Scaling of the Molecular Weight-Dependent Thermal Volume Transition of Poly(N-isopropylacrylamide)

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ABSTRACT: A series of narrowly distributed poly(N-isopropylacrylamide) (PNIPAM) with molecular weight ranging from $8 \times 10^4$ to $2.3 \times 10^7$ g/mol were prepared by a combination of free radical polymerization and fractional precipitation. An ultrasensitive differential scanning calorimetry was used to study the effect of molecular weight on the thermal volume transition of these PNIPAM samples. The specific heat peak of the transition temperature ($T_{c,p,0}$) was obtained by extrapolation to zero heating rate (HR) because of the linear dependence of the transition temperature ($T_c$) on the HR. The relation between $T_{c,p,0}$ and the degree of polymerization ($N$) investigated. © 2010 Wiley Periodicals, Inc.

KEYWORDS: degree of polymerization (DP); differential scanning calorimetry (DSC); dynamic light scattering; poly(N-isopropylacrylamide); stimuli-sensitive polymers

INTRODUCTION It is well known that poly(N-isopropylacrylamide) (PNIPAM) is soluble in water at low temperature and becomes insoluble at higher temperature above its lower critical solution temperature (LCST $\sim 32 \, ^\circ C$). PNIPAM has received much more attention because of its potential biomedical or pharmaceutical applications as well as its application for the separation sciences based on its thermo-sensitivity. The phase separation behavior for the aqueous solution of PNIPAM has been investigated by a variety of techniques including laser light scattering (LLS), fluorescence,11–13 differential scanning calorimetry (DSC),14–21 turbidimetry,18,19,21–23 and infrared spectroscopy.24–26 Moreover, the phase transition of thermally sensitive homopolymers has been investigated theoretically.27–34 In spite of extensive experimental studies on the phase transition of PNIPAM, the issue about the molecular weight ($M_w$) dependence of phase transition is still controversial. Some studies show that the cloud point in turbidimetry studies or transition temperature in calorimetric measurements are dependent on $M_w$,15,19,21,23 whereas others show that they are independent on $M_w$.14,17,22 Recently, Xia et al. synthesized several series of narrowly distributed PNIPAM with end groups of varying polarity by atom transfer radical polymerization (ATRP). Their results from turbidimetry and DSC clearly show that the $M_w$ dependence could be seen as a combination of $M_w$ and end group effects, that is, the aqueous solutions of narrow-disperse PNIPAMs with the same end group showed a dramatic decrease in cloud point with increasing $M_w$ and the aqueous solutions of narrow-disperse PNIPAMs with more hydrophobic group but with the same $M_w$ had lower cloud points.19,21 The results from theoretical studies are also controversial. On the basis of sequential hydrogen bond formation between polymer chains and water molecules, Tanaka and co-workers27 reported phase diagrams with very flat LCST phase separation line, that is, cooperative hydration leads to flat LCST with almost no molecular weight dependence. On the other hand, it has been described by the mean field theory of Flory that there is a simple power law for the degree of polymerization ($N$) dependence of the critical temperature ($T_c$):

$$T_c \propto N^{-1/2}$$

Wilding et al.33 concluded that the scaling of the critical temperature with chain length is well described by the same power law as the Flory theory (eq 1) by using configurational bias Monte Carlo methods. Yan et al.34 also proved the validity of the Flory theory. More recently, Paul et al. studied the $N$ dependence of maximum transition temperature using the Wang–Landau sampling idea.29–31,35,36 They observed the predicted scaling behavior $T \sim N^{-1/2}$, where they used the peaks in the specific heat to determine the transition temperatures for different chain lengths.
Until now, to our best knowledge, quantitative study on the \( M_w \) dependence of transition temperature by DSC experiments, especially in a broad range, has received less attention. In this article, a series of narrow-disperse PNIPAM was obtained by fractional precipitation following the conventional free radical polymerization using azobisisbutyronitrile (AIBN) as initiator. Our DSC results show that the transition temperature \( T_p \) had linear dependence on the heating rate \( (HR) \), so the \( T_{p,0} \) was obtained by extrapolation to zero HR. The results show that \( T_{p,0} \) have a scaling relation with the degree of polymerization \( (N) \) where the power is \(-1/2\), which is consistent with the results described by Paul and coworkers.\(^{29}\) Besides, from the data reported by Lessard et al.,\(^{37}\) we found the same scaling law for poly\((N,N\text{-diethylacrylamide})\) homopolymers.

**EXPERIMENTAL**

**Materials**

Details for synthesis of the PNIPAM homopolymer can be found elsewhere.\(^{7-9,38,39}\) Briefly, monomer \( N\)-isopropylacrylamide was recrystallized three times in a benzene/n-hexane mixture. The purified monomer and recrystallized AIBN as initiator were dissolved in purified solvent benzene. The solution was degassed through three cycles of freezing and thawing and the reaction was carried out at 56 °C for 30 h. The resultant PNIPAM homopolymer was carefully fractionated by a dissolution/precipitation process in a mixture of dry acetone and dry hexane at room temperature. The weight-average molar mass \( (\langle M_w \rangle) \) of PNIPAM fractions used were characterized by static light scattering. The distribution of four PNIPAM fractions with lower \( M_w \) was characterized by gel permeation chromatography (GPC) using a series of three linear Styragel columns HT3, HT4, and HT5. A Waters 1515 pump and a Waters 2414 differential refractometer detector were used. The eluent was \( N,N\text{-dimethylformamide} \) with 1 g/L BrLi at a flow rate of 1.0 mL/min and narrowly distributed poly(ethylene oxide) (PEO) were used as standards. The polydispersity index (PDI, \( M_{w} / M_{n} \)) with higher \( M_w \) was estimated from the relative weight \( \mu_w / (\Gamma)^2 \).\(^{40}\)

**Laser Light Scattering**

A spectrometer (ALV/DLS/LS-S-5022F) equipped with a multi-\( \tau \) digital time correlator (ALV5000) and a cylindrical 22 mW UNIPHASE He–Ne laser \((\lambda_0 = 632.8 \text{ nm})\) as the light source was used. In static LLS,\(^{40,42}\) we were able to obtain the weight-average molar mass \( (\langle M_w \rangle) \) and the z-average root-mean-square radius of gyration \( (\langle R_g^2 \rangle^{1/2}) \) or written as \( (R_g) \) in a very dilute solution from the angular dependence of the excess absolute scattering intensity.

\[
\frac{KC}{\overline{R_{c}}(q)} \approx \frac{1}{M_w} \left( 1 + \frac{1}{3} \frac{R_g^2}{q^2} \right) + 2A_2C
\]

where \( K = 4\pi^2 n^2 (dn/dC)^2 / (N_A \lambda_0)^4 \) and \( q = (4\pi n / \lambda_0) \sin(\theta/2) \) with \( C, dn/dC, N_A, \) and \( \lambda_0 \) being the concentration of the polymer, the specific refractive index increment, the Avogadro’s number, and the wavelength of light, respectively. The refractive index increment of PNIPAM was measured using a precise differential refractometer.\(^{42}\) In dynamic LLS,\(^{43}\) the Laplace inversion of a measured intensity–intensity time correlation function \( G^{(2)}(t, q) \) in the self-beating mode can result in a line-width distribution \( G(T) \). For a pure diffusive relaxation, \( T \) is related to the translational diffusion coefficient \( D \) by \( T/\Gamma^2 = D \) at \( q \rightarrow 0 \) and \( C \rightarrow 0 \), or a hydrodynamic radius \( R_0 = k_BT/(6\pi\eta D) \) with \( k_B, T, \) and \( \eta \) being the Boltzmann constant, absolute temperature, and solvent viscosity, respectively.

**RESULTS AND DISCUSSION**

A series of narrow-distribute PNIPAM with a broad range of molecular weight was prepared by a combination of conventional free radical polymerization and fractional precipitation. These PNIPAM samples were characterized by GPC or LLS. Figure 1 shows typical Zimm plots of PNIPAM sample (PN6). The extrapolation of \( [KC/R_{c}(q)] \) to \( C \rightarrow 0 \) and \( q \rightarrow 0 \) leads to \( M_w \). Figure 2 shows typical normalized intensity–intensity correlation function and the corresponding distribution of hydrodynamic radius, which reveals that the PNIPAM fractions are narrowly distributed. Four PNIPAM samples with lower \( M_w \) were characterized by GPC and the other five PNIPAM samples were measured by LLS and the PDI was estimated from \( M_w / M_n \sim 1 + 4\mu_w / (\Gamma)^2 \). The corresponding data are summarized in Table 1. From Table 1, we know that the distributions of all fractions are narrow. Note that for
PNIPAM fractions with lower molar mass, the $M_w$ measured by LLS was smaller than that characterized by GPC. This phenomenon has also been observed by Schilli et al.\textsuperscript{44} and Xia et al.\textsuperscript{21} where they found that the $M_w$ obtained by GPC were higher than those obtained from Matrix-assisted laser desorption/ionization-time of flight (MALDI-TOF) analysis and NMR method, respectively. In our experiments, narrowly distributed PEOs were used as standards, due to the possibly different chain conformations between the standards and PNIPAMs and/or the different interactions between column material/PEO and column materials/PNIPAM, the values measured by GPC can only be used to reveal the trend of the molecular weight and the distributions of the PNIPAMs. The molecular weight values determined by LLS from Zimm plots were used for further analyses in our work. Note that $^1$H NMR and MALDI-TOF have also been used to characterize the molecular weights of PNIPAMs.\textsuperscript{19,21,45–48} $^1$H NMR spectroscopy has been used to obtain molecular weight by comparing the peak areas of the main chain with that arising from the end group. Xia et al.\textsuperscript{11} has reported that the molecular weight values determined by $^1$H NMR were in good agreement with theoretical values. However, if the signals from the end group overlap with those of the main chain or the molecular weights of PNIPAMs are so high that it is difficult to precisely integrate the area of the signals arising from the end group, the molecular weights cannot be determined by $^1$H NMR under these circumstances. It has been reported that the values determined by MALDI-TOF are in good agreement with those from $^1$H NMR\textsuperscript{19} or theoretical calculation\textsuperscript{49} for molecular weights below $\sim 4 \times 10^4$ g/mol. Ganachaud et al.\textsuperscript{46} mentioned that it was difficult to analyze MALDI data at higher molecular weights because the PNIPAM tended to undergo fragmentation. Xia et al.\textsuperscript{19} also reported that the PNIPAMs with molecular weight higher than $1 \times 10^4$ g/mol gave weak or nonexistent signals. Here, due to the broad range of molecular weight of PNIPAM, both MALDI-TOF and $^1$H NMR are not good characterization methods.

Using these PNIPAM fractions with narrowly distributed $M_w$, we measured the phase transition by using US-DSC. In all measurements, the concentration of polymer was kept as 1 g/L. Our results showed that all data were reproducible.\textsuperscript{20} Figure 3 shows the temperature dependence of specific heat capacity ($C_p$) at four different HRs of the PN8 fraction. From Figure 3, we know that $T_p$ increased from 32.3 to 32.9 $^\circ$C with increasing the HR from 0.081 to 1.49 $^\circ$C/min, which may be due to the competition between intrachain contraction and interchain association in the HR\textsuperscript{20} and/or may be due to the fact that a finite HR experiment is prone to sample nonequilibrium effects. Figure 4 shows $T_p$ is in linear proportion to the HR, that is, $T_p = T_{p,0} + b \cdot HR$. The $T_{p,0}$ values and the coefficients ($b$) for all PNIPAM samples have been summarized in Table 1. The $b$ values did not change obviously with the molecular weight of PNIPAMs. Figure 5 shows that the temperature dependence of $C_p$ for several PNIPAM fractions with different $M_w$. From Figure 5 and the $T_{p,0}$ values in Table 1, we know $T_p$ has inverse $M_w$ dependence, that is, the transition temperature decreases with increasing the $M_w$. Xia et al.\textsuperscript{19,21} also found this same trend using five series of narrowly distributed PNIPAM prepared by ATRP. Similarly, Zhu and coworkers\textsuperscript{37} have reported the inverse $M_w$ dependence of LCST of poly(N,N-diethylacrylamide).

TABLE 1 Characterization of PNIPAM Samples by LLS, GPC, and US-DSC

<table>
<thead>
<tr>
<th>Polymer</th>
<th>$\langle M_w \rangle$ (10^4 g/mol)</th>
<th>$M_w/M_m$</th>
<th>$\langle M_w \rangle$ (10^4 g/mol)</th>
<th>$M_w/M_m$</th>
<th>$T_{p,0}/^\circ$C</th>
<th>$b$/min</th>
</tr>
</thead>
<tbody>
<tr>
<td>PN1</td>
<td>8</td>
<td>1.16</td>
<td>17</td>
<td>1.16</td>
<td>33.99</td>
<td>0.44</td>
</tr>
<tr>
<td>PN2</td>
<td>15</td>
<td>1.19</td>
<td>24</td>
<td>1.19</td>
<td>33.67</td>
<td>0.49</td>
</tr>
<tr>
<td>PN3</td>
<td>42</td>
<td>1.19</td>
<td>61</td>
<td>1.19</td>
<td>32.93</td>
<td>0.38</td>
</tr>
<tr>
<td>PN4</td>
<td>64</td>
<td>1.16</td>
<td>91</td>
<td>1.16</td>
<td>32.67</td>
<td>0.35</td>
</tr>
<tr>
<td>PN5</td>
<td>120</td>
<td>1.5</td>
<td></td>
<td></td>
<td>32.48</td>
<td>0.30</td>
</tr>
<tr>
<td>PN6</td>
<td>240</td>
<td>1.4</td>
<td></td>
<td></td>
<td>32.45</td>
<td>0.36</td>
</tr>
<tr>
<td>PN7</td>
<td>390</td>
<td>1.5</td>
<td></td>
<td></td>
<td>32.35</td>
<td>0.41</td>
</tr>
<tr>
<td>PN8</td>
<td>770</td>
<td>1.4</td>
<td></td>
<td></td>
<td>32.32</td>
<td>0.43</td>
</tr>
<tr>
<td>PN9</td>
<td>2300</td>
<td>1.2</td>
<td></td>
<td></td>
<td>32.26</td>
<td>0.40</td>
</tr>
</tbody>
</table>
Theoretically, by the mean field theory of Flory,32 we know the critical temperature ($T_c$) is scaled to the degree of polymerization ($N$), that is, $T_c \propto N^{-1/2}$. Wilding et al.33 and Yan et al.34 proved the validity of the Flory theory by using configurational bias Monte Carlo Methods and an expanded grand canonical ensemble simulation, respectively. It should be noted that critical temperature $T_c$ is different from the $T_p$ measured by DSC. At $T_c$, the solution separates into two phases with different compositions. $T_p$ is the temperature where the specific heat capacity reaches its maximum. Using the Wang–Landau sampling idea,35,36 Paul et al. have shown that the specific heat peak for the coil-to-globule transition, that is, $T_p$ here, is proportional to $N^{-1/2}$.29–31 Thus, the $T_{p,0}$ values in Table 1 have been plotted in Figure 6(a). For the first time, we experimentally found the $T_{p,0}$ measured by DSC experiments is proportional to $N^{-1/2}$. From Figure 6(a), the intercept $T_0$ and the slope were $32.08 \pm 0.05$ and $52 \pm 3 ^\circ\text{C}$, respectively. To confirm the scaling relation between $T_{p,0}$ and $N$, the data in Figure 6(a) have been replotted in Figure 6(b) in the form of $\ln(T_{p,0} - T_0)$ versus $\ln N$. From Figure 6(b), we know that the slope, that is, the power, was $-0.44 \pm 0.04$ that is close to $-1/2$. By turbidimetry and DSC, Xia et al.19,21 have measured the thermal response of

![Figure 3](image3.png)  
**FIGURE 3** Effect of heating rate on the thermal volume transition of PN8 in water where the heating rate was (1) 0.081, (2) 0.50, (3) 1.00, and (4) 1.49 °C/min.

![Figure 4](image4.png)  
**FIGURE 4** Heating rate dependence of transition temperature ($T_p$) of PNIPAM fraction PN8.

![Figure 5](image5.png)  
**FIGURE 5** Heating rate dependence of transition temperature ($T_p$) of PNIPAM fraction PN8.

![Figure 6](image6.png)  
**FIGURE 6** (a) A plot of $T_{p,0}$ versus $N^{-1/2}$, where $N$ is the degree of polymerization of PNIPAM and the concentration of all PNIPAM fractions in water was 1 g/L. (b) A plot of natural logarithm of the ($T_{p,0} - T_0$) as a function of the natural logarithm of $N$. 

![Figure 7](image7.png)  
**FIGURE 7** Effect of molecular weight on the thermal volume transition of PNIPAM chains in water where the heating rate was 1.00 °C/min. Curves 1–5: (1) PN7, (2) PN4, (3) PN3, (4) PN2, and (5) PN1.
several series of narrow-disperse PNIPAM synthesized by ATRP. Winnik and coworkers\textsuperscript{48} synthesized three linear PNIPAMs with an azido group on one end and propargyl group on the other end by reversible addition-fragmentation chain transfer and characterized the phase transition of these samples by DSC. We found the instruments used by us, Xia et al., and Winnik et al. are VP-DSC microcalorimeters from MicroCal, so we put their data in Figure 7 together with our data just to reveal the trend due to the fact that the molecular weights from different groups were determined by different characterization methods. The dashed lines are guides for the eyes. In the experiments reported by Xia et al.\textsuperscript{21} 2-chloropropionamide (CP), \(N\)-isopropyl-2-chloropropionamide (\(i\)-PrCP), ethyl 2-chloropropionate (ECP), and \(N\)-phenyl-2-chloropropionamide (PhCP) were used as initiators to give polymers with end groups of varying polarity, ranging from hydrophilic for CP to hydrophobic for PhCP. From Figure 7, we know that when \(N^{-1/2}\) is smaller than \(-0.11\), that is, \(M_w\) is larger than \(-9300\) g/mol and \(N\) is larger than \(-83\), all the data are closed to the dash line expect the PNIPAMs with more hydrophobic end groups ECP and PhCP. We also observed that although the \(T_p\) of PNIPAMs with end group PhCP is lower than those of PNIPAMs with other more hydrophilic end groups, \(T_p\) is also proportional to \(N^{-1/2}\). When the \(N\) is smaller than \(-83\), the data deviated from the dash line may be due to the higher order corrections \([\text{i.e., O}(N)]\).\textsuperscript{29} Similarly, using Wang–Landau sampling idea, Paul and coworkers\textsuperscript{29} also observed deviations of the positions of the specific heat peaks from the \(N^{-1/2}\) behavior in the finite \(N\).

Lessard et al.\textsuperscript{37} have studied the effect of molecular weight on the LCST of poly(\(N,N\)-diethylacrylamide). Their data have been replotted in Figure 8(a). From Figure 8(a), we know that for poly(\(N,N\)-diethylacrylamide), a same and simple scaling law exists between \(T_p\) and \(N\), that is, \(T_p \propto N^{-1/2}\). The intercept \(T_0\) and the slope were 27.6 °C and 102 °C, respectively. Note that the molecular weight and the distribution of the polymer samples were precisely determined by size exclusion chromatography on a Waters system equipped with an online differential refractometer by using polystyrene samples as the standards. Figure 8(b) shows that a plot of natural logarithm of the \((T_p - T_0)\) as a function of the natural logarithm of \(N\). The slope is \(-0.57\), which is also close to \(-1/2\), indicating that existence of the scaling relation between \(T_p\) and \(N\) for this thermally sensitive homopolymer.

**CONCLUSIONS**

By using a combination of free radical polymerization and fractional precipitation, a series of PNIPAM with narrowly distributed molar mass has been prepared. DSC measurements show that the \(T_{p,0}\) is proportional to \(N^{-1/2}\), which is consistent with theoretical results from Paul et al. Besides, poly(\(N,N\)-diethylacrylamide) has the same scaling relation between \(T_p\) and \(N\).

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REFERENCES AND NOTES