> has a much smaller band gap of 0.022 eV. T-MoS<sub>2</sub>, on the other hand, is metallic. Our results suggest that due to much higher carrier mobility, ZT-MoS<sub>2</sub> may have a greater potential over H-MoS<sub>2</sub> as a promising material for microelectronics. The calculated optical properties of H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> show that they have different optical features. Furthermore, Li adsorption on the surface can induce a phase transition from H-MoS<sub>2</sub> to an octahedral coordinated MoS<sub>2</sub>. We find that charging the 2D MoS<sub>2</sub> with electrons can reverse the phase stabilities, which is another strategy to induce a phase transition. We also discuss the entire reversible recycling process of the phase transition induced by Li adsorption with detailed evolution of the structures. This will be helpful to better understand the basic processes involved in MoS<sub>2</sub>-based LIB.

## II. COMPUTATIONAL METHODS

Our calculations are based on spin-polarized density functional theory (DFT) with the Perdew–Burke–Ernzerhof (PBE) form

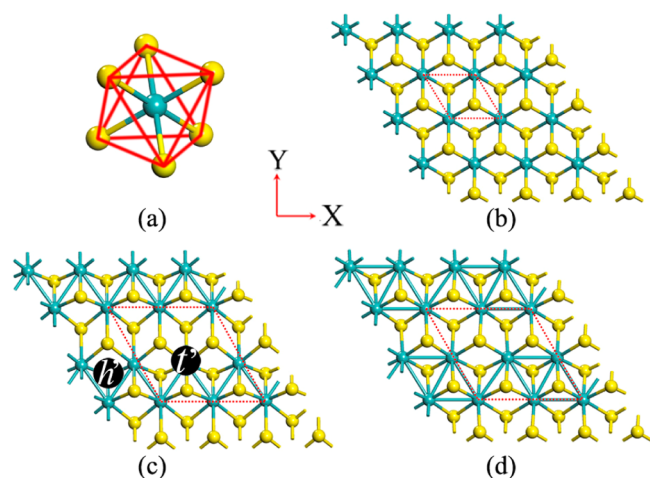
for the generalized gradient approximation (GGA)<sup>23</sup> to the exchange–correlation potential. All calculations are performed using Vienna ab initio simulation package (VASP) code,<sup>24</sup> ultrasoft pseudopotentials, and a plane-wave basis set with the projector augmented plane-wave method (PAW).<sup>25</sup> The periodic boundary condition is used to simulate 2D monolayer MoS<sub>2</sub>, and all of the structures are relaxed without any symmetry constraint. We use a vacuum space of 25 Å in the periodic directions to avoid interactions between two neighboring images. The reciprocal space is represented by Monkhorst–Pack special *k*-point scheme<sup>26</sup> with 19 × 19 × 1, 11 × 11 × 1, and 5 × 5 × 1 grid meshes for the (1 × 1) unit cell, the (2 × 2), and (4 × 4) supercell, respectively. The criteria of convergence for energy and force, as well as energy cutoff, are set to be 1 × 10<sup>−4</sup> eV, 0.01 eV/Å, and **360 eV**, respectively. In addition, for comparison, the state-of-the-art hybrid functional (HSE06)<sup>27,28</sup> is carried out to study the electronic properties. For the optical spectra, the imaginary part of dielectric function is determined by a summation over empty states in the whole Brillouin zone.<sup>29</sup>

## III. RESULTS AND DISCUSSION

**III.1. Phase Stability of 2D Monolayer MoS<sub>2</sub>.** To test the accuracy of our method, we first calculate the trigonal prismatic phase (H-MoS<sub>2</sub>) with GGA-PBE by using a 1 × 1 unit cell. The optimized geometrical parameters are given in Table 1. Our calculated results show that the optimized bond distance between Mo and S atoms  $d_{\text{Mo–S}} = 2.41$  Å, the distance between two S atoms at each corner  $d_{\text{S–S}} = 3.13$  Å, and the angle between Mo–S bonds  $\theta_{\text{S–Mo–S}} = 80.73^\circ$ . These agree well with the results of Ciraci et al.,<sup>30</sup> 2.42 Å, 3.13 Å, and 80.69°, respectively. A monolayer H-MoS<sub>2</sub> is a nonmagnetic semiconductor possessing a direct band gap with the valence band maximum (VBM) and conduction band minimum (CBM)

situated at the K point of the Brillouin zone. The calculated energy gap of H-MoS<sub>2</sub>, 1.67 eV, agrees well with previous theoretical result with GGA-PBE.<sup>31,32</sup> We also calculated the energy band structure using the HSE06 functional, and the energy gap is calculated to be 2.13 eV in agreement with the previous study.<sup>30</sup> To get a precise description of the optical band gap of monolayer MoS<sub>2</sub>, one may need to consider GW and Bethe–Salpeter calculation methods.<sup>33–36</sup> However, due to the limited computational resources, we use the PBE method for the qualitative understanding of the optical properties.

Figure 2 presents the other three possible metastable configurations of MoS<sub>2</sub> single layer synthesized using the

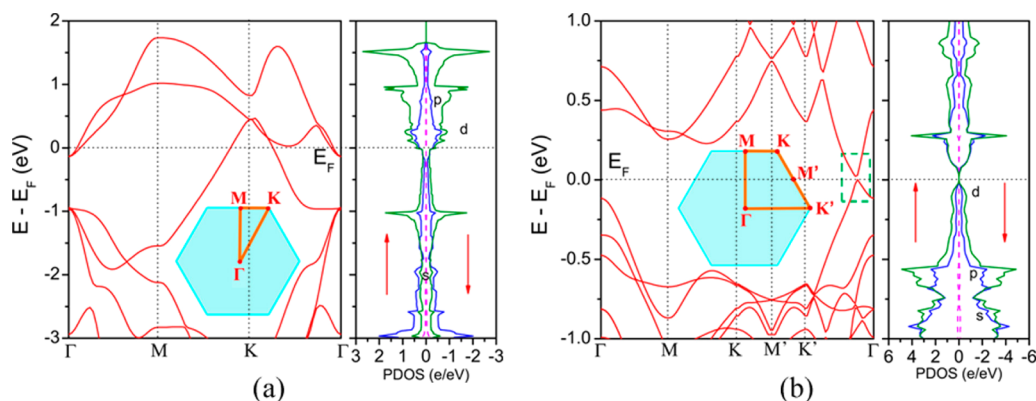


**Figure 2.** (a) Structural unit of octahedral coordinated 2D MoS<sub>2</sub>. Geometric structures of (b) T-MoS<sub>2</sub>, (c) ZT-MoS<sub>2</sub>, and (d) DT-MoS<sub>2</sub>. (The two possible Li adsorption sites  $t'$  and  $h'$  are denoted in (c).)

chemical solvent-based exfoliation methods.<sup>12,13,20</sup> These can be classified into three groups: octahedral coordinated MoS<sub>2</sub>, referred to as T-MoS<sub>2</sub> (Figure 2b); distorted octahedral coordinated MoS<sub>2</sub> with zigzag Mo–Mo chains, referred to as ZT-MoS<sub>2</sub> (Figure 2c); and distorted octahedral coordinated MoS<sub>2</sub> in rhombus-shape with Mo–Mo chains, referred to as DT-MoS<sub>2</sub> (Figure 2d). For convenience, we use O-MoS<sub>2</sub> to describe all three octahedral coordinated MoS<sub>2</sub> regardless of the detail of the molybdenum clusterization.

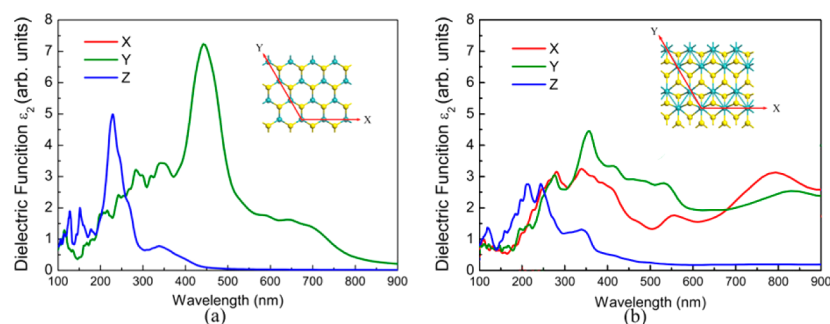
For the calculations of geometric and electronic properties as well as phase stability, we use  $(1 \times 1)$ ,  $(2 \times 2)$ , and  $(2 \times 2)$  super cells for T-MoS<sub>2</sub>, ZT-MoS<sub>2</sub>, and DT-MoS<sub>2</sub>, respectively. It should be noted here that the ZT-MoS<sub>2</sub> phase is the same phase named T-phase in Eda et al.'s work.<sup>22</sup> We first discuss the results of T-MoS<sub>2</sub> and ZT-MoS<sub>2</sub>. The  $(1 \times 1)$  T-MoS<sub>2</sub> and the  $(2 \times 2)$  ZT-MoS<sub>2</sub> maintain their structures after relaxation. However, we observed a structural transition to ZT-MoS<sub>2</sub> after the  $(1 \times 1)$  cell of T-MoS<sub>2</sub> is increased to  $(2 \times 2)$  and  $(4 \times 4)$ . In other words, free-standing T-MoS<sub>2</sub> is unstable at 0 K. The structural transition from T-MoS<sub>2</sub> to ZT-MoS<sub>2</sub>, which is a charge density wave (CDW) state,<sup>37,38</sup> is due to the Peierls instability. Below the critical Peierls transition temperature ( $T_p$ ), the elastic energy cost to modulate the atomic positions in T-MoS<sub>2</sub> to ZT-MoS<sub>2</sub> is less than the gain in electronic energy. Thus, the lattice of atoms undergoes a periodic distortion, and the electrons condense into a collective state with a periodic modulation of the charge density leading to the CDW state. This is known as Peierls' transition.<sup>39</sup> Because the Mo atom in the octahedral coordinated position has a  $d^2$  configuration, each Mo uses only two of the three in-plane  $t_{2g}$  orbitals. This fits the two-center, two-electron bonding model, which requires each Mo atom to bind with two neighboring Mo atoms to form two bonds as shown in Figure 2c. This results in a relatively stable zigzag chain configuration. In addition, an earlier experimental study<sup>4</sup> showed that the octahedral-based phase (O-MoS<sub>2</sub>) will transform to H-MoS<sub>2</sub> if the annealing temperature reaches to a critical temperature  $T_t$  ( $\sim 300$  °C). As for DT-MoS<sub>2</sub>, our results show that the  $(2 \times 2)$  structure is also unstable and transforms to the ZT-MoS<sub>2</sub> spontaneously. Although the pure free-standing DT-MoS<sub>2</sub> is not stable, it can exist in some impure state through the lithium adsorption or charging as shown in section III.3.

Numerically, the optimized ZT-MoS<sub>2</sub> is more stable than the undistorted T-MoS<sub>2</sub> by 0.34 eV in total energy. It is higher than that of H-MoS<sub>2</sub> by 0.51 eV for a unit cell as listed in Table 1. The fully relaxed lattice parameters and interatomic distances are also given in Table 1. The cell parameter " $a$ " for ZT-MoS<sub>2</sub> undergoes about 0.3% contraction, while " $b$ " undergoes about 2.8% expansion as compared to that of H-MoS<sub>2</sub>. No significant deviation from  $120^\circ$  is found for the " $\alpha$ " ( $=119.0^\circ$ ) angle. The Mo–S and Mo–Mo bond lengths (2.45 and 3.29 Å on average) are elongated for the ZT-MoS<sub>2</sub> as compared to H-MoS<sub>2</sub>. We obtain a shorter Mo–Mo distance of 2.77 Å inside

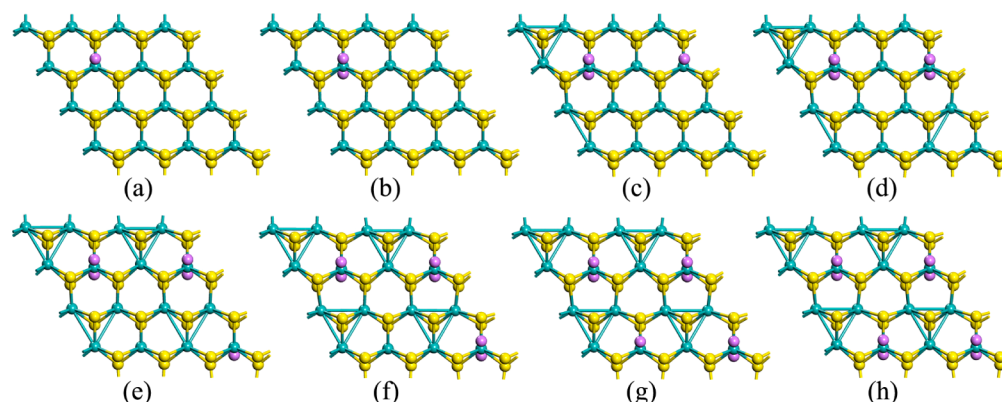


**Figure 3.** Band structures and PDOS of the optimized (a)  $(1 \times 1)$  T-MoS<sub>2</sub> and (b)  $(2 \times 2)$  ZT-MoS<sub>2</sub> along the lines connecting high-symmetry points of the Brillouin zone.





**Figure 4.** Calculated imaginary part of the dielectric function for parallel (X, Y) and perpendicular (Z) polarization of (a) monolayer H-MoS<sub>2</sub> and (b) ZT-MoS<sub>2</sub>.



**Figure 5.** The optimized structures of the most stable Li@H-MoS<sub>2</sub> with 1–8 Li atoms.

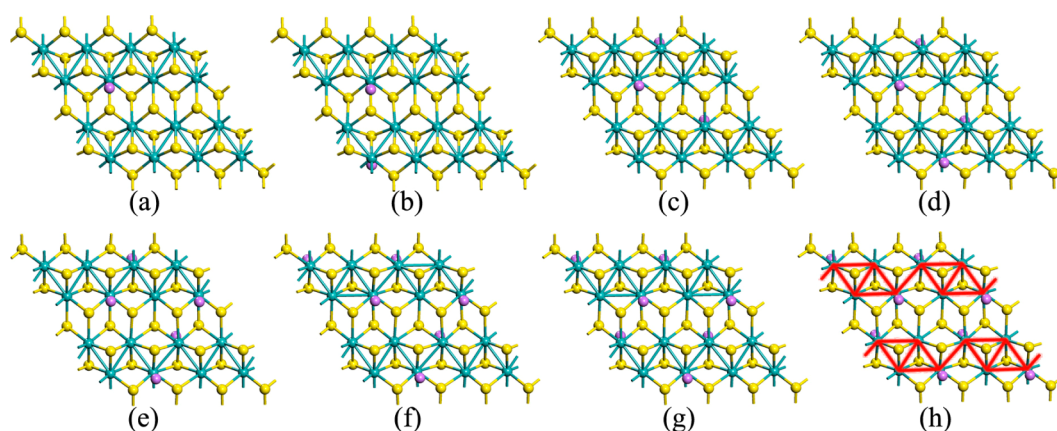
the cluster and a longer distance of 3.81 Å between the clusters, which results from the CDW.

**III.2. Electronic and Optical Properties of MoS<sub>2</sub> Monolayer.** The electronic properties of pure 2D MoS<sub>2</sub> are studied in detail below. The band structures calculated by GGA-PBE for a monolayer of T-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> along the lines connecting the high-symmetry points of the Brillouin zone are shown in Figure 3. We have carried out spin-polarized calculations to see if the ground state could be magnetic, but two-dimensional T-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> remain nonmagnetic. The structural distortions of monolayer dichalcogenides ZT-MoS<sub>2</sub> lead to the opening of a direct gap of 0.022 eV in the electronic structure as compared to the undistorted metallic T-MoS<sub>2</sub> as shown in Figure 3b. Additionally, the band gap of ZT-MoS<sub>2</sub> is calculated to be 0.23 eV, and T-MoS<sub>2</sub> is still metallic with HSE06. In the following, we calculate the carrier mobility and optical properties of 2D H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub>. T-MoS<sub>2</sub> is not considered because it is metallic as shown in Figure 3a.

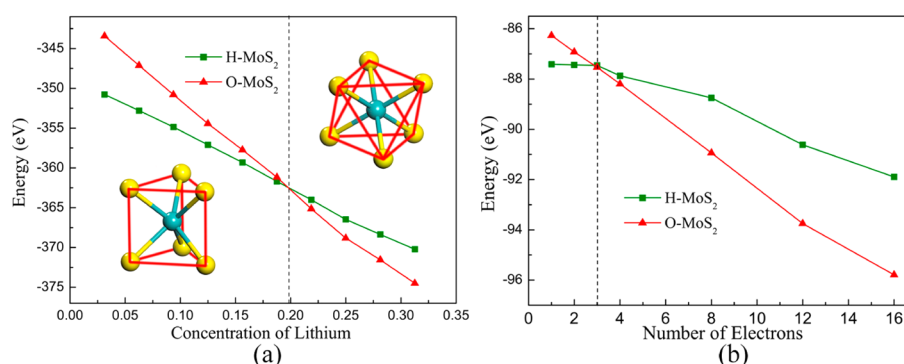
To further explore the potential applications of the less studied 2D ZT-MoS<sub>2</sub>, we use density functional theory coupled with Boltzmann transport equation<sup>40</sup> to investigate the acoustic phonon-dominated mobility<sup>41</sup> of ZT-MoS<sub>2</sub> and H-MoS<sub>2</sub> at temperature  $T = 100$  K. Two transporting directions labeled as X and Y (Figures 1 and 2) were considered. The intrinsic electron density is estimated to be  $1 \times 10^{10} \text{ cm}^{-2}$ , which is much lower than that of n-doped H-MoS<sub>2</sub> used in the experiment.<sup>7</sup> The calculated electron (hole) mobility of H-MoS<sub>2</sub> is  $1.2$  ( $3.8$ )  $\times 10^2 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  along both X and Y directions. These results fit well with the theoretical predictions when the dependence of mobility on carrier density and temperature is considered.<sup>42,43</sup> Interestingly, ZT-MoS<sub>2</sub> has electron and hole mobility 1 (2) order(s) of magnitude higher

than that of H-MoS<sub>2</sub> along the X (Y) direction. More specifically, the electron (hole) mobility of ZT-MoS<sub>2</sub> is  $4.1$  ( $2.1$ )  $\times 10^3$  and  $6.4$  ( $5.7$ )  $\times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  along the X and Y directions, respectively. The great improvement in the mobility can be attributed to the reduction of electron (hole) effective mass<sup>44</sup> from 0.49 (0.60)  $m_e$  to 0.12 (0.05)  $m_e$  when H-MoS<sub>2</sub> is transformed to ZT-MoS<sub>2</sub>. In particular, the mobility of ZT-MoS<sub>2</sub> is higher than that of silicon and comparable to that of graphene nanoribbons and graphene transistors.<sup>45–47</sup> Up to now, only 2D monolayer H-MoS<sub>2</sub> has been studied experimentally for application in electronic devices. According to the high carrier mobility of ZT-MoS<sub>2</sub>, it is reasonable to believe that the ZT-MoS<sub>2</sub> would have extensive potential applications in electronic devices.

Because of the strong photoluminescence of monolayer H-MoS<sub>2</sub>,<sup>48</sup> we have studied the optical properties of both phases. The PBE-calculated imaginary parts of the dielectric functions for monolayer H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> are shown in Figure 4. The calculation details can be found in a previous study.<sup>49</sup> We see that our results for monolayer H-MoS<sub>2</sub> can accurately reproduce the experimentally observed optical absorption spectrum.<sup>4</sup> Our calculations show a sharp absorption peak around 450 nm and another lower peak at 230 nm, which fits the experimental results of Eda et al.<sup>4</sup> very well. The absorption of ZT-MoS<sub>2</sub> covers a wider range than that of H-MoS<sub>2</sub>, although there are no sharp absorption peaks. For in-plane polarization, ZT-MoS<sub>2</sub> monolayer is optically anisotropic, which is different from the H-MoS<sub>2</sub> monolayer because of their different lattice structure. Thus, our calculated results indicate that the two different MoS<sub>2</sub> monolayer phases may have different optical applications. Additionally, the absorption



**Figure 6.** The optimized structures of the most stable Li@ZT-MoS<sub>2</sub> with 1–8 Li atoms. Mo atoms form a diamond-like chain in (h) as highlighted in red.



**Figure 7.** (a) Variation of the energy for H-MoS<sub>2</sub> and O-MoS<sub>2</sub> as the concentration of Li changes. (b) The variation of the energy for H-MoS<sub>2</sub> and O-MoS<sub>2</sub> with respect to the number of electrons in the systems.

spectra of different phases provide an efficient method to identify them experimentally.

**III.3. Phase Transition of 2D MoS<sub>2</sub> Monolayer Induced by Lithium Insertion.** In recent years, 2D MoS<sub>2</sub> has attracted much attention as electrode material for LIB due to its high surface area and short diffusion length.<sup>2,50</sup> In the following, we introduce lithium atoms on the surface of 2D MoS<sub>2</sub> to induce phase transition, which is a typical procedure for both the discharge/charge processes in LIB and the solvent-based exfoliation of MoS<sub>2</sub> monolayer. As far as we know, no experimental or theoretical studies have been reported in detail on the phase transition process.

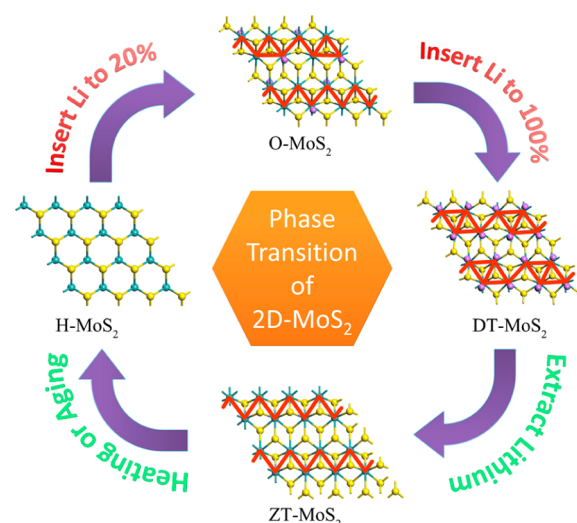
First, we check the stable lithium adsorption sites on 2D H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> as illustrated in Figures 5a and 6a. For H-MoS<sub>2</sub>, two possible sites are examined as shown in Figure 1: (1) top of Mo atom (*t*) sites; and (2) hollow (*h*) sites above the center of hexagon. For ZT-MoS<sub>2</sub>, two other possible sites are also considered as shown in Figure 2: (1) top of Mo atom (*t'*) sites; and (2) hollow (*h'*) sites above the center of S–S triangle but not on top of a Mo atom. It should be pointed out that the Li atoms move from the *t'* sites slightly after relaxation in ZT-MoS<sub>2</sub>, while they stay above the *t* sites in H-MoS<sub>2</sub>. To represent the stability of the Li adsorbed system, we calculate the binding energy ( $E_b$ ), which is defined as  $E_b = E_{\text{Li@MoS}_2} - nE_{\text{Li}} - E_{\text{MoS}_2}$ .  $n$  indicates the number of Li atoms, while  $E_{\text{Li@MoS}_2}$ ,  $E_{\text{Li}}$ , and  $E_{\text{MoS}_2}$  indicate the energies of Li adsorbed MoS<sub>2</sub>, Li atom, and MoS<sub>2</sub> monolayer, respectively. The calculated binding energy shows that a Li atom on *t* site is about 0.15 eV lower than that on *h* site for H-MoS<sub>2</sub>, while it is

energetically degenerate for a Li atom to occupy *t'* and *h'* sites in ZT-MoS<sub>2</sub>. Nevertheless, we still consider *h* and *h'* sites for inserting additional Li atoms in the following. All possible Li distributions are considered in our calculations keeping symmetry in mind. Once the Li site distribution with the lowest energy has been found, we choose this as well as the second lowest energy configuration as two initial structures for introducing another Li atom. This process is repeated until the number of Li atoms increases to 10 in a (4 × 4) supercell.

We extensively examined the most stable configurations of Li@MoS<sub>2</sub>. These are shown in Figures 5 and 6 for 1–8 Li atoms. As more Li atoms are added to the surface, clustering of Mo increases in both phases. Comparing the possible sites of *t*, *t'*, *h*, and *h'*, we found that Li atoms prefer to reside on *t* and *t'* sites for all concentrations. Figure 7a gives the variation of the energies for both Li@H-MoS<sub>2</sub> and Li@ZT-MoS<sub>2</sub> as the concentration of Li increases. Because there are 32 most stable sites for Li atoms on (4 × 4) supercell of 2D MoS<sub>2</sub>, the concentration of Li is defined as the number of Li atoms  $n$  divided by 32 ( $n/32 \times 100\%$ ). As shown in Figure 5a, the H-MoS<sub>2</sub> is still the most stable phase when 1–6 Li atoms are added to the system. When the concentration of Li atoms exceeds 20%, O-MoS<sub>2</sub> becomes more stable, which means that the phase transition in 1 kg of 2D H-MoS<sub>2</sub> can be induced with only 17.5 g of Li. Before the transition point, some triangular Mo–Mo clustering appears in Li@H-MoS<sub>2</sub>, while after the transition point the state of the Mo–Mo clustering in 7Li@O-MoS<sub>2</sub> is between ZT-MoS<sub>2</sub> and DT-MoS<sub>2</sub>. When 8 Li atoms are introduced, Mo atoms form a diamond-like chain as shown

in Figure 6h. As we continue introducing up to 10 Li atoms, the system can maintain the “diamond chain” structure. We subsequently checked the structure of O-MoS<sub>2</sub> with 100% Li concentration, which shows that the DT-MoS<sub>2</sub> configuration is still stable. The transformation of the Mo–Mo clustering from zigzag chain to diamond chain can also be understood by analyzing the valence electronic configuration. As Li atoms are added on the surface of MoS<sub>2</sub>, electrons transfer from Li atoms to the host. In other words, the valence electron configuration of Mo atoms in the octahedral coordination will undergo a transformation from  $d^2$  to  $d^3$ . Thus, the  $t_{2g}$  levels of each Mo atom can accommodate one electron per level, and each Mo atom will need to form two-center two-electron  $\sigma$ -bonds with the three neighboring Mo atoms,<sup>38</sup> resulting in the diamond-chain configuration. We believe that the transition from trigonal prismatic coordination to octahedral coordination is also caused by the transfer of electrons from Li atoms to the MoS<sub>2</sub> sheet. From the band structure of H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub>, it can be seen that the conduction band of H-MoS<sub>2</sub> is much higher above the Fermi level as compared to that of ZT-MoS<sub>2</sub>. Thus, the introduced electrons in H-MoS<sub>2</sub> will increase the energy of H-MoS<sub>2</sub> by a higher level than that of ZT-MoS<sub>2</sub>. To verify this conjecture, we charged the  $(2 \times 2)$  supercell of H-MoS<sub>2</sub> and O-MoS<sub>2</sub> with electrons, and the results are shown in Figure 7b. Note that O-MoS<sub>2</sub> becomes more stable than the H-MoS<sub>2</sub> as the number of electrons increases. The DT-MoS<sub>2</sub> configuration is formed after charging. This is similar to what we observed with Li doping. Only 3 electrons can induce a  $(2 \times 2)$  supercell to undergo phase transition, corresponding to  $-8.33 \times 10^{14} \text{ cm}^{-2}$ . We further check the dependence of the results on the supercell size in the transverse direction. Our result shows that the phase transition occurs when 14 electrons are injected in a  $4 \times 4 \times 1$  supercell with the charge density of  $-9.71 \times 10^{14} \text{ cm}^{-2}$ . The required concentrations for inducing the phase transition are quite similar for the two supercells. We also confirmed Kertesz–Hoffmann’s theory that a  $d^2$  to  $d^3$  transformation can sometimes induce a transfer from trigonal prismatic coordination to octahedral coordination.

It is important to note that in an earlier experimental study,<sup>12</sup> S atoms in 2D MoS<sub>2</sub> were found to keep the octahedral coordination after all of the Li atoms were removed, but the detailed structural information was lacking. On the basis of our study, we conclude that this kind of octahedral coordinated configuration without Li atoms is possible for the ZT-MoS<sub>2</sub> phase, which is metastable and can transform to H-MoS<sub>2</sub> after heating or aging.<sup>4</sup> Combining these experimental works with our theoretical calculation, we summarize the possible pathways for structural phase transition among different structures in Figure 8: H-MoS<sub>2</sub>  $\rightarrow$  O-MoS<sub>2</sub>  $\rightarrow$  DT-MoS<sub>2</sub>  $\rightarrow$  ZT-MoS<sub>2</sub>  $\rightarrow$  H-MoS<sub>2</sub>. The detailed process is the following: (1) When Li atoms are introduced to H-MoS<sub>2</sub>, the trigonal prismatic H-MoS<sub>2</sub> remains stable until the Li concentration reaches 20%. (2) When more Li atoms are inserted, the octahedral coordinated O-MoS<sub>2</sub> becomes more stable. The structure transforms from zigzag chains to “diamond chains” and finally forms the stable DT-MoS<sub>2</sub> phase. (3) When all of the Li atoms are extracted from the system, the structure becomes ZT-MoS<sub>2</sub>. (4) Through heating or aging, the ZT-MoS<sub>2</sub> will transform back to the most stable phase H-MoS<sub>2</sub>. We hope that the pathways discussed above will help experimentalists to better understand the detailed process involved in MoS<sub>2</sub>-based LIB and in the liquid phase exfoliation of monolayer MoS<sub>2</sub> through Li intercalation.



**Figure 8.** Possible pathways of structural phase transition in MoS<sub>2</sub> monolayer.

#### IV. SUMMARY

A comprehensive study of the relative phase stability of MoS<sub>2</sub> monolayer led us to the following conclusions: (1) Two phases were identified that can be stable under normal conditions, the traditional trigonal prismatic H-MoS<sub>2</sub> phase and the distorted octahedral ZT-MoS<sub>2</sub> phase with zigzag Mo–Mo chains. (2) Li insertion with concentration of 20% or electron charging with concentration of  $8.33 \times 10^{14} \text{ cm}^{-2}$  can induce structural transitions. (3) MoS<sub>2</sub> monolayer not only displays complicated geometries but also exhibits rich physical properties: H-MoS<sub>2</sub> is a semiconductor with a direct band gap of 1.67 eV. ZT-MoS<sub>2</sub> is also a direct band gap semiconductor, but with a much smaller band gap of 0.022 eV. T-MoS<sub>2</sub>, on the other hand, is metallic. Furthermore, the electron (hole) mobility of ZT-MoS<sub>2</sub> is found to be  $4.1 (2.1) \times 10^3$  and  $6.4 (5.7) \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  along the X and Y directions, respectively, which are much higher than the corresponding values of  $1.2 (3.8) \times 10^2 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  in H-MoS<sub>2</sub>. (4) H-MoS<sub>2</sub> and ZT-MoS<sub>2</sub> show very different optical properties, which can be used to identify their structures. (5) DT-MoS<sub>2</sub> can be formed with lithium adsorptions or electron injections; when the lithium atoms on the surface are removed, the ZT-MoS<sub>2</sub> phase then forms. It is hoped that the information provided in this study will help experimentalists to better understand the geometries and properties of MoS<sub>2</sub> monolayers.

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##### Notes

The authors declare no competing financial interest.

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