#### **Pointer Analysis**

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Most content comes from <u>http://cs.au.dk/~amoeller/spa/</u> <u>http://staff.ustc.edu.cn/~yuzhang/pldpa</u>

# Agenda

- Introduction to pointer analysis
- Andersen's analysis
- Steensgaard's analysis
- Interprocedural pointer analysis
- Records and objects
- Null pointer analysis
- Flow-sensitive pointer analysis

# Analyzing Programs with Pointers

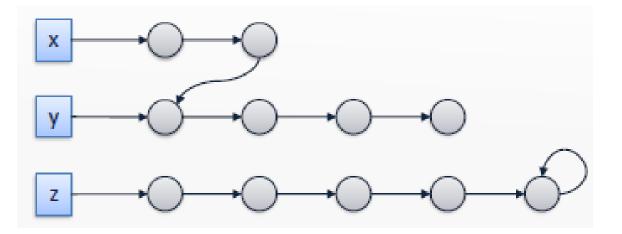
How do we perform e.g. constant propagation analysis when the programming language has pointers? (or object references?)

 $E \rightarrow \& X$ alloc E \*E null  $S \rightarrow *X = E;$ 

Depend on whether x and y point to the same location, if so, z is -87

#### **Heap Pointers**

- For simplicity, we ignore records
  - alloc then only allocates a single cell
  - only linear structures can be built in the heap



- Let's at first also ignore functions as values
- We still have many interesting analysis challenges...

# **Pointer Targets**

- The fundamental question about pointers: What cells can they point to?
  - p =alloc null alloc-1 \*p = z
- We need a suitable abstraction
- The set of (abstract) cells, Cells, contains
  - alloc-*i* for each allocation site with index *i*
  - X for each program variable named X
- This is called *allocation site abstraction*
- Each abstract cell may correspond to many concrete memory cells at runtime

## **Points-to Analysis**

- Determine for each pointer variable X the set pt(X) of the cells X may point to
  - \*x = 42; \*y = -87; z = \*x; // is z 42 or -87?
- A conservative ("may points-to") analysis:
  - the set may be too large
  - can show absence of aliasing:  $pt(X) \cap pt(Y) = \emptyset$
- We'll focus on *flow-insensitive* analyses:
  - Take place on the AST
  - Before or together with the control-flow analysis

# **Obtaining Points-to Information**

- An almost-trivial analysis (called address-taken 取址):
  - include all alloc-*i* cells 注:为程序正文中的分配点
  - Include the X cell if the expression &X occurs in the program

- Improvement for a typed language
  - Eliminate those cells whose types do not match

- This is sometimes good enough
  - and clearly very fast to compute

## **Pointer Normalization**

- Assume that all pointer usage is normalized:
  - X=alloc P where P is null or an integer constant
  - X=&Y
  - X=Y
  - X=\*Y
  - \*X=Y
  - X=null
- Simply introduce lots of temporary variables...
- All sub-expressions are now named
- We choose to ignore the fact that the cells created at variable declarations are uninitialized

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# Andersen's Analysis (1/2)

- For every cell *c*, introduce a constraint variable  $[\![c]\!]$  ranging over sets of cells, i.e.  $[\![\cdot]\!]$ : *Cells*  $\rightarrow \mathcal{P}(Cells)$
- Generate constraints:
  - X = alloc P:
  - X = &Y:
  - X = Y:
  - X = \*Y:
  - \*X = Y:
  - *X* = null:

alloc- $i \in [X]$   $Y \in [X]$   $[Y] \subseteq [X]$   $c \in [Y] \Rightarrow [c] \subseteq [X]$  for each  $c \in Cells$   $c \in [X] \Rightarrow [Y] \subseteq [c]$  for each  $c \in Cells$ (no constraints)

基于集合的包含关系

(For the conditional constraints, there's no need to add a constraint for the cell x if &x does not occur in the program)

#### Andersen's Analysis (2/2)

- The points-to map is defined as:
   pt(X) = [X]
- The constraints fit into the cubic framework <sup>(2)</sup>
- Unique minimal solution in time O(n<sup>3</sup>)
- In practice, for Java: O(n<sup>2</sup>)
- The analysis is flow-insensitive but directional
  - models the direction of the flow of values in assignments

#### **Example Program**

var p,q,x, p = alloc x = y;		
x = y; x = z;	X=alloc P:	$alloc-i \in [X]$
	X = &Y:	$Y \in \llbracket X \rrbracket$
*p = z;	X = Y:	$\llbracket Y \rrbracket \subseteq \llbracket X \rrbracket$
p = q;	X = *Y:	$c \in \llbracket Y \rrbracket \Rightarrow \llbracket c \rrbracket \subseteq \llbracket X \rrbracket$ for each $c \in Cells$
q = &y	*X = Y:	$c \in \llbracket X \rrbracket \Rightarrow \llbracket Y \rrbracket \subseteq \llbracket c \rrbracket$ for each $c \in Cells$
x = *p;	X = null:	(no constraints)
x = p; p = &z		

*Cells*= {p, q, x, y, z, alloc-1}

# **Applying Andersen**

```
var p,q,x,y,z;
p = alloc null;
x = y;
X = Z;
*p = z;
p = q;
q = &y;
x = *p;
p = \&z;
```

alloc-1  $\in [\![p]\!]$   $[\![Y]\!] \subseteq [\![X]\!]$   $[\![Z]\!] \subseteq [\![X]\!]$   $c \in [\![p]\!] \Rightarrow [\![Z]\!] \subseteq [\![\alpha]\!]$  for each  $c \in Cells$   $[\![q]\!] \subseteq [\![p]\!]$   $y \in [\![q]\!]$   $c \in [\![p]\!] \Rightarrow [\![\alpha]\!] \subseteq [\![X]\!]$  for each  $c \in Cells$  $Z \in [\![p]\!]$ 

Smallest solution:  $pt(p) = \{ alloc-1, y, z \}$   $pt(q) = \{ y \}$  $pt(x) = pt(y) = pt(z) = \phi$  13

# A Specialized Cubic Solver

 At each load/store instruction, instead of generating a conditional constraint for each cell, generate a single universally quantified constraint:



- $\llbracket x \rrbracket \subseteq \llbracket y \rrbracket$
- $\forall t \in \llbracket x \rrbracket \colon \llbracket t \rrbracket \subseteq \llbracket y \rrbracket$

•  $\forall t \in \llbracket x \rrbracket \colon \llbracket y \rrbracket \subseteq \llbracket t \rrbracket$ 

**Original constraint forms** 

• 
$$t \in x$$
  
•  $t \in x \Rightarrow y \subseteq z$ 

- Whenever a token is added to a set, lazily add new edges according to the universally quantified constraints
- Note that every token is also a constraint variable here
- Still cubic complexity, but faster in practice

# A Specialized Cubic Solver

- x.sol ⊆ T: the set of tokens for x (the bitvectors)
- x.succ ⊂ V: the successors of x (the edges)
- x.from  $\subseteq$  V: the first kind of quantified constraints for x
- x.to  $\subseteq$  V: the second kind of quantified constraints for x
- W ⊆ T×V: a worklist (initially empty)

#### Implementation: SpecialCubicSolver

#### A Specialized Cubic Solver

- *t* ∈ [[*x*]] addToken(t, x) propagate()
- [[X]] ⊆ [[Y]] addEdge(x, y) propagate()
- ∀t ∈ [[x]]: [[t]] ⊆ [[y]]
   add y to x.from
   for each t in x.sol
   addEdge(t, y)
   propagate()

∀t ∈ [[x]]: [[y]] ⊆ [[t]]
 add y to x.to
 for each t in x.sol
 addEdge(y, t)
 propagate()

addToken(t, x): if t∉x.sol add t to x.sol add (t, x) to W

addEdge(x, y): if x ≠ y ∧ y ∉ x.succ add y to x.succ for each t in x.sol addToken(t, y)

propagate(): while W ≠ Ø pick and remove (t, x) from W for each y in x.from addEdge(t, y) for each y in x.to addEdge(y, t) for each y in x.succ addToken(t, y)

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# Steensgaard's Analysis

- View assignments as being bidirectional
- Generate constraints:
  - X = alloc P:
  - X = &Y:
  - X = Y:
  - X = \*Y:
  - \*X = Y:

alloc- $i \in [X]$ 

基于类型及其

 $Y \in \llbracket X \rrbracket$ [X] = [Y]

- $c \in [Y] \implies [c] = [X]$  for each  $c \in Cells$
- $c \in [X] \implies [Y] = [c]$  for each  $c \in Cells$

Extra constraints:

 $\mathbf{c}_1, \mathbf{c}_2 \in [\mathbf{c}] \Longrightarrow [\mathbf{c}_1] = [\mathbf{c}_2] \text{ and } [\mathbf{c}_1] \cap [\mathbf{c}_2] \neq \emptyset \Longrightarrow [\mathbf{c}_1] = [\mathbf{c}_2]$ (whenever a cell may point to two cells, they are essentially merged into one)

Steensgaard's original formulation uses conditional unification for X = Y:  $c \in \llbracket Y \rrbracket \Rightarrow \llbracket X \rrbracket = \llbracket Y \rrbracket$  for each  $c \in Cells$  (avoids unifying if Y is never a pointer)

价关系

## Steensgaard's Analysis

- Reformulate as term unification
- Generate constraints:
  - X = alloc P: [X] = f[alloc P]
  - X = &Y:
  - *X* = *Y*:
  - X = \*Y:
  - \*X = Y:

 $\begin{bmatrix} X \end{bmatrix} = \mathbf{\hat{1}} \begin{bmatrix} a \\ a \end{bmatrix} \mathbf{oc} - i \end{bmatrix}$  $\begin{bmatrix} X \end{bmatrix} = \mathbf{\hat{1}} \begin{bmatrix} Y \end{bmatrix}$  $\begin{bmatrix} X \end{bmatrix} = \begin{bmatrix} Y \end{bmatrix}$  $\begin{bmatrix} X \end{bmatrix} = \begin{bmatrix} Y \end{bmatrix}$ 

- \*Y:  $[[Y]] = \mathbf{1} \alpha \land [[X]] = \alpha$  where  $\alpha$  is fresh = Y:  $[[X]] = \mathbf{1} \alpha \land [[Y]] = \alpha$  where  $\alpha$  is fresh
- Terms:
  - term variables, e.g. [X], [a]loc-i],  $\alpha$  (each representing the possible values of a cell)
  - each a single (unary) term constructor 1 t (representing pointers)
  - each [[c]] is now a term variable, not a constraint variable holding a set of cells
- Fits with our unification solver! (union-find...)
- The points-to map is defined as pt(X) = { c∈Cells | [[X]] = ↑ [[c]] }
- Note that there is only one kind of term constructor, so unification never fails,

# **Applying Steensgaard**

var p,q,x,y,z; p = alloc null;x = y;X = Z;\*p = z;p = q;q = &y;x = \*p;p = &z;

$$[p] = f[a]loc-1]$$
  

$$[y] = [x]$$
  

$$[z] = [x]$$
  

$$[p] = f \alpha_1 \quad [z] = \alpha_1$$
  

$$[q] = [p]$$
  

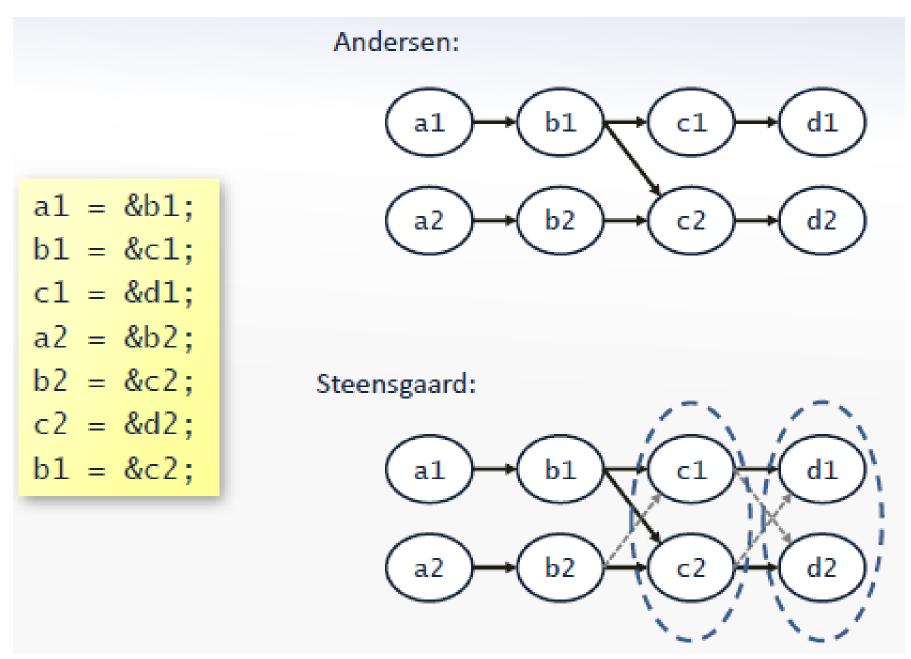
$$[q] = f[y]$$
  

$$[p] = f \alpha_2 \quad [x] = \alpha_2$$
  

$$[p] = f [z]$$

Smallest solution: pt(p) = { alloc-1, y, z} pt(q) = {alloc-1, y, z}

#### Another Example



# Recall Our Type Analysis...

- Focusing on pointers...
- Constraints:
  - X = alloc P: [X] = f[P]
  - X = &Y: [X] = 1 [Y]
  - X = Y:  $\llbracket X \rrbracket = \llbracket Y \rrbracket$
  - X = \*Y: **1**  $\llbracket X \rrbracket = \llbracket Y \rrbracket$
  - \*X = Y: [X] = 1 [Y]
- Implicit extra constraint for term equality:  $\mathbf{1}_1 = \mathbf{1}_2 \Longrightarrow t_1 = t_2$
- Assuming the program type checks, is the solution for pointers the same as for Steensgaard's analysis?

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# Interprocedural Points-to Analysis

 In TIP, function values and pointers may be mixed together:

(\*\*\*x)(1,2,3)

 In this case the CFA and the points-to analysis must happen simultaneously!

The idea: Treat function values as a kind of pointers

#### **Function Call Normalization**

• Assume that all function calls are of the form

 $x = y(a_1,...,a_n)$ 

- y may be a variable whose value is a function pointer
- Assume that all return statements are of the form return z;
- As usual, simply introduce lots of temporary variables...
- Include all function names in Cells

#### CFA with Andersen

- For the function call x = y(a<sub>1</sub>, ..., a<sub>n</sub>) and every occurrence of f(x<sub>1</sub>, ..., x<sub>n</sub>) { ... return z; } add these constraints:
   Andersen's analysis is already closely connected to control-flow analysis!
  - $f \in \llbracket f \rrbracket$  $f \in \llbracket y \rrbracket \Rightarrow (\llbracket a_i \rrbracket \subseteq \llbracket x_i \rrbracket \text{ for } i=1,...,n \land \llbracket z \rrbracket \subseteq \llbracket x \rrbracket)$
- (Similarly for simple function calls)
- Fits directly into the cubic framework!

## CFA with Steensgaard

For the function call

 x = y(a<sub>1</sub>, ..., a<sub>n</sub>)
 and every occurrence of
 f(x<sub>1</sub>, ..., x<sub>n</sub>) { ... return z; }
 add these constraints:

 $f \in \llbracket f \rrbracket$  $f \in \llbracket y \rrbracket \Rightarrow (\llbracket a_i \rrbracket = \llbracket x_i \rrbracket \text{ for } i=1,...,n \land \llbracket z \rrbracket = \llbracket x \rrbracket)$ 

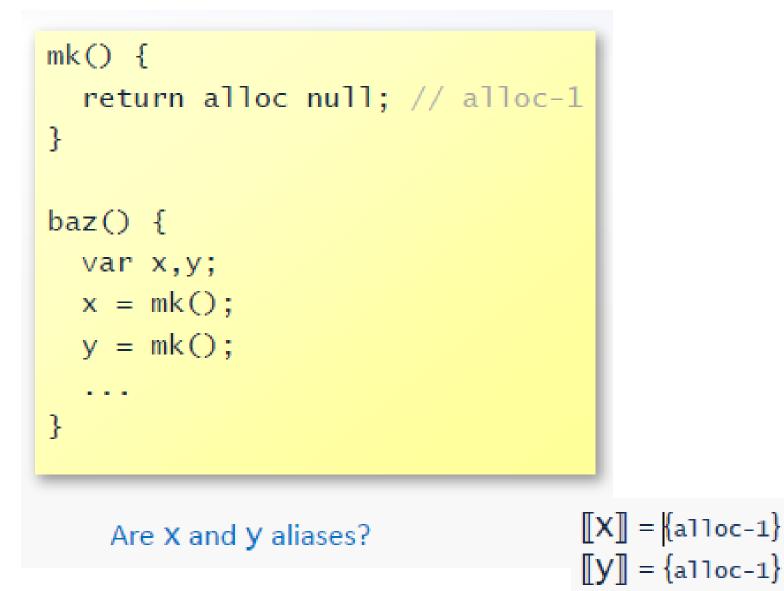
- (Similarly for simple function calls)
- Fits into the unification framework, but requires a generalization of the ordinary union-find solver

```
foo(a) {
  return *a;
}
bar() {
  x = alloc null; // alloc-1
  y = alloc null; // alloc-2
  *x = alloc null; // alloc-3
  *y = alloc null; // alloc-4
  q = foo(x);
  w = foo(y);
}
```

- Generalize the abstract domain  $Cells \rightarrow P(Cells)$  to  $Contexts \rightarrow Cells \rightarrow P(Cells)$ (or equivalently:  $Cells \times Contexts \rightarrow P(Cells)$ ) where Contexts is a (finite) set of call contexts
- As usual, many possible choices of *Contexts*
  - recall the call string approach and the functional approach
- We can also track the set of reachable contexts (like the use of lifted lattices earlier):

 $Contexts \rightarrow lift(Cells \rightarrow \mathcal{P}(Cells))$ 

Does this still fit into the cubic solver?



- We can go one step further and introduce *context*sensitive heap (a.k.a. *heap cloning*)
- Let each abstract cell be a pair of
  - alloc-*i* (the alloc with index *i*) or *X* (a program variable)
  - a heap context from a (finite) set HeapContexts
- This allows abstract cells to be named by the source code allocation site

#### and (information from) the current context

- One choice:
  - set *HeapContexts* = *Contexts*
  - at alloc, use the entire current call context as heap context

# Context-sensitive Pointer Analysis with Heap Cloning

Assuming we use the call string approach with k=1, so Contexts = { $\epsilon$ , C1, C2}, and HeapContexts = Contexts

```
mk() {
   return alloc null; // alloc-1
}
baz() {
   var x,y;
   x = mk(); // c1
   y = mk(); // c2
   ...
}
```

Are x and y aliases?

[[X]] = { (alloc-1, c1) }
[[Y]] = { (alloc-1, c2) }

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#### Records in TIP

- Field write operations: see SPA ...
- Values of record fields cannot themselves be records
- After normalization

- 
$$X = \{F_1: X_1, \dots, F_k: X_k\}$$

- $X = alloc{F_1: X_1, \dots, F_k: X_k}$
- X= Y.F

Let us extend Andersen's analysis accordingly ...

#### **Constraint Variables for Record Fields**

•  $\llbracket \cdot \rrbracket$ : (*Cells*  $\cup$  (*Cells*  $\times$  *Fields*))  $\rightarrow \mathcal{P}(Cells$ ) where is the set of field names in the program

Notation: [[c . f]] means [[(c, f)]]

#### Analysis Constraints

- $X = \{F_1: X_1, \dots, F_k: X_k\}$ :  $[X_1] \subseteq [X.F_1] \land \dots \land [X_k] \subseteq [X.F_k]$
- $X = \text{alloc} \{ F_1 : X_1, \dots, F_k : X_k \}$ :  $\text{alloc} -i \in \llbracket X \rrbracket \land$  $\llbracket X_1 \rrbracket \subseteq \llbracket \text{alloc} -i.F_1 \rrbracket \land \dots \land \llbracket X_k \rrbracket \subseteq \llbracket \text{alloc} -i.F_k \rrbracket$
- X = Y.F:  $\llbracket Y.F \rrbracket \subseteq \llbracket X \rrbracket$
- X = Y:  $[Y] \subseteq [X] \land [Y.F] \subseteq [X.F]$  for each  $F \in Fields$
- X = \*Y:  $c \in \llbracket Y \rrbracket \Rightarrow (\llbracket c \rrbracket \subseteq \llbracket X \rrbracket \land \llbracket c.F \rrbracket \subseteq \llbracket X.F \rrbracket)$ for each  $c \in Cells$  and  $F \in Fields$
- \*X = Y:  $c \in [X] \implies ([Y] \subseteq [c] \land [Y.F] \subseteq [c.F])$ for each  $c \in Cells$  and  $F \in Fields$

See example in SPA

#### **Objects as Mutable Heap Records**

$$Exp \rightarrow \dots$$

$$| Id$$

$$| alloc \{ Id: Exp, \dots, Id: Exp \}$$

$$| (*Exp) . Id$$

$$| null$$

$$Stm \rightarrow \dots$$

- E.X in Java corresponds to (\*E).X in TIP (or C)
- Can only create pointers to heap-allocated records (=objects), not to variables or to cells containing non-record values

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## **Null Pointer Analysis**

- Decide for every dereference \*p, is p different from null?
- (Why not just treat null as a special cell in an Andersen or Steensgaard-style analysis?)
- Use the monotone framework
  - Assuming that a points-to map *pt* has been computed
- Let us consider an intraprocedural analysis (i.e. we ignore function calls)

#### A Lattice for null Analysis

• Define the simple lattice Null:

? | NN

where NN represents "definitely not null" and ? represents "maybe null"

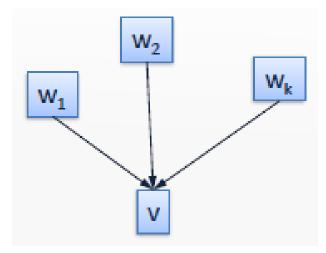
• Use for every program point the map lattice:  $Cells \rightarrow Null$ 

# Setting Up

- For every CFG node, v, we have a variable [[v]]:
  - a map giving abstract values for all cells at the program point after v

• Auxiliary definition:

 $JOIN(v) = \bigsqcup_{w \in pred(v)} \llbracket w \rrbracket$ 



(i.e. we make a *forward* analysis)

- For operations involving pointers:
  - X = alloc P: [[v]]= ???
  - X = & Y: [v] = ???
  - X = Y: [v] = ???
  - X = Y: [v] = ???
  - \*X = Y: [v] = ???
  - X = null: [[v]] = ???
- For all other CFG nodes:
  - [[v]]= *JOIN*(v)

where *P* is null or an integer constant

- For a heap store operation \*X = Y we need to model the change of whatever X points to
- That may be *multiple* abstract cells(i.e. the cells *pt*(X))
- With the present abstraction, each abstract heap cell alloc-*i* may describe *multiple* concrete cells
- So we settle for weak update:

\*X = Y:  $\llbracket v \rrbracket = store(JOIN(v), X, Y)$ 

where

$$store(\sigma, X, Y) = \sigma[\underset{\alpha \in pt(X)}{\alpha \in pt(X)} \sqcup \sigma(Y)]$$

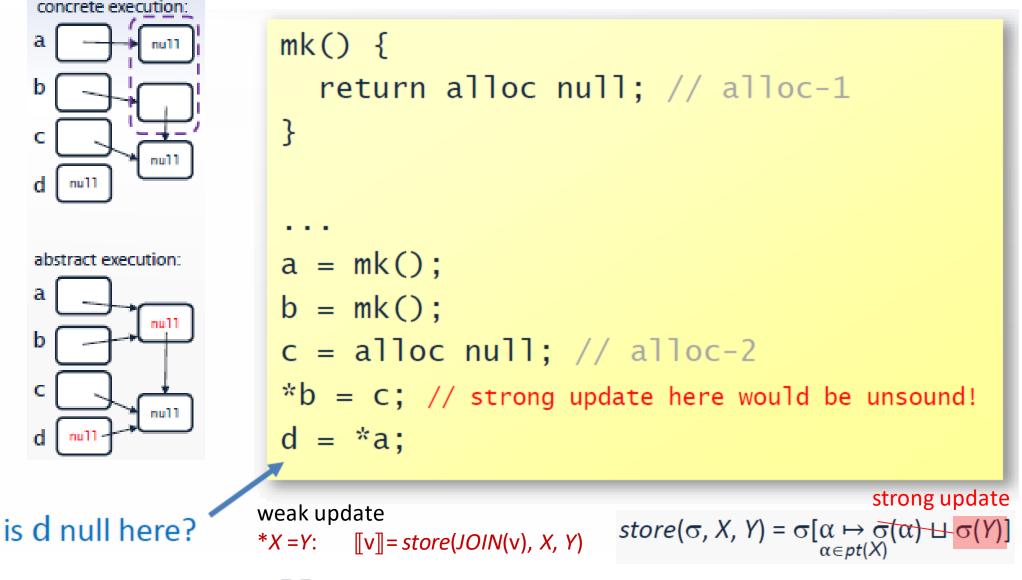
- For a heap load operation X = \*Y we need to model the change of the program variable X
- Our abstraction has a *single* abstract cell for *X*
- That abstract cell represents a single concrete cell
- So we can use **strong** update:

X = Y:  $\llbracket v \rrbracket = Ioad(JOIN(v), X, Y)$ 

where

$$load(\sigma, X, Y) = \sigma[X \mapsto \bigsqcup_{\alpha \in pt(Y)} \sigma(\alpha)]$$

#### Strong and Weak Updates



The abstract cell alloc-1 corresponds to *multiple concrete cells* 

#### Strong and Weak Updates

```
a = alloc null; // alloc-1
                 b = alloc null; // alloc-2
                 *a = alloc null; // alloc-3
                 *b = alloc null; // alloc-4
                 if (...) {
                  x = a;
                 } else {
                  x = b;
                 }
                 n = null;
                 *X = n; // strong update here would be unsound!
is C null here?
                 c = *x;
```

The points-to set for x contains *multiple abstract cells* 

- X = alloc P:  $[v] = JOIN(v)[X \mapsto NN, alloc-i \mapsto ?]$
- X = &Y:  $\llbracket v \rrbracket = JOIN(v)[X \mapsto NN]$
- X = Y:  $\llbracket v \rrbracket = JOIN(v)[X \mapsto JOIN(v)(Y)]$
- $X = null: [v] = JOIN(v)[X \mapsto ?]$
- In each case, the assignment modifies a program variable
- So we can use strong updates, as for heap load operations

could be improved ...

#### Strong and Weak Updates, Revisited

- Strong update: σ[c→new-value]
  - possible if *c* is known to refer to a single concrete cell
  - works for assignments to local variables (as long as TIP doesn't have e.g. nested functions)
- Weak update:  $\sigma[c \mapsto \sigma(c) \sqcup new-value]$ 
  - necessary if c may refer to multiple concrete cells
  - bad for precision, we lose some of the power of flowsensitivity
  - required for assignments to heap cells (unless we extend the analysis abstraction!)

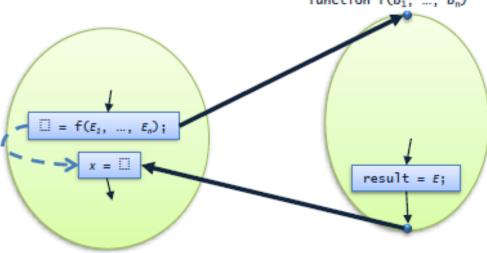
## Interprocedural Null Analysis

- Context insensitive or context sensitive, as usual...
  - at the after-call node, use the heap from the callee
- But be careful!

Pointers to local variables may escape to the callee

- the abstract state at the after-call node cannot simply copy the abstract values for local variables from the abstract state





## Using the Null Analysis

 The pointer dereference \*p is "safe" at entry of v if *JOIN*(v)(p) = NN

• The quality of the null analysis depends on the quality of the underlying points-to analysis

#### **Example Program & Constraints**

```
p = alloc null;
q = &p;
n = null;
*q = n;
*p = n;
```

Andersen generates:  $pt(p) = \{alloc-1\}$   $pt(q) = \{p\}$  $pt(n) = \emptyset$ 

```
 [p=alloc null] = \bot[p \mapsto NN, alloc-1 \mapsto ?] 
 [q=&p]] = [[p=alloc null]][q \mapsto NN] 
 [n=null]] = [[q=&p]][n \mapsto ?] 
 [[*q=n]] = [[n=null]][p \mapsto [[n=null]](p) \sqcup [[n=null]](n)] 
 [[*p=n]] = [[*q=n]][alloc-1 \mapsto [[*q=n]](alloc-1) \sqcup [[*q=n]](n)]
```

#### Solution

$$\begin{split} & [[p=alloc null]]=[p\mapsto NN, q\mapsto NN, n\mapsto NN, alloc-1\mapsto?] \\ & [[q=&p]]=[p\mapsto NN, q\mapsto NN, n\mapsto NN, alloc-1\mapsto?] \\ & [[n=null]]=[p\mapsto NN, q\mapsto NN, n\mapsto?, alloc-1\mapsto?] \\ & [[*q=n]]=[p\mapsto?, q\mapsto NN, n\mapsto?, alloc-1\mapsto?] \\ & [[*p=n]]=[p\mapsto?, q\mapsto NN, n\mapsto?, alloc-1\mapsto?] \end{split}$$

- At the program point before the statement \*q=n the analysis now knows that q is definitely non-null
- ... and before \*p=n, the pointer p is may be null
- Due to the weak updates for all heap store operations, precision is bad for alloc-i cells

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#### Points-to Graphs

- Graphs that describe possible heaps:
  - nodes are abstract cells
  - edges are possible pointers between the cells
- The lattice of points-to graphs is *P*(Cells × Cells) ordered under subset inclusion (or alternatively, *Cells*→*P*(Cells))
- For every CFG node, v, we introduce a constraint variable [[v]] describing the state after v
- Intraprocedural analysis (i.e. ignore function calls)

#### Constraints

- For pointer operations:
  - X = alloc P:  $[v] = JOIN(v) \downarrow X \cup \{(X, alloc-i)\}$
  - X = &Y:  $[v] = JOIN(v) \downarrow X \cup \{(X, Y)\}$
  - X = Y:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{ (X, t) \mid (Y, t) \in JOIN(v) \}$
  - X = \*Y:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{ (X, t) \mid (Y, s) \in \sigma, (s, t) \in JOIN(v) \}$
  - \*X = Y:  $[v] = JOIN(v) \cup \{(s, t) \mid (X, s) \in JOIN(v), (Y, t) \in JOIN(v)\}$
  - $X = \text{null:} [v] = JOIN(v) \downarrow X$

note: weak update!

where  $\sigma \downarrow X = \{ (s,t) \in \sigma \mid s \neq X \}$ 

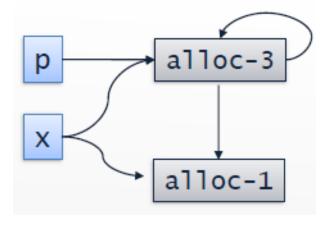
 $JOIN(v) = \bigcup_{w \in pred(v)} [w]$ 

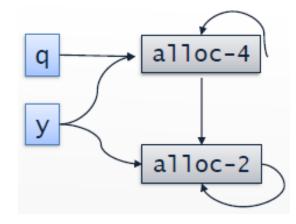
- For all other CFG nodes:
  - [[v]] = JOIN(v)

#### Example Program

#### **Result of Analysis**

• After the loop we have this points-to graph:





 We conclude that x and y will always be disjoint

```
var x,y,n,p,q;
x = alloc null; y = alloc null;
*x = null; *y = y;
n = input;
while (n>0) {
    p = alloc null; q = alloc null;
    *p = x; *q = y;
    x = p; y = q;
    n = n-1;
}
```

#### Points-to Maps from Points-to Graphs

A points-to map for each program point v:

 $pt(X) = \{ t \mid (X, t) \in [\![V]\!] \}$ 

- More expensive, but more precise:
  - Andersen:
  - flow-sensitive:

$$pt(x) = \{ y, z \}$$

$$pt(x) = \{ z \}$$

#### Improving Precision with Abstract Counting

- The points-to graph is missing information:
   alloc-2 nodes always form a self-loop in the example
- We need a more detailed lattice:

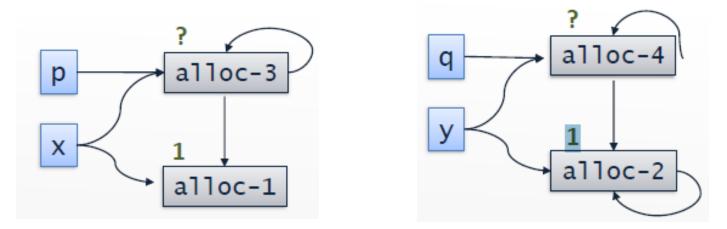
 $2^{Cell \times Cell} \times (Cell \rightarrow Count)$ 

where we for each cell keep track of how many concrete cells that abstract cell describes

- Count = 0
- This permits strong updates on those that describe precisely 1 concrete cell

#### **Constraints and Better Results**

- *X* = alloc *P*: ...
- \*X=Y: ...
- •
- After the loop we have this extended points-to graph:



• Thus, alloc-2 nodes form a self-loop

### **Escape Analysis**

- Perform a points-to analysis
- Look at return expression
- Check reachability in the points-to graph to arguments or variables defined in the function itself
- None of those
   ↓

no escaping stack cells

```
baz() {
  var x;
  return &x;
}
main() {
  var p;
  p=baz();
  *p=1;
  return *p;
```

#### THANKS