# One-pot synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanostructures with rationally tunable morphologies

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## ABSTRACT

Shape control has proven to be a powerful and versatile means of tailoring the properties of Bi<sub>2</sub>Se<sub>3</sub> nanostructures for a wide variety of applications. Here, three different Bi<sub>2</sub>Se<sub>3</sub> nanostructures, i.e., spiral-type nanoplates, smooth nanoplates, and dendritic nanostructures, were prepared by manipulating the supersaturation level in the synthetic system. This mechanism study indicated that, at low supersaturation, defects in the crystal growth could cause a step edge upon which Bi<sub>2</sub>Se<sub>3</sub> particles were added continuously, leading to the formation of spiral-type nanoplates. At intermediate supersaturation, the aggregation of amorphous Bi<sub>2</sub>Se<sub>3</sub> particles and subsequent recrystallization resulted in the formation of smooth nanoplates. Furthermore, at high supersaturation, polycrystalline Bi<sub>2</sub>Se<sub>3</sub> cores formed initially, on which anisotropic growth of Bi<sub>2</sub>Se<sub>3</sub> occurred. This work not only advances our understanding of the growth mechanism but also offers a new approach to control the morphology of Bi<sub>2</sub>Se<sub>3</sub> nanostructures.

# 1 Introduction

Over the past decades,  $Bi_2Se_3$  has attracted considerable attention owing to its unique structure and promising applications [1–7]. In  $Bi_2Se_3$ , five covalently bonded atomic sheets (Se-Bi-Se-Bi-Se) along the *c*-axis compose one quintuple layer (QL, ~1 nm), and these QLs are linked together by van der Waals interactions [8]. As a topological insulator with an insulating bulk phase and an exotic metal surface,  $Bi_2Se_3$  has a remarkable band gap up to 0.3 eV and a single Dirac cone at the  $\Gamma$  points [9, 10]. The unique surface structure leads to the attractive electronic and optical properties of  $Bi_2Se_3$  [11, 12] and thus opens up many important applications including photodetection [13], ultrafast lasers [14], cancer treatment [15], and thermoelectric materials [16–18]. Since these applications are highly sensitive to the size, shape, and structure of

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nanomaterials [19–24], morphological modulation can be introduced as an effective tool to tailor the properties and optimize the performance towards a specific application for Bi<sub>2</sub>Se<sub>3</sub> nanostructures.

For these reasons, much effort has been devoted to the preparation of Bi<sub>2</sub>Se<sub>3</sub> nanostructures with well-defined morphologies. To date, diverse chemical methods have been adopted to prepare Bi<sub>2</sub>Se<sub>3</sub> nanostructures, such as solvothermal synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanoplates and nanoflowers [25, 26], photochemical synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanospheres and nanorods [27], and polyol synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanosheets and architectural nanostructures [28–31]. Recently, our group achieved screw-dislocation-driven bidirectional growth of spiraltype Bi<sub>2</sub>Se<sub>3</sub> nanoplates with a bipyramid-like shape [32]. Despite the success of preparing Bi<sub>2</sub>Se<sub>3</sub> nanostructures with a fixed shape, a universal system that is of highly amenability to preparing Bi<sub>2</sub>Se<sub>3</sub> nanostructures with rationally tunable morphologies has not yet been lucubrated. In addition, a fundamentally significant process during the synthesis, i.e., the growth mechanism, has not been elucidated.

Herein, we demonstrate a polyol synthesis to obtain a set of well-defined Bi<sub>2</sub>Se<sub>3</sub> nanostructures. Through fine control of the supersaturation level in the synthetic system, three different types of Bi<sub>2</sub>Se<sub>3</sub> nanostructures, i.e., spiral-type nanoplates, smooth nanoplates, and dendritic nanostructures, were successfully prepared. The mechanism study indicated that, at low supersaturation, defects in the crystal growth could cause a step edge, upon which Bi<sub>2</sub>Se<sub>3</sub> particles were added continuously, leading to the formation of spiral-type nanoplates. At intermediate supersaturation, the aggregation of amorphous Bi2Se3 particles and subsequent recrystallization resulted in the formation of smooth nanoplates. Furthermore, at high supersaturation, polycrystalline Bi<sub>2</sub>Se<sub>3</sub> cores were formed initially, on which anisotropic growth of Bi<sub>2</sub>Se<sub>3</sub> occurred subsequently. As a result, dendritic nanostructures were obtained in the final products. We believe that the method in this work can be utilized as a guideline to obtain other nanomaterials with rationally tunable morphologies and optimized performance for a given application.

#### 2 **Experimental**

#### 2.1 Chemicals and materials

Sodium selenite (Na<sub>2</sub>SeO<sub>3</sub>, 99%), bismuth nitrate pentahydrate (Bi(NO<sub>3</sub>)<sub>3</sub>·5H<sub>2</sub>O, 99%), L-ascorbic acid (AA), poly(vinylpyrrolidone) (PVP,  $M_W \approx 40,000$ ), ethylene glycol (EG, 99%), sodium hydroxide (NaOH), and hydrochloric acid (HCl, 38% in H<sub>2</sub>O) were purchased from Sinopharm Chemical Reagent Co. Ltd., Shanghai, China. All chemicals were used as received without further purification. Deionized water with a resistivity of 18.2 MΩ·cm was used for the preparation of NaOH aqueous solution.

# 2.2 Synthesis of three Bi<sub>2</sub>Se<sub>3</sub> nanostructures with different morphologies

Stoichiometric amounts of Bi(NO<sub>3</sub>)<sub>3</sub>·5H<sub>2</sub>O (9 mg) and Na<sub>2</sub>SeO<sub>3</sub> (4.8 mg) were dissolved separately in 0.45 mL of EG and then injected rapidly into another EG solution (14.1 mL) containing PVP (143 mg), AA (87 mg), and HCl (11.8 M)/NaOH aqueous solution (1 M) at 175 °C under a N<sub>2</sub> atmosphere. Specifically, when adding 100  $\mu$ L of HCl, 20  $\mu$ L of HCl, or 20  $\mu$ L of aqueous NaOH into the mixture, spiral-type nanoplates, smooth nanoplates, or dendritic nanostructures were obtained, respectively. After the reaction finished, the products were precipitated at a rotation speed of 8,000 rpm for 5 min and washed three times by ethanol.

#### 2.3 Instrumentation

Transmission electron microscopy (TEM) images were taken using a Hitachi H-7650 microscope at an acceleration voltage of 100 kV. High-resolution TEM (HRTEM), high-angle annular dark-field scanning TEM (HAADF-STEM), and X-ray energy dispersive spectrometry (EDS) analysis were performed on a JEOL ARM-200F field-emission TEM operating at 200 kV. Atomic force microscopy (AFM) study was performed with a Veeco DI Nano-scope MultiMode V system. X-ray diffraction (XRD) characterization was performed using a Philips X'Pert Pro X-ray diffractometer with a monochromatized Cu K $\alpha$  radiation source at a wavelength of 0.1542 nm. The extinction spectra were attained using a U-4100 UV-visible (UV-vis) spectrophotometer (Hitachi, Japan).

#### 3 Results and discussion

# 3.1 Structural and compositional analysis of Bi<sub>2</sub>Se<sub>3</sub> nanostructures with controllable morphologies

In a typical synthesis,  $Bi(NO_3)_3 \cdot 5H_2O$  (9 mg) and  $Na_2SeO_3$  (4.8 mg) were dissolved separately in 0.45 mL of EG and then rapidly injected into another EG solution (14.1 mL) containing PVP (143 mg), AA (87 mg), and HCl (11.8 M) held at 175 °C under N<sub>2</sub>. As the reaction proceeded, the solution changed color to dark grey, indicating the formation of  $Bi_2Se_3$  nanocrystals. A typical TEM image shows that the  $Bi_2Se_3$  nanocrystals obtained using 100 µL of HCl were hexagonal and plate-like, with a typical lateral size of 1–2 µm (Fig. 1(a)). An individual nanoplate was further characterized by high-magnification TEM analysis (Fig. 1(b)), through which two sets of densely distributed centrosymmetric helical fringes on the surface could be clearly seen. Figure 1(c) presents HAADF-STEM

image of a typical spiral-type nanoplate and corresponding elemental mapping by means of EDS. Both Bi (green) and Se (red) were distributed uniformly (Figs. 1(c) and 1(d)). A radical drop in the EDS linescanning profile indicated a hollow core near the center area of the spiral-type nanoplate (Fig. 1(d)), which was in agreement with our previous work [32]. To better visualize the structure of spiral-type nanoplates, AFM analyses are presented in Fig. 2. The AFM amplitude image in Fig. 2(b) clearly shows a hexagonal nanoplate with helical fringes on the surface. The height profile (Fig. 2(c)) along the black line in Fig. 2(a) indicates that the thickness increased gradually from the edge to the center, which was also confirmed by three-dimensional AFM images (Figs. 2(d) and 2(e)). Bi<sub>2</sub>Se<sub>3</sub> nanostructures with different morphologies were obtained by adjusting the pH value of the solution. Smooth nanoplates took the place of spiral-type nanoplates when 100 µL of HCl was switched to 20 µL of HCl with the other conditions unchanged. As shown in Fig. 1(e), the resultant  $Bi_2Se_3$ nanocrystals were hexagonal as well, with an average lateral size of ~3.5 µm. A high-magnification TEM



Figure 1 (a), (e), and (i) Low-magnification TEM images of spiral-type  $Bi_2Se_3$  nanoplates, smooth  $Bi_2Se_3$  nanoplates, and dendritic  $Bi_2Se_3$  nanostructures, respectively. (b), (f), and (j) High-magnification TEM images from an individual nanostructure. (c), (g), and (k) HAADF-STEM images and corresponding elemental maps showing the distribution of Bi (green) and Se (red). (d), (h), and (l) Line-scanning EDS profiles for different elements.

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**Figure 2** (a) AFM image of an individual spiral-type nanoplate. (b) AFM amplitude image of the nanoplate in (a). (c) AFM height profile along the black line in (a). (d) and (e) Three-dimensional AFM images from the side and top views, respectively.

image indicated that the nanoplate was smooth on the surface, containing no helical fringes, unlike the spiral-type one. Homogeneous distributions of Bi and Se in the smooth nanoplate were revealed by EDS mapping and line-scanning analysis (Figs. 1(g) and 1(h)). No drastic drops were found in the EDS line-scanning profile, supporting the formation of smooth nanoplates with relatively uniform thickness. Dendritic nanostructures were obtained when adding 20 µL of NaOH solution (1 M) instead of HCl with the other conditions unchanged (Fig. 1(i)). A highmagnification TEM image indicated that the dendritic nanostructure was composed of several irregular branches protruding from the center with thin surrounding peripheries (Fig. 1(j)). Similar to the spiral-type and smooth nanoplates mentioned above, the dendritic nanostructure had uniform distributions of Bi and Se as well (Figs. 1(k) and 1(l)). Sharply fluctuating curves in the EDS line-scanning profile revealed the uneven thickness of the dendritic nanostructure (Fig. 1(l)). EDS spectra showed that Bi and Se had an atomic ratio close to 2:3 in all three nanostructures (Fig. S1 in the Electronic Supplementary Material (ESM)).

To determine the crystalline structure of the three Bi<sub>2</sub>Se<sub>3</sub> nanostructures, the XRD data provided in Fig. 3 indicated a rhombohedral crystalline structure for all samples (JCPDS No. 89-2008; *a* = 4.139 Å, *c* = 28.636 Å). However, for the spiral-type and smooth nanoplates, the diffraction peaks in (006) and (0, 0, 15) were both much stronger than the standard ones, which can be attributed to the enhancement in the diffraction in the vertical direction (z-axis). A high-quality single crystal for spiral-type and smooth nanoplates was revealed by selected area electron diffraction (SAED) patterns (insets in Figs. S2(a) and S2(c) in the ESM). In Figs. S2(b) and S2(d) (see ESM), HRTEM images of spiral-type and smooth nanoplates show lattice fringes with a lattice spacing of 0.21 nm, corresponding to the  $(11\overline{2}0)$  planes. The polycrystalline characteristic of



Figure 3 XRD patterns of spiral-type  $Bi_2Se_3$  nanoplates, smooth  $Bi_2Se_3$  nanoplates, and dendritic  $Bi_2Se_3$  nanostructures. The dark columns at the bottom refer to standard JCPDS data for  $Bi_2Se_3$ .

the dendritic nanostructures was confirmed by the SAED pattern in the inset of Fig. 4(a). HRTEM images of the regions indicated by boxes in Fig. 4(a) are shown in Figs. 4(b)–4(d), indicating different lattice orientations in these regions.

## 3.2 Shape evolution of three different Bi<sub>2</sub>Se<sub>3</sub> nanostructures

To determine the growth process of the three different Bi<sub>2</sub>Se<sub>3</sub> nanostructures, a series of TEM images were taken of samples obtained at different time points, as shown in Fig. 5. The formation process of spiral-type  $Bi_2Se_3$  nanoplates is presented in Figs. 5(a)–5(d). After the rapid injection of both precursors into the reaction medium at 175 °C, the color of the solution gradually turned from faint yellow to light red. A Se sphere was observed in the initial stage ( $t = 6 \min$ , Fig. 5(a)), and  $Bi_2Se_3$  emerged later (t = 10 min, Fig. 5(b)). An incipient nanoplate appeared with a slip plane on the surface as the reaction continued (t = 20 min, t)Fig. 5(c)). Subsequently, growth along the step edge was observed ( $t = 40 \min$ , Fig. 5(d)). With prolonged reaction, the product evolved into a well-defined spiral-type nanoplate (t = 2.5 h, Fig. 1(b)). A HAADF-STEM image of an individual nanostructure in Fig. 5(b) is presented in Fig. S3(a) (see ESM). As shown in Fig. S3(b) in the ESM, Bi<sub>2</sub>Se<sub>3</sub> extending from the Se sphere had well-organized lattice fringes with a lattice spacing of 0.36 nm, which corresponded to the  $(10\overline{11})$ 



Figure 4 (a) TEM image of an individual dendritic  $Bi_2Se_3$  nanostructure. The corresponding SAED pattern is shown in the inset. (b)–(d) HRTEM images of the three different regions marked in (a).

planes. The single-crystal nature of exposed  $Bi_2Se_3$  was revealed by the fast Fourier transform (FFT) pattern (inset of Fig. S3(b) in the ESM). The EDS elemental mapping images (Figs. S3(c)–S3(e) in the ESM) show that the content of Se was much higher than that of Bi. The HAADF image taken from the broken nanostructure caused by the irradiation of the high-energy electron beam indicated that the amorphous Se vanished, basically leaving only  $Bi_2Se_3$  (Fig. S3(f) in the ESM). A random and overlapped deposition of single-crystal  $Bi_2Se_3$  particles is observed in Fig. S3(g) in the ESM.

Since the addition of HCl can effectively lower the reducing capacity of AA [33],  $\text{SeO}_3^{2-}$  was initially reduced to a zero-valence Se sphere, which was confirmed by the change in the solution color from faint yellow to light red. The Se sphere grew larger as the reaction proceeded; meanwhile, some Se species were reduced further to form Bi<sub>2</sub>Se<sub>3</sub>. In the subsequent growth process, defects and stacking faults inevitably appeared because of the "imperfect" deposition of Bi<sub>2</sub>Se<sub>3</sub> crystallites [34, 35], leading to the formation of a slip plane on the surface. Given that there is always a step edge to which atoms can be added on this occasion, the energy barrier to create new crystal steps can be overcome [36, 37]. Thus, the Bi<sub>2</sub>Se<sub>3</sub> particles were continuously deposited along the step edge and



**Figure 5** (a)–(d) TEM images of spiral-type  $Bi_2Se_3$  nanoplates obtained at different time points: (a) 6 min, (b) 10 min, (c) 20 min, and (d) 40 min. (e)–(h) TEM images of smooth  $Bi_2Se_3$  nanoplates obtained at different time points: (e) 70 s, (f) 100 s, (g) 140 s, and (h) 4 min. (i)–(l) TEM images of dendritic  $Bi_2Se_3$  nanostructures obtained at different time points: (i) 10 s, (j) 30 s, (k) 1.5 min, and (l) 3 min.

lateral side, resulting in the formation of the final spiral-type  $Bi_2Se_3$  nanoplates.

The formation process of smooth nanoplates is schematically illustrated in Figs. 5(e)-5(h). The color of the solution turned from faint yellow to light red immediately after the rapid injection of both precursors, indicating a faster reduction rate than that of spiraltype nanoplates. At the initial stage (t = 70 s, Fig. 5(e)), Bi<sub>2</sub>Se<sub>3</sub> particles appeared in great abundance with an amorphous structure, as revealed by HRTEM and FFT analysis (Fig. S4 in the ESM). When the reaction proceeded to t = 100 s, these particles aggregated, forming a budding nanoplate (Fig. 5(f)). Afterwards, a larger nanoplate was observed with agglomerates around it (t = 140 s, Fig. 5(g)). The sample further developed into a mature Bi2Se3 nanoplate as the reaction continued ( $t = 4 \min$ , Fig. 5(h) and  $t = 15 \min$ , Fig. 1(f)). Different shapes (hexagonal and truncated triangular) coexist in Fig. 1(e), possibly owing to the formation of non-uniform budding nanoplates in the initial stage [38].

Figures 5(i)-5(l) display the growth process of dendritic  $Bi_2Se_3$  nanostructures. After the rapid

injection of both precursors, the color of the solution immediately changed from faint yellow to dark grey, indicating the fastest reaction rate among all the three synthetic processes. At the initial stage, small cores formed within t = 10 s (Fig. 5(i)), followed by random attachment of some irregular flakes (t = 30 s, Fig. 5(j)). The FFT pattern taken from the region (marked by a white box in Fig. S5(a) in the ESM) shows evidence of the polycrystalline characteristic of the core (inset in Fig. S5(b) in the ESM). Homogeneous distributions of Bi and Se were revealed by STEM-EDS mapping (Figs. S5(c)–S5(f) in the ESM). Subsequently, the sample grew larger (t = 1.5 min, Fig. 5(k)) with more branches protruding from the core ( $t = 3 \min$ , Fig. 5(1)). Further development finally resulted in the formation of a typical dendritic Bi<sub>2</sub>Se<sub>3</sub> nanostructure (t = 10 min, Fig. 1(j)).

# **3.3** Formation mechanism of Bi<sub>2</sub>Se<sub>3</sub> nanostructures with different morphologies

It is indubitable that the supersaturation of the reaction system has a pivotal impact on crystal growth [39]. According to the classical crystal growth theory [40], the supersaturation ( $\sigma$ ) of a reaction system represents the driving force for crystal growth:  $\sigma = \ln(c/c_0)$ , where *c* is the Bi<sub>2</sub>Se<sub>3</sub> concentration and  $c_0$  is the equilibrium concentration. The growth rate (*R*) in different modes of crystal growth as a function of  $\sigma$  is presented in Fig. 6, where R continuously increases as the value of  $\sigma$  rises. In this work,  $\sigma$  was highly sensitive to the amount of HCl. Specifically, a greater amount of HCl weakened the reducing capacity of AA, leading to a lower  $\sigma$ . At low supersaturation, the energy barrier to nucleate new step edges was too high to be overcome; thus, the dislocation-driven growth dominated the crystal process, giving rise to the formation of spiraltype nanoplates. Since greater supersaturation can help nucleate new edge steps, layer-by-layer (LBL) growth started to dominate the process at intermediate supersaturation. Finally, fast nucleation and growth at high supersaturation promoted the generation of a number of "active centers" in the system. The nucleus could not grow along certain crystallographic directions [41], leading to dendritic growth in this situation.

To verify the regulatory role of supersaturation in the growth of different Bi<sub>2</sub>Se<sub>3</sub> nanostructures, we varied the amount of AA with the other conditions unchanged. When a larger amount of AA was involved, the reduction was accelerated, resulting in a higher supersaturation of the system. Therefore, the modes of dislocation-driven growth, LBL growth, and dendritic growth are expected to progressively dominate the crystal growth when increasing the amount of AA. Figure S6 (see ESM) shows Bi<sub>2</sub>Se<sub>3</sub> nanostructures



Supersaturation  $\sigma \longrightarrow$ 

**Figure 6** Schematic illustration of the growth rate in different modes of crystal growth as a function of the supersaturation.

prepared using different amounts of AA based on 20 µL of HCl. As expected, when a small amount of AA (43.5 mg) was used, spiral-type nanoplates constituted the majority of the resultant products (Fig. S6(a) in the ESM). A mixture containing spiral-type and smooth nanoplates was obtained when the amount of AA was increased to 64.8 mg (Fig. S6(b) in the ESM). When a larger amount of AA was added (174 mg), smooth nanoplates of high purity were produced (Figs. S6(c)-S6(e) in the ESM). When the amount of AA was further increased to 1,392 mg, dendritic nanostructures became an integral part of the final products (Fig. S6(f) in the ESM). In addition to the morphological modulation, this method can also achieve size control within a certain range. As shown in Figs. S6(c)–S6(e) in the ESM, when more AA was added, the size of smooth nanoplates became smaller. It is known that the size largely depends on the balance between the nucleation rate and the growth rate [42]. When more AA was introduced, a faster reduction rate was achieved, leading to the formation of more nuclei in the initial stage. In the subsequent growth stage, since the total amount of precursors was constant, less Bi<sub>2</sub>Se<sub>3</sub> was deposited on each nucleus, resulting in the smaller size of the final nanoplates.

### 4 Conclusions

In summary, we demonstrated a polyol method for the shape-controlled synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanostructures through fine control of the supersaturation level. Specifically, by increasing the pH value or the amount of AA in the system, three different Bi<sub>2</sub>Se<sub>3</sub> nanostructures including spiral-type nanoplates, smooth nanoplates, and dendritic nanostructures were obtained. A mechanism study indicated that the modes of dislocation-driven growth, LBL growth, and dendritic growth progressively dominated the crystal growth as the supersaturation increased. The inspiring results strengthen our confidence to fabricate Bi<sub>2</sub>Se<sub>3</sub> and other nanostructures with rationally tunable morphologies.

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### References

- Moore, J. E. The birth of topological insulators. *Nature* 2010, 464, 194–198.
- [2] Hasan, M. Z.; Kane, C. L. Topological insulators. *Rev. Mod. Phys.* 2010, *82*, 3045–3067.
- [3] Taskin, A. A.; Sasaki, S.; Segawa, K.; Ando, Y. Achieving surface quantum oscillations in topological insulator thin films of Bi<sub>2</sub>Se<sub>3</sub>. *Adv. Mater.* **2012**, *24*, 5581–5585.
- [4] Peng, H. L.; Dang, W. H.; Cao, J.; Chen, Y. L.; Wu, D.; Zheng, W. S.; Li, H.; Shen, Z. X.; Liu, Z. F. Topological insulator nanostructures for near-infrared transparent flexible electrodes. *Nat. Chem.* 2012, *4*, 281–286.
- [5] Qi, X. L.; Zhang, S. C. Topological insulators and superconductors. *Rev. Mod. Phys.* 2011, 83, 1057–1110.
- [6] Kong, D. S.; Cui, Y. Opportunities in chemistry and materials science for topological insulators and their nanostructures. *Nat. Chem.* 2011, *3*, 845–849.
- [7] Müchler, L.; Casper, F.; Yan, B. H.; Chadov, S.; Felser, C. Topological insulators and thermoelectric materials. *Phys. Status Solidi RRL* 2013, 7, 91–100.

- [8] Wyckoff, R. W. G. Crystal Structures; Krieger: Malabar, FL, 1986.
- [9] Zhang, H. J.; Liu, C. X.; Qi, X. L.; Dai, X.; Fang, Z.; Zhang, S. C. Topological insulators in Bi<sub>2</sub>Se<sub>3</sub>, Bi<sub>2</sub>Te<sub>3</sub> and Sb<sub>2</sub>Te<sub>3</sub> with a single Dirac cone on the surface. *Nat. Phys.* 2009, *5*, 438–442.
- [10] Xia, Y.; Qian, D.; Hsieh, D.; Wray, L.; Pal, A.; Lin, H.; Bansil, A.; Grauer, D.; Hor, Y. S.; Cava, R. J. et al. Observation of a large-gap topological-insulator class with a single Dirac cone on the surface. *Nat. Phys.* **2009**, *5*, 398–402.
- [11] Zareapour, P.; Hayat, A.; Zhao, S. Y. F.; Kreshchuk, M.; Jain, A.; Kwok, D. C.; Lee, N.; Cheong, S. W.; Xu, Z. J.; Yang, A. et al. Proximity-induced high-temperature superconductivity in the topological insulators Bi<sub>2</sub>Se<sub>3</sub> and Bi<sub>2</sub>Te<sub>3</sub>. *Nat. Commun.* **2012**, *3*, 1056.
- [12] Sun, L. P.; Lin, Z. Q.; Peng, J.; Weng, J.; Huang, Y. Z.; Luo, Z. Q. Preparation of few-layer bismuth selenide by liquidphase-exfoliation and its optical absorption properties. *Sci. Rep.* 2014, *4*, 4794.
- [13] Zhang, X.; Wang, J.; Zhang, S. C. Topological insulators for high-performance terahertz to infrared applications. *Phys. Rev. B* 2011, *82*, 245107.
- [14] Zhao, C. J.; Zou, Y. H.; Chen, Y.; Wang, Z. T.; Lu, S. B.; Zhang, H.; Wen, S. C.; Tang, D. Y. Wavelength-tunable picosecond soliton fiber laser with topological insulator: Bi<sub>2</sub>Se<sub>3</sub> as a mode locker. *Opt. Express* **2012**, *20*, 27888– 27895.
- [15] Li, J.; Jiang, F.; Yang, B.; Song, X. R.; Liu, Y.; Yang, H. H.; Cao, D. R.; Shi, W. R.; Chen, G. N. Topological insulator bismuth selenide as a theranostic platform for simultaneous cancer imaging and therapy. *Sci. Rep.* **2013**, *3*, 1998.
- [16] Sun, Y. F.; Cheng, H.; Gao, S.; Liu, Q. H.; Sun, Z. H.; Xiao, C.; Wu, C. Z.; Wei, S. Q.; Xie, Y. Atomically thick bismuth selenide freestanding single layers achieving enhanced thermoelectric energy harvesting. J. Am. Chem. Soc. 2012, 134, 20294–20297.
- [17] Soni, A.; Zhao, Y. Y.; Yu, L. G.; Aik, M. K. K.; Dresselhaus, M. S.; Xiong, Q. H. Enhanced thermoelectric properties of solution grown Bi<sub>2</sub>Te<sub>3-x</sub>Se<sub>x</sub> nanoplatelet composites. *Nano Lett.* 2012, *12*, 1203–1209.
- [18] Min, Y.; Roh, J. W.; Yang, H.; Park, M.; Kim, S. I.; Hwang, S.; Lee, S. M.; Lee, K. H.; Jeong, U. Surfactant-free scalable synthesis of Bi<sub>2</sub>Te<sub>3</sub> and Bi<sub>2</sub>Se<sub>3</sub> nanoflakes and enhanced thermoelectric properties of their nanocomposites. *Adv. Mater.* 2013, 25, 1425–1429.
- [19] Yu, J. K.; Mitrovic, S.; Than, D.; Varghese, J.; Heath, J. R. Reduction of thermal conductivity in phononic nanomesh structures. *Nat. Nanotechnol.* **2010**, *5*, 718–721.
- [20] Son, J. S.; Park, K.; Han, M. K.; Kang, C.; Park, S. G.; Kim,

J. H.; Kim, W.; Kim, S. J.; Hyeon, T. Large-scale synthesis and characterization of the size-dependent thermoelectric properties of uniformly sized bismuth nanocrystals. *Angew. Chem., Int. Ed.* **2011**, *123*, 1399–1402.

- [21] Zuev, Y. M.; Lee, J. S.; Galloy, C.; Park, H.; Kim, P. Diameter dependence of the transport properties of antimony telluride nanowires. *Nano Lett.* **2010**, *10*, 3037–3040.
- [22] Dirmyer, M. R.; Martin, J.; Nolas, G. S.; Sen, A.; Badding, J. V. Thermal and electrical conductivity of size-tuned bismuth telluride nanoparticles. *Small* 2009, *5*, 933–937.
- [23] Linder, J.; Yokoyama, T.; Sudbø, A. Anomalous finite size effects on surface states in the topological insulator Bi<sub>2</sub>Se<sub>3</sub>. *Phys. Rev. B* 2009, *80*, 205401.
- [24] Zhang, Y.; He, K.; Chang, C. Z.; Song, C. L.; Wang, L. L.; Chen, X.; Jia, J. F.; Fang, Z.; Dai, X.; Shan, W. Y. et al. Crossover of the three-dimensional topological insulator Bi<sub>2</sub>Se<sub>3</sub> to the two-dimensional limit. *Nat. Phys.* **2010**, *6*, 584–588.
- [25] Fan, H.; Zhang, S. X.; Ju, P.; Su, H. C.; Ai, S. Y. Flowerlike Bi<sub>2</sub>Se<sub>3</sub> nanostructures: Synthesis and their application for the direct electrochemistry of hemoglobin and H<sub>2</sub>O<sub>2</sub> detection. *Electrochim. Acta* **2012**, *64*, 171–176.
- [26] Yao, J.; Koski, K. J.; Luo, W. D.; Cha, J. J.; Hu, L. B.; Kong, D. S.; Narasimhan, V. K.; Huo, K. F.; Cui, Y. Optical transmission enhacement through chemically tuned twodimensional bismuth chalcogenide nanoplates. *Nat. Commun.* 2014, *5*, 5670.
- [27] Xu, S.; Zhao, W. B.; Hong, J. M.; Zhu, J. J.; Chen, H. Y. Photochemical synthesis of Bi<sub>2</sub>Se<sub>3</sub> nanosphere and nanorods. *Mater. Lett.* **2005**, *59*, 319–321.
- [28] Zhuang, A. W.; Zhao, Y. Z.; Liu, X. L.; Xu, M. R.; Wang, Y. C.; Jeong, U.; Wang, X. P.; Zeng, J. Controlling the lateral and vertical dimensions of Bi<sub>2</sub>Se<sub>3</sub> nanoplates via seeded growth. *Nano Res.* 2015, *8*, 246–256.
- [29] Min, Y.; Moon, G. D.; Kim, B. S.; Lim, B.; Kim, J. S.; Kang, C. Y.; Jeong, U. Quick, controlled synthesis of ultrathin Bi<sub>2</sub>Se<sub>3</sub> nanodiscs and nanosheets. *J. Am. Chem. Soc.* 2012, 134, 2872–2875.
- [30] Zhang, J.; Peng, Z. P.; Soni, A.; Zhao, Y. Y.; Xiong, Y.; Peng, B.; Wang, J. B.; Dresselhaus, M. S.; Xiong, Q. H. Raman spectroscopy of few-quintuple layer topological insulator Bi<sub>2</sub>Se<sub>3</sub> nanoplatelets. *Nano Lett.* **2011**, *11*, 2407– 2414.

- [31] Sun, Z. L.; Liufu, S.; Chen, X. H.; Chen, L. D. Controllable synthesis and electrochemical hydrogen storage properties of Bi<sub>2</sub>Se<sub>3</sub> architectural structures. *Chem. Commun.* 2010, 46, 3101–3103.
- [32] Zhuang, A. W.; Li, J. J.; Wang, Y. C.; Wen, X.; Lin, Y.; Xiang, B.; Wang, X. P.; Zeng, J. Screw-dislocation-driven bidirectional spiral growth of Bi<sub>2</sub>Se<sub>3</sub> nanoplates. *Angew. Chem., Int. Ed.* 2014, *126*, 6543–6547.
- [33] Zhou, J. H.; Zeng, J.; Grant, J.; Wu, H. K.; Xia, Y. N. On-chip screening of experimental conditions for the synthesis of noble-metal nanostructures with different morphologies. *Small* 2011, 7, 3308–3316.
- [34] Jin, S.; Bierman, M. J.; Morin, S. A. A new twist on nanowire formation: Screw-dislocation-driven growth of nanowires and nanotubes. *J. Phys. Chem. Lett.* **2010**, *1*, 1472–1480.
- [35] Penn, R. L.; Banfield, J. F. Imperfect oriented attachment: Dislocation generation in defect-free nanocrystals. *Science* 1998, 281, 969–971.
- [36] Hirth, J. P.; Lothe, J. *Theory of Dislocations;* MaGraw-Hill: New York, 1968.
- [37] Burton, W. K.; Cabrera, N.; Frank, F. C. Role of dislocations in crystal growth. *Nature* **1949**, *163*, 398–399.
- [38] Xia, Y. N.; Xia, X. H.; Peng, H. C. Shape-controlled synthesis of colloidal metal nanocrystals: Thermodynamic versus kinetic products. J. Am. Chem. Soc. 2015, 137, 7947–7966.
- [39] Meng, F.; Morin, S. A.; Forticaux, A.; Jin, S. Screw dislocation driven growth of nanomaterials. *Acc. Chem. Res.* 2013, 46, 1616–1626.
- [40] Markov, I. V. Crystal Growth for Beginners: Fundamentals of Nucleation, Crystal Growth, and Epitaxy; World Scientific Publishing Co. Pte. Ltd.: Singapore, 1995.
- [41] Zhuo, R. F.; Feng, H. T.; Chen, J. T.; Yan, D.; Feng, J. J.; Li, H. J.; Geng, B. S.; Cheng, S.; Xu, X. Y.; Yan, P. X. Multistep synthesis, growth mechanism, optical, and microwave absorption properties of ZnO dendritic nanostructures. *J. Phys. Chem. C* 2008, *112*, 11767–11775.
- [42] Shevchenko, E. V.; Talapin, D. V.; Schnablegger, H.; Kornowski, A.; Festin, Ö.; Svedlindh, P.; Haase, M.; Weller, H. Study of nucleation and growth in the organometallic synthesis of magnetic alloy nanocrystals: The role of nucleation rate in size control of CoPt<sub>3</sub> nanocrystals. *J. Am. Chem. Soc.* 2003, *125*, 9090–9101.