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Overloading and Type Classes

(Adhoc Polymorphism)

《程序语言设计和程序分析》

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- **D. Rémy**([Cambium](#) project-team): [Type systems for PLs](#)
 - Chapter 7 Overloading
- **[Concepts in PLs]** [Revised Chapter 7 Type Classes](#)
- [PFPL](#)
 - Chapter 44 Type Abstractions and Type Classes
- **Papers**
 - [\[ESOP 1988\]](#) Parametric Overloading in Polymorphic PLs
 - [\[POPL 2007\]](#) Modular Type Classes
- **Implementation**
 - [Implementing, and Understanding Type Classes](#)
 - [Implementing type classes as OCaml modules](#)
- **Types and Propositions:**
 - [\[TPHOLs 1997\]](#) Type classes and overloading in higher-order logic



- **Parametric Polymorphism vs. Overloading**
- **Why Overloading**
- **Overloading Mechanisms**
 - **Static / dynamic resolution of overloading**
- **Parametric Overloading and Type Classes**
 - also known as bounded polymorphism, or type classes
 - **Dictionary passing**
 - **Macro**
 - **Intentionally type analysis**



□ Parametric polymorphism

- Single algorithm for *any* type

If $f:t \rightarrow t$, then $f:\text{int} \rightarrow \text{int}$, $f:\text{bool} \rightarrow \text{bool}$, ...

□ Overloading

- Single symbol may refer to different algorithms/operations.
- Each algorithm may have different unrelated type.
- Choice of algorithm determined by type context.

□ Parametric overloading

- The types being instances of a single type expression over some extended set of type variables
 - + has types $\text{int} \rightarrow \text{int} \rightarrow \text{int}$, $\text{float} \rightarrow \text{float} \rightarrow \text{float}$,
 - but not $X \rightarrow X \rightarrow X$ for any X .



Why Overloading ?

- Many useful functions are not parametric
- Can list membership work for any type?

$\text{member} : \forall X. X \text{ list} \rightarrow X \rightarrow \text{bool}$

- Can list sorting work for any type?

$\text{sort} : \forall X. X \text{ list} \rightarrow X \text{ list}$



Why Overloading ?

□ Many useful functions are not parametric

□ Can list membership work for any type?

$\text{member} : \forall X. X \text{ list} \rightarrow X \rightarrow \text{bool}$

■ **No!** Only for types X that support **equality**.

□ Can list sorting work for any type?

$\text{sort} : \forall X. X \text{ list} \rightarrow X \text{ list}$

■ **No!** Only for types X that support **ordering**.



Variants of Overloading

- **Static overloading: *static* resolution strategy**
 - Simple semantics: meaning determined statically
 - Does not increase expressiveness
 - Reduce verbosity, increase modularity and abstraction
- **Dynamic overloading**
 - meaning determined dynamically
 - Increase expressiveness
 - Extra mechanism to support the dynamic resolution
 - Require full or partial type info., or some type-related info.



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Overloading Mechanisms



□ Approach 1:

A function containing overloaded symbols => multiple functions

□ e.g. `double x = x + x`

defines two versions: `Int -> Int` and `Float -> Float`

But, how to resolve

`doubles (x, y, z) = (double x, double y, double z)`

□ 8 possible versions!

=> *Exponential growth in number of versions*



□ Approach 2 (used in SML-[MLton](#)):

restrict the definition, i.e., specify one of the possible versions as the meaning

■ e.g. `double x = x + x` \Rightarrow `double: Int -> Int`

`double 3` ✓

`double 3.2` ✗

If you want `double: Float -> Float`, you need define the function explicitly specifying type.

□ In Java

■ Overloading a method in a class \Rightarrow static resolution

■ But if an argument has a runtime type that is subtype of the compile-time type
 \Rightarrow dynamic resolution



Dynamic Overloading

□ Resolution with a type passing semantics

Runtime type dispatch using a general *typecase* construct

- **High runtime cost** of *typecase* unless type patterns are significantly restricted

□ Resolution with a type erasing semantics

To avoid the expensive cost of *typecase*,

restrict the overloaded functions by using tags.

$$\text{let } f = \lambda x.x + x \text{ in } []$$

e.g. Dictionary passing

can be elaborated into

$$\text{let } f = \lambda(+).\lambda x.x + x \text{ in } []$$

f 1.0 is then elaborated to **f (+.) 1.0**



□ Overloading Equality

1. Equality was overloaded as an operator.

But *member* using `'=='` does not work in general

`member [] y = False`

`member (x : xs) y = (x == y) || member xs y`

`member [1, 2, 3] 32 ✓`

`member "Haskell" 'k' ✗`



□ Overloading Equality

1. Equality was overloaded as an operator.
But *member* using '==' does not work in general
2. Make type of equality fully polymorphic (Miranda)

$(==) :: t \rightarrow t \rightarrow \text{Bool}$

thus *member* is polymorphic, $\text{member} :: [t] \rightarrow t \rightarrow \text{Bool}$

If t does not provide a definition of equality, then there is a **runtime error** when equality applied to a value of type t .

\Rightarrow Violate principle of abstraction



□ Overloading Equality

1. Equality was overloaded as an operator.
But *member* using '==' does not work in general
2. Make type of equality fully polymorphic (Miranda)
3. Make equality polymorphic in a limited way
(used in current SML)

$(==) :: 't \rightarrow 't \rightarrow \text{Bool}$ "'t indicate t is an eqtype variable

member has precise type, i.e. $['t] \rightarrow 't \rightarrow \text{Bool}$

if t does not support equality, there will be a **static error**



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if t does not support equality, there will be a **static** error

**Equality is a special case,
how can we generalize overloading?**



□ Type classes are a mechanism in Haskell

- Generalize `eqtype` to user-defined collections of types (called *type classes*)

`member :: (a -> a -> Bool) -> [a] -> a -> Bool`

`member cmp [] y = False`

`member cmp (x : xs) y = (cmp x y) || member cmp xs y`

□ Dictionary-passing style implementation [[ESOP1988](#)]

- Type-class declaration – `dictionary`
- Name of a type class method – `label in the dictionary`
- Parametric overloading
 - `pass the dictionary to the function`

<https://okmij.org/ftp/Computation/typeclass.html>



Examples: Dictionary Passing

□ Haskell

```
class Show a where  
  show :: a -> String
```

```
instance Show Bool where  
  show True = "True "  
  show False = "False "
```

```
instance Show Int where  
  show x = Prelude.show x --  
internal
```

In Haskell

- `Show a` is type class
- `Show Bool` and `Show Int` are instances of `Show`.



□ OCaml

```
type 'a show = {show: 'a ->  
string}
```

```
let show_bool : bool show =  
  {show = function  
    | true -> "True "  
    | false -> "False"}
```

```
let show_int : int show =  
  {show = string_of_int}
```

In OCaml

- `'a show` is dictionary
- `show_bool` and `show_int` are labels in the dictionary.



Examples: Dictionary Passing

□ Haskell

```
class Show a where  
  show :: a -> String
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instance Show Bool where  
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```

```
instance Show Int where  
  show x = Prelude.show x -- internal
```

Define an overloaded function **print**:

```
print :: Show a => a -> IO ()  
print x = putStrLn $ show x
```

```
test_print :: IO ()  
test_print = print True
```

- **print** is a **restricted** polymorphic function, and it applies to values *whose types are showable*
- In Haskell: **Show Bool** and **Show Int** are members of **Show** class.
- In OCaml: the evidence of being showable, the dictionary, is the explicit argument.

□ OCaml

```
type 'a show = {show: 'a -> string}
```

```
let show_bool : bool show =  
  {show = function  
    | true -> "True "  
    | false -> "False"}
```

```
let show_int : int show =  
  {show = string_of_int}
```

```
let print : 'a show -> 'a -> unit =  
  fun {show=show} x -> print_endline (show x)
```

```
let test_print : unit =  
  print show_bool true
```



□ Type class whose methods have a different of overloading: e.g. Num

□ An instance with a constraint:

e.g. a Show instance for all list types `[a]` where the element type `a` is also restricted to be a member of Show.

`show_list: 'a show -> 'a list show (OCaml)`

□ A class of comparable types

e.g. class `Eq a` (Haskell) or type `'a eq` (OCaml)

□ Polymorphic recursion

See <http://okmij.org/ftp/Computation/typeclass.html#dict>



□ Type classes as macros

■ Static monomorphization (compile-time)

□ Take the **type-checked** code with type classes

□ Generate code with no type classes and no bounded polymorphism

vs. C++ templates ? Template instantiation may produce ill-typed code

□ Intentional type analysis (run-time)

Choose the appropriate overloading operation at run-time

See <http://okmij.org/ftp/Computation/typeclass.html#dict>



THANKS

- Rust支持trait，这是具有一致性的有限形式的类型类
- 在Scala中，类型类是编程惯例，可以用现存语言特征比如隐式参数来实现，本身不是独立的语言特征