# 操作系统原理与设计 第9章 VM (虚存2)

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#### Page Replacement

- Basic Page Replacement
- First-In-First-Out (FIFO) Algorithm
- Optimal Algorithm
- Least Recently Used (LRU) Algorithm
- LRU Approximation Algorithms
- Counting Algorithms
- Page-Buffeing Algorithms
- 2 Allocation of Frames
- 3 小结和作业

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Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

# Page Replacement I

- Free page frame is managed by OS using free-frame-list
- What happens if there is no free frame?
  - $\bullet \ \Rightarrow \mathsf{Page \ replacement}$
- over-allocation
  - no free frames;
  - all memory is in use
- Prevent over-allocation of memory by modifying page-fault service routine to include page replacement
- example:

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Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

### Page Replacement II



Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

# Outline

#### 1 Page Replacement

#### • Basic Page Replacement

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Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

# Basic Page Replacement

- Find the location of the desired page on disk
- I Find a free frame:
  - If there is a free frame, use it
  - If there is no free frame, use a page replacement algorithm to select a victim frame
- Bring the desired page into the (newly) free frame; update the page and frame tables
- Restart the process

Basic Page Replacement

## Page Replacement



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Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

- NO MODIFY, NO WRITTEN (to disk/swap space)
  - Use modify (dirty) bit to reduce overhead of page transfers
    - only modified pages are written to disk
  - This technique also applies to read-only pages

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- for example, pages of binary code
- Page replacement completes separation between logical memory and physical memory
  - large virtual memory can be provided on a smaller physical memory
- demand paging, to lowest page-fault rate, two major problems
  - frame-allocation algorithms
  - page-replacement algorithms

Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

## Page Replacement Algorithms

- GOAL: to lowest page-fault rate
- Different algorithms are evaluated by running it on a particular string of memory references (reference string) and computing the number of page faults on that string

- A **reference string** is a sequence of addresses referenced by a program
- Example:
  - An address reference string:
     0100 0432 0101 0612 0102 0103 0104 0101 0611 0103 0104 0101 0610 0102 0103 0104 0101 0609 0102 0105

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### Page Replacement Algorithms II

- Assuming page size = 100 B, then its corresponding page reference string is:
   1 4 1 6 1 6 1 6 1 6 1
- how many page faults?
  - determined by the number of page frames assigned to the process
- if  $\geq 3,$  then only 3 page faults
- if = 1, 11 pages faults

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### Graph of Page Faults Versus The Number of Frames



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Page Replacement Allocation of Frames 小结和作业	Basic Page Replacement First-In-First-Out (FIFO) Algorithm Optimal Algorithm Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

• In all our examples, the reference string is

```
1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
```

• another one is

7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1



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# First-In-First-Out (FIFO) Algorithm I

#### • example 1



- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
  - if 3 frames

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# First-In-First-Out (FIFO) Algorithm II



• if 4 frames



● Belady's (贝莱迪) Anomaly: more frames ⇒ more page faults

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### FIFO Illustrating Belady' s Anomaly



• more memory, better performance? MAY BE NOT !!

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• Belady's anomaly

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Page Replacement Allocation of Frames 小结和作业 Optimal Algorithm Counting Algorithms Page-Buffeing Algorithms Page-Buffeing Algorithms

- Replace page that will not be used for longest period of time
- 4 frames example
  - 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5



- How do you know this?
- Used for measuring how well your algorithm performs

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Basic Page Replacement First-In-First-Out (FIFO) Algorithm **Optimal Algorithm** Least Recently Used (LRU) Algorithm LRU Approximation Algorithms Counting Algorithms Page-Buffeing Algorithms

### **Optimal Page Replacement**



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## Least Recently Used (LRU) Algorithm I

#### • Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5





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# Least Recently Used (LRU) Algorithm II

HOW to implement LRU replacement?

- **O Counter** implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
  - When a page needs to be changed, look at the counters to determine which are to change
- Stack implementation keep a stack of page numbers in a double link form:
  - Page referenced:
    - move it to the top
    - requires 6 pointers to be changed

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• No search for replacement

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# Least Recently Used (LRU) Algorithm III

• stack example:



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# LRU Approximation Algorithms I

- Reference bit
  - $\bullet\,$  With each page associate a bit, initially = 0
  - ${\scriptstyle \bullet}$  When page is referenced bit set to 1
  - Replace the one which is 0 (if one exists)
    - We do not know the order, however
- Additinal-Reference-Bits Algorithm
  - $\bullet~$  reference bits +~ time ordering, for example
    - 8 bits
    - HW modifies the highest bit, only
    - periodically, right shift the 8 bits for each page
    - 00000000, ..., 01110111, ..., 11000100, ..., 11111111

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## LRU Approximation Algorithms II

- Second chance Algorithm
  - Need 1 reference bit, modified FIFO algorithm
    - First, a page is selected by FIFO
    - then, the reference bit of the page is checked:
      - $0{\Rightarrow}\mathsf{replace} \text{ it }$
      - $1 \Rightarrow$  not replace it, get a second chance with reference bit:
      - 1 $\rightarrow$ 0, and time $\rightarrow$ current
  - Implementation: Clock replacement
    - clock order

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### LRU Approximation Algorithms III



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# LRU Approximation Algorithms IV

- Inhanced Second-Chance Algorhm
  - $\bullet~$  reference bit +~ modify bit
  - Four page classes (访问位,修改位)
    - (0, 0) best page to replace
    - (0, 1) not quite as good
    - (1, 0) probably be used again soon
    - (1, 1) probably be used again soon, and be dirty
  - Replace the first page encountered in the lowest nonempty class.
    - **1** Scan for (0, 0)
    - **2** Scan for (0, 1), & set reference bits to 0

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# Counting Algorithms

- Keep a counter of the number of references that have been made to each page
- LFU Algorithm: replaces page with smallest count
- **MFU Algorithm**: based on the argument that the page with the smallest count was probably just brought in and has yet to be used

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# Page-Buffeing Algorithms I

- system commonly keep a pool of free frames
- when replacement occurs, two frames are involved
  - a free frame from the pool is allocated to the process
    - the desired page is read into the frame
  - a viction frame is chosen
    - written out later and the frame is added to the free pool
  - NO NEED to write out before read in
- An expansion
  - maintain a list of modified pages

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# Page-Buffeing Algorithms II

- $\bullet\,$  when a paging device is idle, select a modified page, write it out, modify bit {\rightarrow} 0
- Another modification
  - free frame with old page
  - the old page can be reused
    - less write out and less read in
  - VAX/VMS
  - some UNIX: + second chance
  - ...

### Allocation of Frames

#### Image: minimum number of pages

- Each process needs minimum number of pages
- Determined by ISA (Instruction-Set Architecture )
  - We must have enough frames to hold all the different pages that any single instruction can reference

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Example: IBM 370

6 pages to handle SS MOVE instruction:

- instruction is 6 bytes, might span 2 pages
- 2 pages to handle from
- 2 pages to handle to

#### Two major allocation schemes

- fixed allocation ; priority allocation
- Two replacement policy
  - global vs. local

## Fixed Allocation I

 Equal allocation – For example, if there are 100 frames and 5 processes, give each process 20 frames.

frame number for any process =  $\frac{m}{n}$ m = total memory frames n = number of processes



### Fixed Allocation II

Proportional allocation – Allocate according to the size of process

• example:

- $s_i$  = size of process  $p_i$
- $S = \Sigma s_i$
- m = total number of frames
- $a_i$  = allocation for  $p_i = \frac{s_i}{S} \times m$

m = 64  $S_{1} = 10$   $S_{2} = 127$   $a_{1} = \frac{10}{137} \times 64 \approx 5$   $a_{2} = \frac{127}{137} \times 64 \approx 59$ 

## **Priority Allocation**

- Use a proportional allocation scheme using priorities rather than size
- If process  $P_i$  generates a page fault,
  - select for replacement one of its frames
  - select for replacement a frame from a process with lower priority number

### Global vs. Local Allocation

- Global replacement process selects a replacement frame from the set of all frames; one process can take a frame from another
  - problem: a process cannot control its own page-fault rate
- Local replacement each process selects from only its own set of allocated frames

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• problem?



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