

Interprocedural Analysis

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Most content comes from <http://cs.au.dk/~amoeller/spa/>

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Interprocedural Analysis

- Analyzing the body of a single function
 - *intra*procedural analysis
- Analyzing the whole program with function calls
 - *inter*procedural analysis
- For now, we consider TIP without function pointers and indirect calls
- A naive approach:
 - analyze each function in isolation
 - be maximally pessimistic about results of function calls
 - rarely sufficient precision...

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CFG for Whole Programs

The idea:

- Construct a CFG for each function
- Then glue them together to reflect function calls and returns

We need to take care of:

- parameter passing
- return values
- values of local variables across calls (including recursive functions, so not enough to assume unique variable names)

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A Simplifying Assumption

- Assume that all function calls are of the form

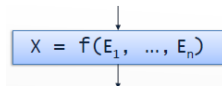
$$X = f(E_1, \dots, E_n);$$

- This can always be obtained by normalization

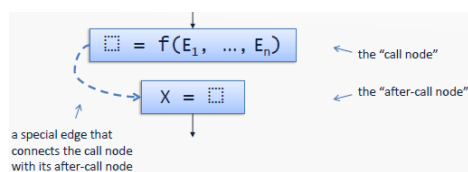
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Interprocedural CFGs (1/3)

Split each original call node



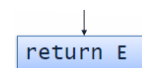
into two nodes:



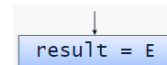
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Interprocedural CFGs (2/3)

Change each return node



into an assignment:

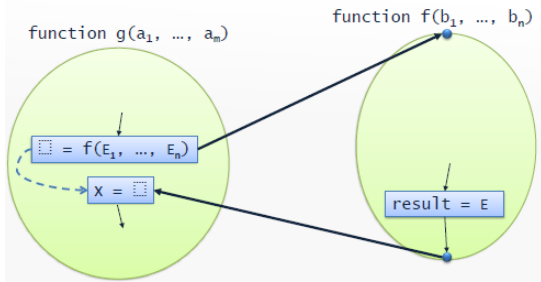


(where result is a fresh variable)

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Interprocedural CFGs (3/3)

Add call edges and return edges:

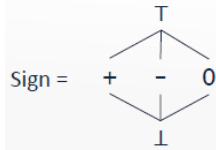


Constraints

- For call/entry nodes:
 - be careful to model evaluation of *all* the actual parameters before binding them to the formal parameter names (otherwise, it may fail for recursive functions)
- For after-call/exit nodes:
 - like an assignment: $X = \text{result}$
 - but also restore local variables from before the call using the call \rightarrow after-call edge
- The details depend on the specific analysis...

Example: Interprocedural Sign Analysis

- Recall the intraprocedural sign analysis...
- Lattice for abstract values:



- Lattice for abstract states:
 $\text{Vars} \rightarrow \text{Sign}$

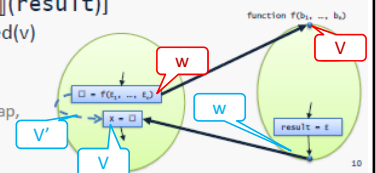
Example: Interprocedural Sign Analysis

- Constraint for entry node v of function $f(b_1, \dots, b_n)$:

$$\llbracket v \rrbracket = \sqcup_{w \in \text{pred}(v)} \llbracket [b_1 \rightarrow \text{eval}(\llbracket w \rrbracket, E_1^w), \dots, b_n \rightarrow \text{eval}(\llbracket w \rrbracket, E_n^w)] \rrbracket$$
 where E_i^w is i 'th argument at w
- Constraint for after-call node v labeled $X = \square$, with call node v' :

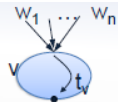
$$\llbracket v \rrbracket = \llbracket v' \rrbracket [X \rightarrow \llbracket w \rrbracket(\text{result})]$$
 where $w \in \text{pred}(v)$

(Recall: no global variables, no heap, and no higher-order functions)



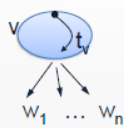
Alternative Formulations

1) $\llbracket v \rrbracket = t_v(\sqcup_{w \in \text{pred}(v)} \llbracket w \rrbracket)$



2) $\forall w \in \text{succ}(v): t_v(\llbracket v \rrbracket) \sqsubseteq \llbracket w \rrbracket$

- recall "solving inequations"
- may require fewer join operations if there are many CFG edges
- more suitable for *interprocedural* flow



The Worklist Algorithm (original version)

```

x1 = ⊥; ... xn = ⊥
W = {v1, ..., vn}
while (W ≠ ∅) {
  vi = W.removeNext()
  y = fi(x1, ..., xn)
  if (y ≠ xi) {
    for (vj ∈ dep(vi)) {
      W.add(vj)
    }
    xi = y
  }
}
    
```

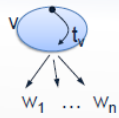
如果CFG结点vi的语义值发生变化, 则将计算vi语义值所依赖的结点vj加入到worklist

The Worklist Algorithm (alternative version)

```

 $x_1 = \perp; \dots x_n = \perp$ 
 $W = \{v_1, \dots, v_n\}$ 
while ( $W \neq \emptyset$ ) {
   $v_i = W.removeNext()$ 
   $y = \tau_i(x_i)$ 
  for ( $v_j \in dep(v_i)$ ) {
    propagate( $y, v_j$ ) {
       $z = x_j \sqcup y$ 
      if ( $z \neq x_j$ ) {
         $x_j = z$ 
         $W.add(v_j)$ 
      }
    }
  }
}

```



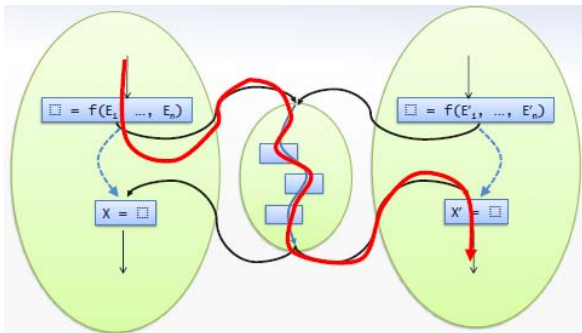
Implementation: WorklistFixpointPropagationSolver

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- Interprocedural analysis
- Context-sensitive interprocedural analysis

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Interprocedurally Invalid Paths



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Example

What is the sign of the return value of g ?

```

f(z) {
  return z*42;
}

g() {
  var x,y;
  x = f(0);
  y = f(87);
  return x + y;
}

```

Our current analysis says "T"

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Function Cloning (alternatively, function inlining)

- Clone functions such that each function has only one callee
- Can avoid interprocedurally invalid paths ☺
- For high nesting depths, gives exponential blow-up ☹
- Doesn't work on (mutually) recursive functions ☹
- Use heuristics to determine when to apply (trade-off between CFG size and precision)

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Example, with cloning

- What is the sign of the return value of g ?

```

f1(z1) {
  return z1*42;
}

f2(z2) {
  return z2*42;
}

g() {
  var x,y;
  x = f1(0);
  y = f2(87);
  return x + y;
}

```

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Context Sensitive Analysis

- Function cloning provides a kind of context sensitivity (also called poly-variant analysis)
- Instead of physically copying the function CFGs, do it *logically*
- Replace the lattice for abstract states, States, by **Contexts** \rightarrow $\text{lift}(\text{States})$ where Contexts is a set of **call contexts**
 - the contexts are abstractions of the state at function entry
 - Contexts must be finite to ensure finite height of the lattice
 - the bottom element of $\text{lift}(\text{States})$ represents "unreachable" contexts
- Different strategies for choosing the set Contexts...

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One-level Cloning

- Let c_1, \dots, c_n be the call nodes in the program
- Define $\text{Contexts} = \{c_1, \dots, c_n\} \cup \{\epsilon\}$
 - each call node now defines its own "call context" (using ϵ to represent the call context at the main function)
 - the context is then like the return address of the top-most stack frame in the call stack
- Same effect as one-level cloning, but without actually copying the function CFGs
- Usually straightforward to generalize the constraints for a context insensitive analysis to this lattice
- (Example: context-sensitive sign analysis –later...)

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The Call String Approach

- Let c_1, \dots, c_n be the call nodes in the program
- Define Contexts as the set of strings over $\{c_1, \dots, c_n\}$ of length $\leq k$
 - such a string represents the top-most k call locations on the call stack
 - the empty string ϵ again represents the call context at the main function
- For $k=1$ this amounts to one-level cloning

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Example:

interprocedural sign analysis with call strings ($k=1$)

Lattice for abstract states: $\text{Contexts} \rightarrow \text{lift}(\text{Vars} \rightarrow \text{Sign})$
 where $\text{Contexts} = \{\epsilon, c_1, c_2\}$

```

f(z) {
  var t1, t2;
  t1 = z*6;
  t2 = t1*7;
  return t2;
}
...
x = f(0); // c1
y = f(87); // c2
...
    
```

$\{\epsilon \mapsto \text{unreachable},$
 $c_1 \mapsto \perp[z \mapsto 0, t_1 \mapsto 0, t_2 \mapsto 0],$
 $c_2 \mapsto \perp[z \mapsto +, t_1 \mapsto +, t_2 \mapsto +]\}$

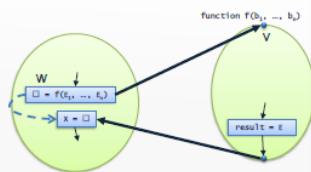
What is an example program that requires $k=2$ to avoid loss of precision?

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Context Sensitivity with Call Strings function entry nodes, for $k=1$

Constraint for entry node v of function $f(b_1, \dots, b_n)$:
 (if not 'main')

$$\llbracket v \rrbracket(c) = \bigsqcup_{\substack{w \in \text{pred}(v) \wedge \\ c = w \wedge \\ c' \in \text{Contexts}}} s_w^c$$



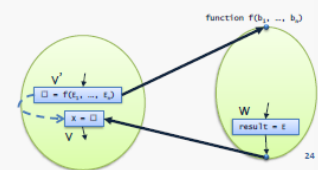
$$s_w^c = \begin{cases} \text{unreachable} & \text{if } \llbracket w \rrbracket(c') = \text{unreachable} \\ \perp[b_1 \rightarrow \text{eval}(\llbracket w \rrbracket(c'), E_1^w), \dots, b_n \rightarrow \text{eval}(\llbracket w \rrbracket(c'), E_n^w)] & \text{otherwise} \end{cases}$$

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Context Sensitivity with Call Strings after-call nodes, for $k=1$

Constraint for after-call node v labeled $X = \square$,
 with call node v' and exit node $w \in \text{pred}(v)$:

$$\llbracket v \rrbracket(c) = \begin{cases} \text{unreachable} & \text{if } \llbracket v' \rrbracket(c) = \text{unreachable} \vee \llbracket w \rrbracket(v') = \text{unreachable} \\ \llbracket v' \rrbracket(c)[X \rightarrow \llbracket w \rrbracket(v')(\text{result})] & \text{otherwise} \end{cases}$$



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The Functional Approach

- The call string approach considers *control flow*
 - but why distinguish between two different call sites if their abstract states are the same?
- The functional approach instead considers *data*
- In the most general form, choose **Contexts = States** (requires States to be finite)
- Each element of the lattice **States \rightarrow lift(States)** is now a map m that provides an element $m(x)$ from States (or "unreachable") for each possible x where x describes the state at function entry

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Example:

interprocedural sign analysis with the functional approach

Lattice for abstract states: Contexts \rightarrow lift(Vars \rightarrow Sign)
 where Contexts = Vars \rightarrow Sign

```
f(z) {
  var t1, t2;
  t1 = z^6;
  t2 = t1*7;
  return t2;
}
...
x = f(0);
y = f(87);
...
```

$\perp[z \mapsto 0] \mapsto \perp[z \mapsto 0, t1 \mapsto 0, t2 \mapsto 0]$,
 $\perp[z \mapsto +] \mapsto \perp[z \mapsto +, t1 \mapsto +, t2 \mapsto +]$,
 all other contexts \mapsto unreachable

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The Functional Approach

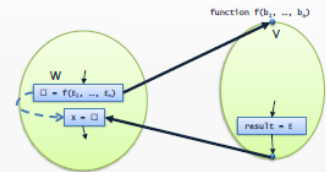
- The lattice element for a function exit node is thus a **function summary** that maps abstract function input to abstract function output
- This can be exploited at call nodes!
- When entering a function with abstract state x :
 - consider the function summary s for that function
 - if $s(x)$ already has been computed, use that to model the entire function body, then proceed directly to the after-call node
- Avoids the problem with interprocedurally invalid paths!
- ...but may be expensive if States is large

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Context sensitivity with the functional approach function entry nodes

Constraint for entry node v of function $f(b_1, \dots, b_n)$:
 (if not 'main')

$$\llbracket v \rrbracket(c) = \bigsqcup_{\substack{w \in \text{pred}(v) \wedge \\ c = s_w^c \wedge \\ c' \in \text{Contexts}}} s_w^c$$



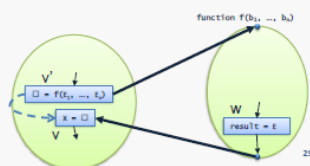
where s_w^c is defined as before

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Context sensitivity with the functional approach after-call nodes

Constraint for after-call node v labeled $X = \square$,
 with call node v' and exit node $w \in \text{pred}(v)$:

$$\llbracket v \rrbracket(c) = \begin{cases} \text{unreachable} & \text{if } \llbracket v' \rrbracket(c) = \text{unreachable} \vee \llbracket w \rrbracket(s_{v'}^c) = \text{unreachable} \\ \llbracket v' \rrbracket(c)[X \mapsto \llbracket w \rrbracket(s_{v'}^c)(\text{result})] & \text{otherwise} \end{cases}$$



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