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# Why Program Analysis

## (Static and Dynamic Analysis)

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# Code Review



## □ Different types of reviews

- Code/design review
- Informal walkthrough
- Formal inspection

**A requirement for many safety-critical systems.**



## □ Different types of reviews

- Code/design review
- Informal walkthrough
- Formal inspection

```
double foo(double[] d) {  
    int n = d.length;  
    double s = 0;  
    int i = 0;  
    while (i<n){  
        s = s + d[i];  
        i = i + 1;}  
    double a = s / n;  
    return a;  
}
```

What can we improve in this (Java) code?



## □ Different types of reviews

- Code/design review
- Informal walkthrough
- Formal inspection

```
double foo(double[] d) {  
    int n = d.length;  
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    int i = 0;  
    while (i<n){  
        s = s + d[i];  
        i = i + 1;}  
    double a = s / n;  
    return a;  
}
```

- Naming
- Indent
- New line

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0;  
    while (i<n) {  
        sum = sum + nums[i];  
        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

What can we improve in this (Java) code?



## □ In function `SSLVerifySignedServerKeyExchange` ([sslKeyExchange.c](#))

```
if ((err = SSLHashSHA1.update(&hashCtx, &serverRandom)) != 0)
    goto fail;
if ((err = SSLHashSHA1.update(&hashCtx, &signedParams)) != 0)
    goto fail;
    goto fail;
if ((err = SSLHashSHA1.final(&hashCtx, &hashOut)) != 0)
    goto fail; ...
```

Apple's "goto fail" bug:  
A security vulnerability for 2 years!



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# Terminology about PA



# Terminology and Important Concepts

- Precision vs. Recall (and FP/FN/TP/TN)
- Soundness vs. Completeness
- Concrete domain vs. Abstract domain
- Accuracy vs. Precision (and conservative analysis)





# Precision vs. Recall

## □ FP/FN/TP/TN

		Analysis result	
		Positive	Negative
Ground Truth	Positive		
	Negative		



# Precision vs. Recall

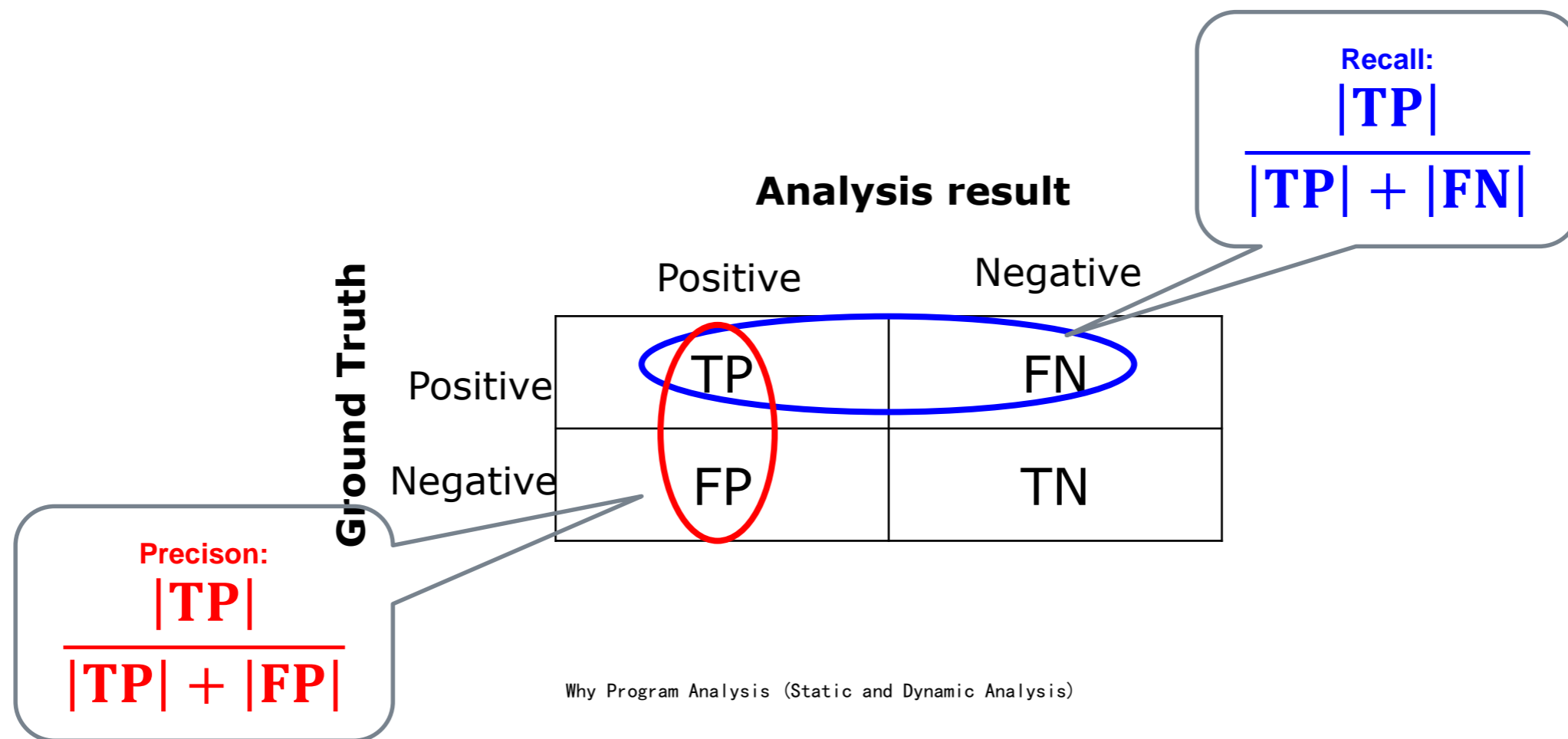
## □ FP/FN/TP/TN

		Analysis result	
		Positive	Negative
Ground Truth	Positive	TP	FN漏报
	Negative	FP误报	TN



# Precision vs. Recall

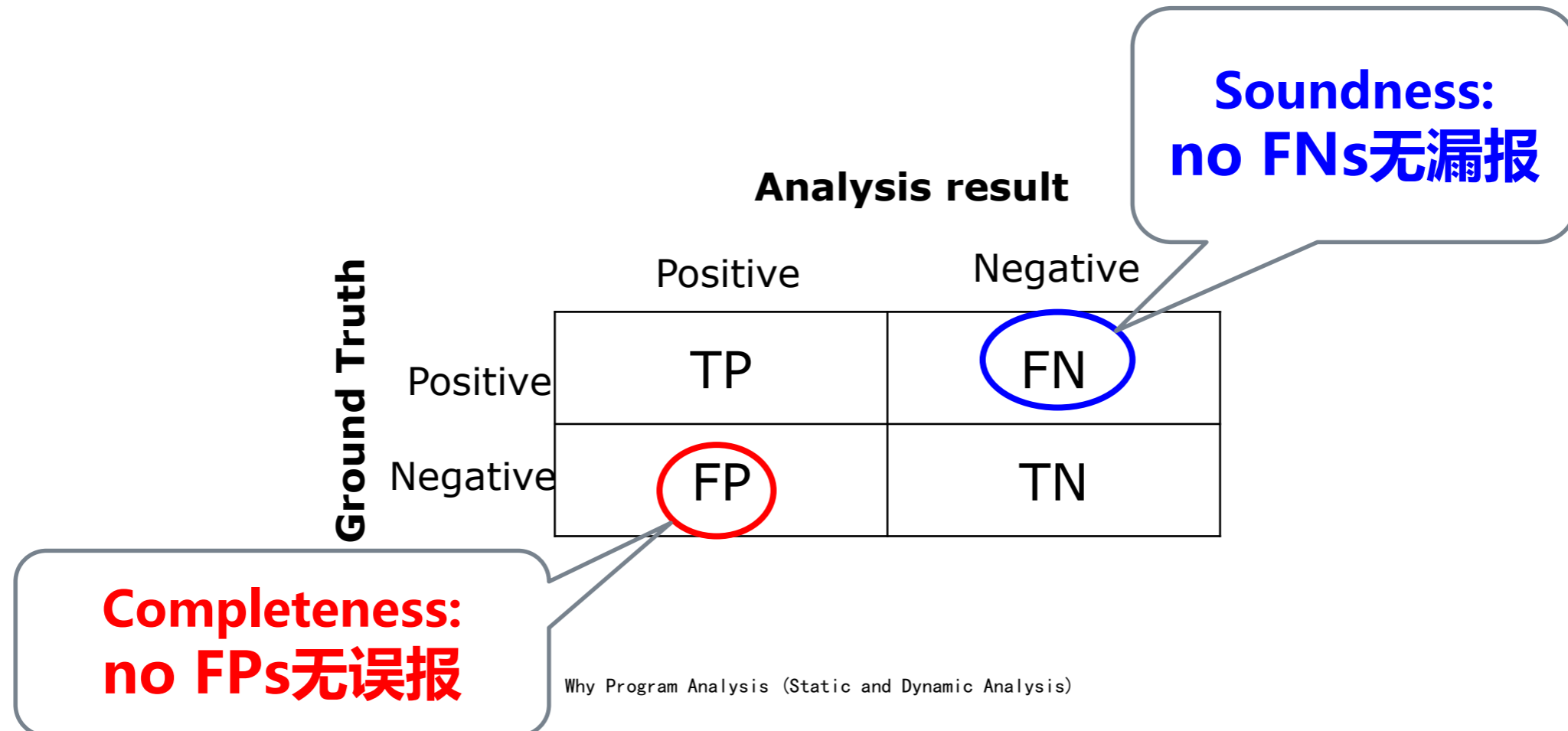
## □ FP/FN/TP/TN



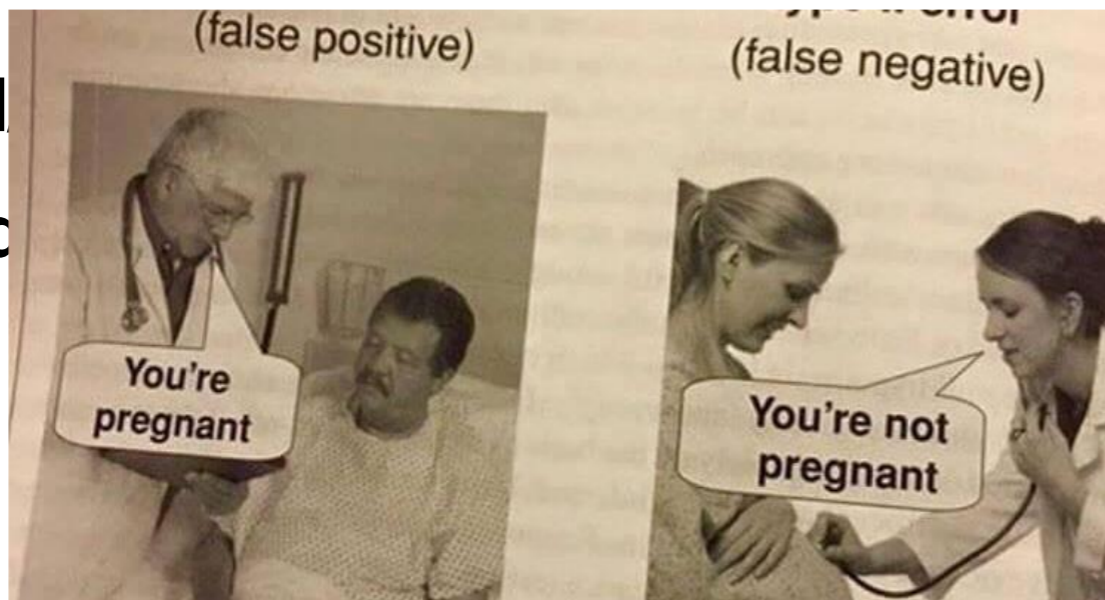


# Soundness vs. Completeness

- FP/FN/TP/TN
- Soundness vs. Completeness



- FP/FN
- Soundness



Analysis result

		Analysis result	
		Positive	Negative
Ground Truth	Positive	TP	FN
	Negative	FP	TN

**Soundness:  
no FNs 无漏报**

**Completeness:  
no FPs 无误报**



## □ Soundness (no FNs无漏报) vs. Completeness (no FPs无误报)

**Concrete domain**

0, 1, 2, 3, 4, ...

**Abstract domain**

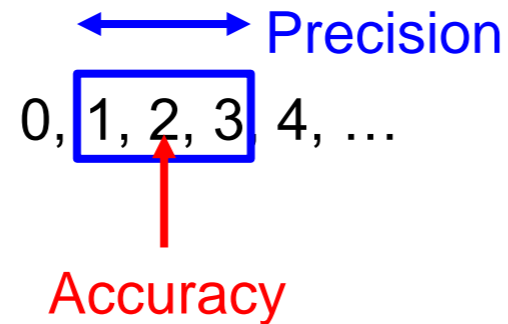
even, odd, ...



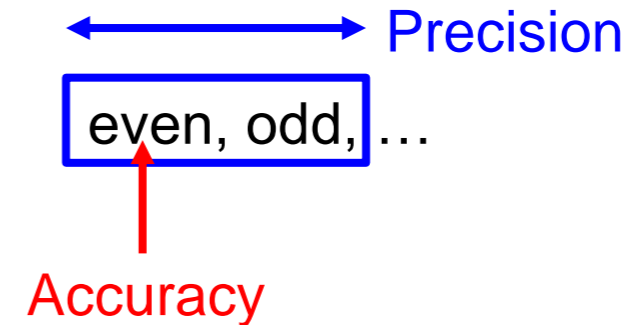
# Accuracy vs. Precision

- Soundness (no FNs无漏报) vs. Completeness (no FPs无误报)
- Accuracy = **correct** estimate vs.  
Precision = **small** estimate

Concrete domain



Abstract domain





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# Static vs. Dynamic Analysis





# Static vs. Dynamic Analysis

## □ Static Analysis

- Reason about the program without executing it.
- Build an abstraction of run-time states.
- Reason over abstract domain.
- Prove a property of the program.
- Sound\* but conservative.

\* Some static analyses are unsound; dynamic analyses can be sound.



# Selecting an Abstract Domain

$\langle x = 2; y = 5 \rangle$   
 $y = x++;$   
 $\langle x = 3; y = 2 \rangle$

$\langle x = \{ 3, 5, 7 \}; y = \{ 9, 11, 13 \} \rangle$   
 $y = x++;$   
 $\langle x = \{ 4, 6, 8 \}; y = \{ 3, 5, 7 \} \rangle$

$\langle x \text{ is odd}; y \text{ is odd} \rangle$   
 $y = x++;$   
 $\langle x \text{ is even}; y \text{ is odd} \rangle$

$\langle x=3, y=11 \rangle, \langle x=5, y=9 \rangle, \langle x=7, y=13 \rangle$   
 $y = x++;$   
 $\langle x=4, y=3 \rangle, \langle x=6, y=5 \rangle, \langle x=8, y=7 \rangle$

$\langle x \text{ is prime}; y \text{ is prime} \rangle$   
 $y = x++;$   
 $\langle x \text{ is anything}; y \text{ is prime} \rangle$

$\langle x_n = f(a_{n-1}, \dots, z_{n-1}); y_n = f(a_{n-1}, \dots, z_{n-1}) \rangle$   
 $y = x++;$   
 $\langle x_{n+1} = x_n + 1; y_{n+1} = x_n \rangle$



## □ Static Analysis

- Reason about the program without executing it.
- Build an abstraction of run-time states.
- Reason over abstract domain.
- Prove a property of the program.
- Sound\* but conservative.

## □ Dynamic Analysis

- Reason about the program based on some program executions.
- Observe concrete behavior at run time.
- Improve confidence in correctness.
- Unsound\* but precise.

\* Some static analyses are unsound; dynamic analyses can be sound.



## □ Type checking (also compiler optimizations)

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0.0;  
    while (i < n) {  
        sum = sum + nums[i];  
        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

```
double avg(double[] nums) {  
    int n = nums.length;  
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        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```



## □ Rule/pattern-based analysis (PMD, Findbugs, etc.)

```
double avg(double[] nums) {  
    int n = nums.length;  
    double sum = 0;  
  
    int i = 0;  
    while (i < n)  
        sum = sum + nums[i];  
        i = i + 1;  
  
    double avg = sum / n;  
  
    return avg;  
}
```

```
double avg(double[] nums) {  
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        sum = sum + nums[i];  
        i = i + 1;  
    }  
    double avg = sum / n;  
  
    return avg;  
}
```

<https://github.com/pmd/pmd> An extensible multilanguage static code analyzer.

<https://github.com/findbugsproject/findbugs> Find Bugs in Java Programs



## □ Software testing (also monitoring and profiling)

```
double avg(double[] nums) {
    int n = nums.length;
    double sum = 0;

    int i = 0;
    while (i < n)
        sum = sum + nums[i];
        i = i + 1;

    double avg = sum / n;

    return avg;
}
```

## A test for the avg function:

```
@Test
public void testAvg() {
    double nums =
        new double[] {1.0, 2.0, 3.0};
    double actual = Math.avg(nums);
    double expected = 2.0;
    assertEquals(expected, actual, EPS);
}
```



# Static vs. Dynamic Analysis

**What are the key challenges?**



## What are the key challenges?

- **Static analysis: choose good abstractions**
  - Chosen abstraction determines cost (time and space)
  - Chosen abstraction determines precision (what information is lost)
- **Dynamic analysis: choose good representatives (tests)**
  - Chosen tests determine cost (time and space)
  - Chosen tests determine accuracy (what executions are never seen)





## Summary

### Static analysis

- Abstract domain
- Conservative due to abstraction
- Sound due to conservatism
- Slow if precise

### Dynamic analysis

- Concrete domain
- Precise no approximation
- Unsound, does not generalize
- Slow if exhaustive



# Google: Why developers don't use static analysis?

- **Not integrated** into the developer's workflow.
- Reported **issues** are **not actionable**.
- Developers **do not trust the results** (FPs).
- Fixing an issue **is too expensive** or risky.
- Developers **do not understand** the reported **issues**.
- **Issues** theoretically possible but **don't manifest in practice**.

*“Produce **less than 10% effective false positives**. Developers should feel the check is pointing out an actual issue at least 90% of the time.”*

[[ICSE 2013](#)] Google: Why developers don't use static analysis?

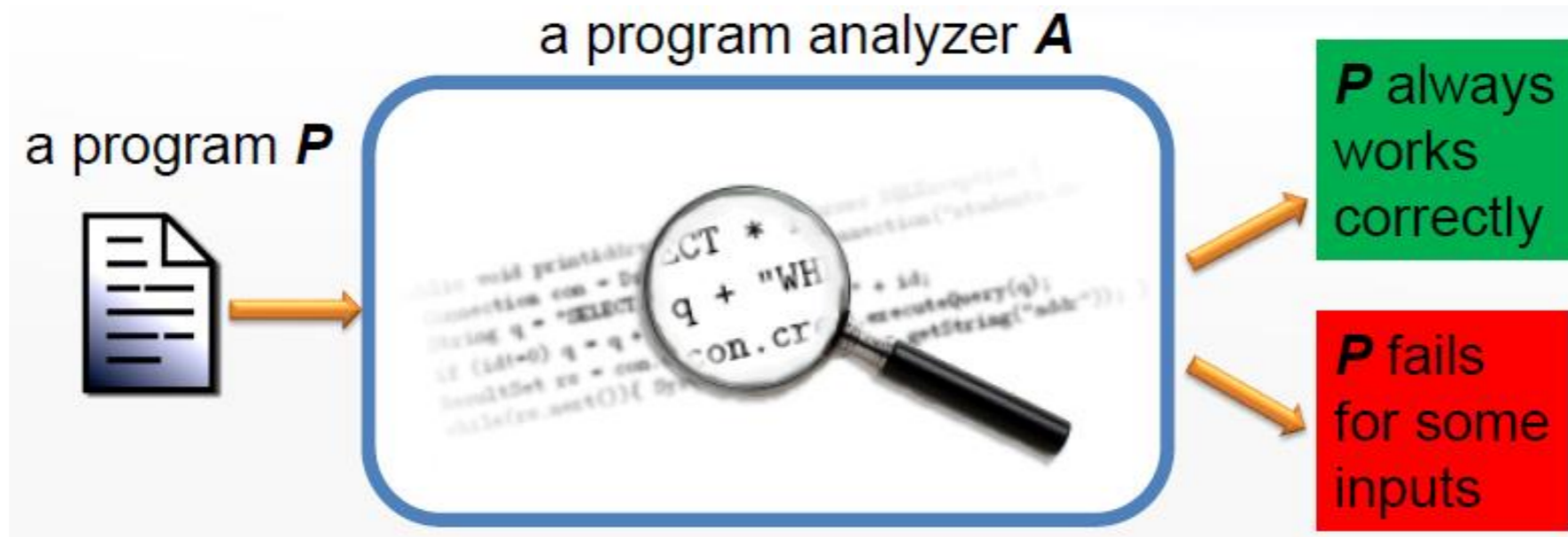


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# Program Analyzer

# Programs that reason about programs

- Soundness(可靠性): don't miss any errors
- Completeness(完备性): don't raise false alarms
- Termination(终止性): always give an answer





# Why are the Answers Interesting?

## Increase efficiency

- Resource usage
- Optimization

## Ensure correctness

- Verify behavior
- Catch bugs early



## Support program understanding

## Enable refactorings



# Rice's theorem, 1953

□ H.G. Rice: *Classes of recursively enumerable sets and their decision problem*

□ Rice定理: Any nontrivial property of the behavior of programs in a Turing-complete language is undecidable!



**递归可枚举语言的所有非平凡(nontrivial)性质都是不可判定的**

**平凡性质:** 要么对全体程序都为真, 要么对全体程序都为假

**非平凡性质:** 所有不平凡的性质



# Approximation

- **Approximate answers may be decidable!**
  - Output yes/no => output yes/no/unknown
- **The approximation must be *conservative***
- **More subtle approximations if not only yes/no**
  - E.g. memory usage, pointer targets

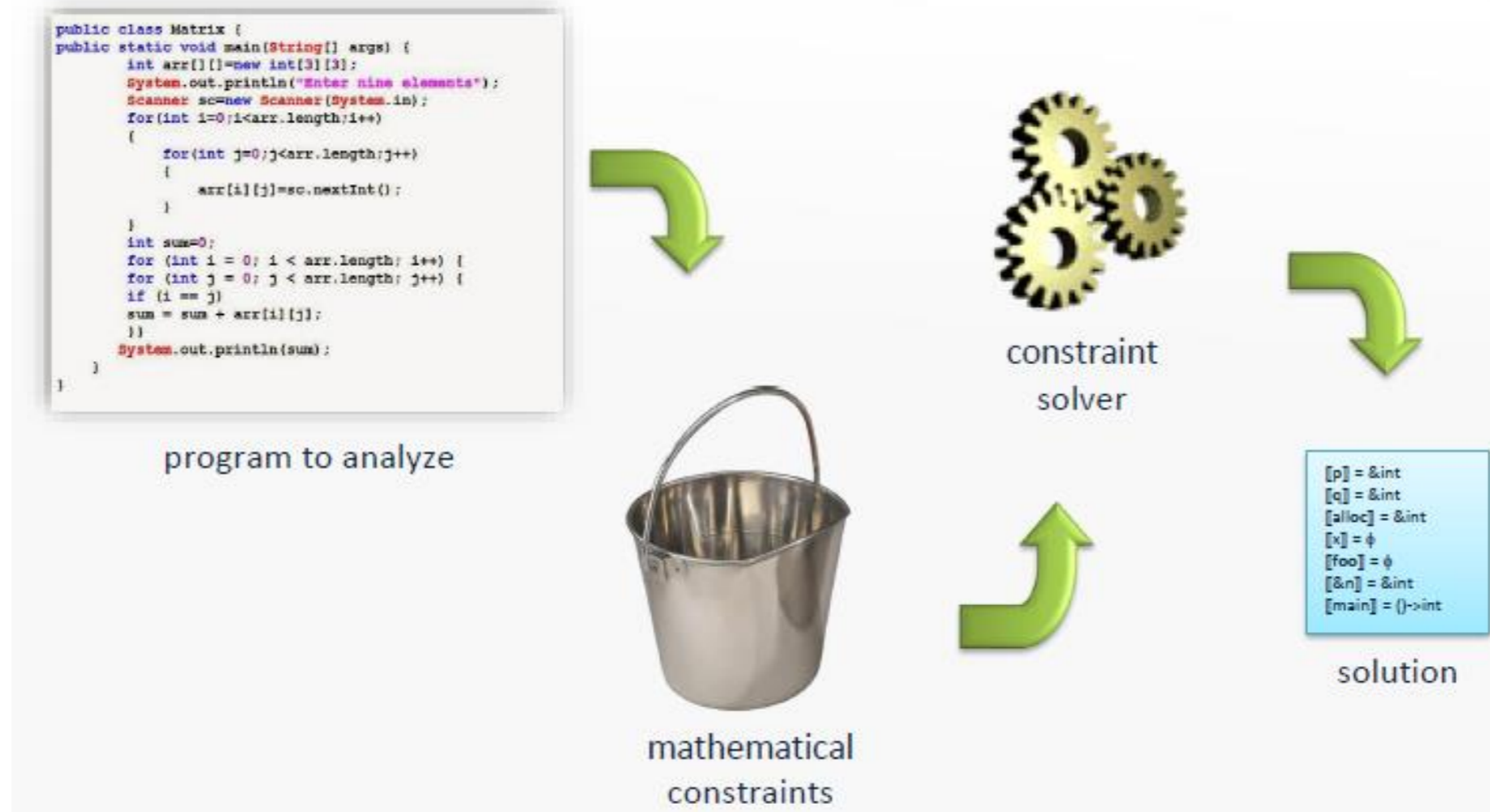


# The Engineering Challenge

- A correct but trivial approximation algorithm may just give the useless answer every time
- The engineering challenge is to give the useful answer often enough to fuel the client application
- ... and to do so within reasonable time and space
- Hard (but fun) part of static analysis



- Conceptually separates the **analysis specification** from **algorithmic aspects** and **implementation details**





# Challenging Features in Modern PLs

- Higher-order functions
- Mutable records or objects, arrays
- Integer or floating-point computations
- Dynamic dispatching
- Inheritance
- Exceptions
- Reflection
- ...



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Thanks